

# **Linear Pendulum Rangefinder for Education**

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## **Abstract**

The apparatus produced in this project can measure physical quantities of a pendulum bound by small amplitudes. This device is intended as an educational model for SHM, specifically that of a linear pendulum. The device produced can measure distances and periods of an oscillating pendulum. The data collected by the device can then be graphed.(e.g., by physica)

The device utilizes a rangefinder. The rangefinder emits ultrasonic pulses which are received again by the rangefinder. Then, the rangefinder creates a high on its output; proportional to the time between the emission and detection of the ultrasonic pulse. By measuring the time the output stays high, one can determine the distance the pulse had to travel, and thus the distance of an object.

To measure the period, a simple stopwatch was implemented. The stopwatch initially records the distance of a given object, then records the time until the stop button is pushed. This creates data of amplitude vs time.

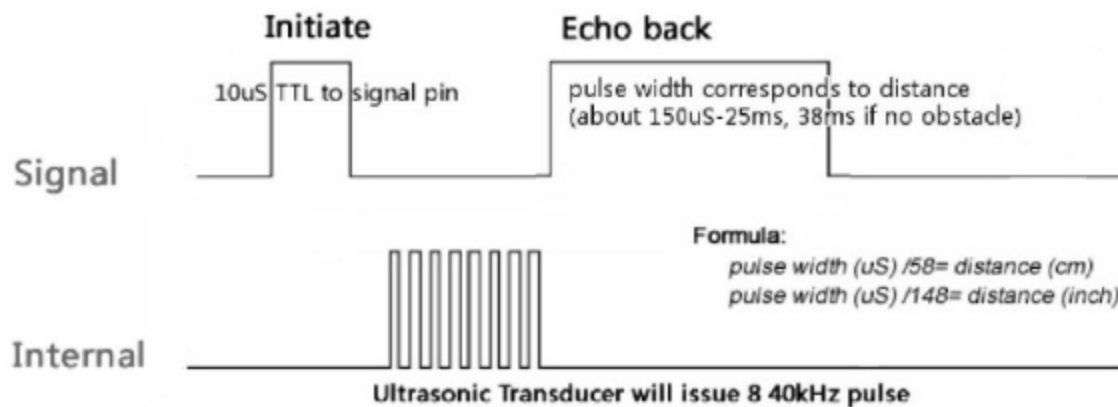
This device was created as an educational model for SHM. A linear pendulum was chosen because basic physical properties are observable in the model(e.g., the amplitude should never increase due to conservation of energy), as well as some properties specific to a pendulum. However, the device will also operate on other apparatus, such as a spring oscillator.

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## 1.1:Introduction:

The sensor used in the project is a HC-SR04 Ultrasonic rangefinder. The device operates by emitting a bundle of ultrasonic pulses from an emitting device. This is done by setting the trigger high for a certain amount of time (~20 $\mu$ s was used in this project). Then, upon receiving the bundle of pulses in the receiving device, the sensor outputs a high signal on the echo output. The duration of the signal is equal to the time between the emission of the bundle and the reception of said bundle. From this, one can determine the distance by using a calibrated counter. In this project, the counter is calibrated to cycle every 5.8 $\mu$ s. This gives the distance in millimeters. A timing diagram is shown below in figure 1.1.0.

Figure 1.1.0 HC-SR04 Timing Diagram



Taken from Cytron Technologies: *HC-SR04 User's Manual*

The purpose of the device constructed in this project is to model the SHM of a linear pendulum. The device produced can model the position,  $x(t)$ , of a pendulum or spring oscillator by providing data points; which can then be graphed. In addition, a stopwatch function has been included. This is to measure the period of oscillation, however it requires manual control.

This device measures distance fairly precise and accurately and could be used for quantitative analysis. However the period measurements, hence relying on the judgment of the user, should not be used quantitatively. Instead, the period should be determined graphically.

The device produced in this project is a distance measuring device. The device measures distance in millimeters, and outputs the data, along with a trial number, to the PICLab output. The trial number is added for graphing purposes. An example of this is shown below in figure 1.1.1. This process is automated. This mode is selected by pressing any button excluding reset and switch 2 on the Picboard.

Figure 1.1.1 Example Data Mode 1; left column = trial number, right column=distance(mm)

Read PIC	Open	Clear	Save
269	292		
270	302		
271	308		
272	321		
273	331		
274	350		
275	350		
276	330		
277	318		
278	311		
279	299		
280	307		
281	264		
282	246		
283	232		
284	223		
285	199		
286	200		
287	180		

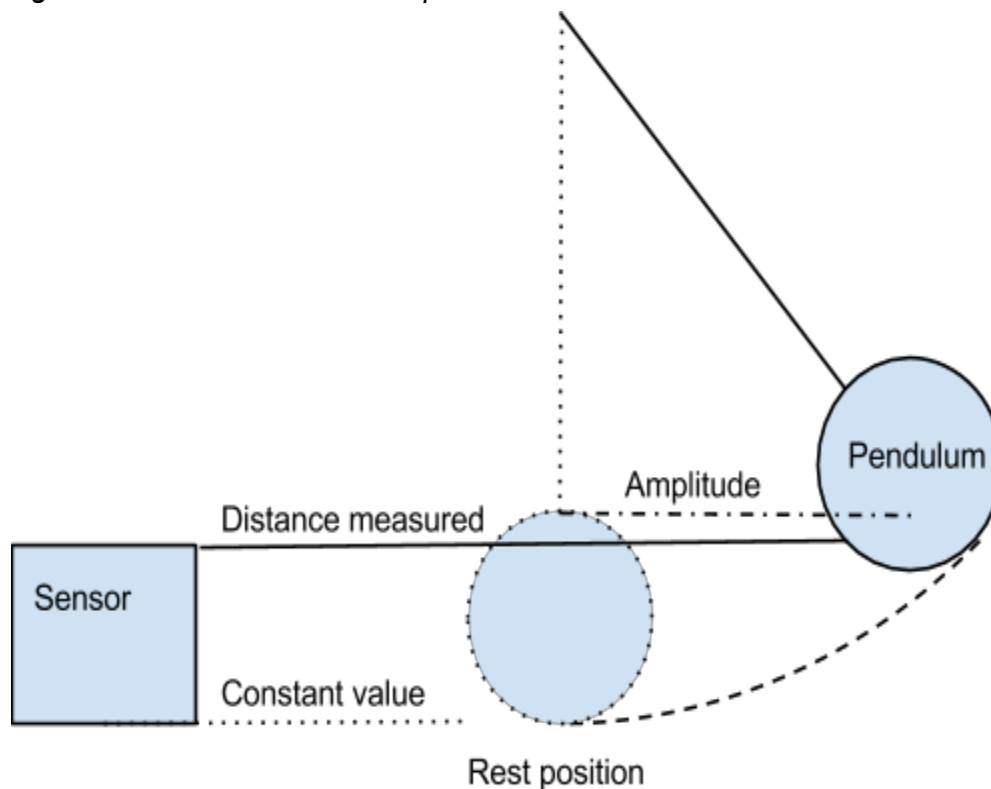
In addition to the distance measuring technique mentioned above; this device can also measure the period of an oscillation. The program first measures the distance between the object in question and the Picboard. Then, a counter is run until a button (switch 2) is released. The counter measures in milliseconds. This mode is selected by pressing switch 2 and is manual. An example of the data collected via this mode of operation is shown in figure 1.1.2.

Figure 1.1.2 Example Data Mode 2; left column=distance(mm), right column=time(ms)

Read PIC	Open	Clear	Save
87	1143		
121	497		
448	479		
109	465		
159	555		
311	400		
2636	426		
454	453		
337	529		
232	530		
139	433		
105	2579		
88	610		
90	113		
86	109		
90	96		
86	95		
86	101		
90	3115		
202	852		
336	544		
453	529		
162	1296		
57	464		
50	353		
170	4769		

In terms of the oscillation of a pendulum, this distance will be the amplitude of oscillation, plus some constant distance (see figure 1.2.3). For the intended purposes of this mode of operation, it is not necessary to find the actual amplitude. It is only necessary to show that the amplitude may have changes between data points.

Figure 1.2.3 Constant Value Explanation



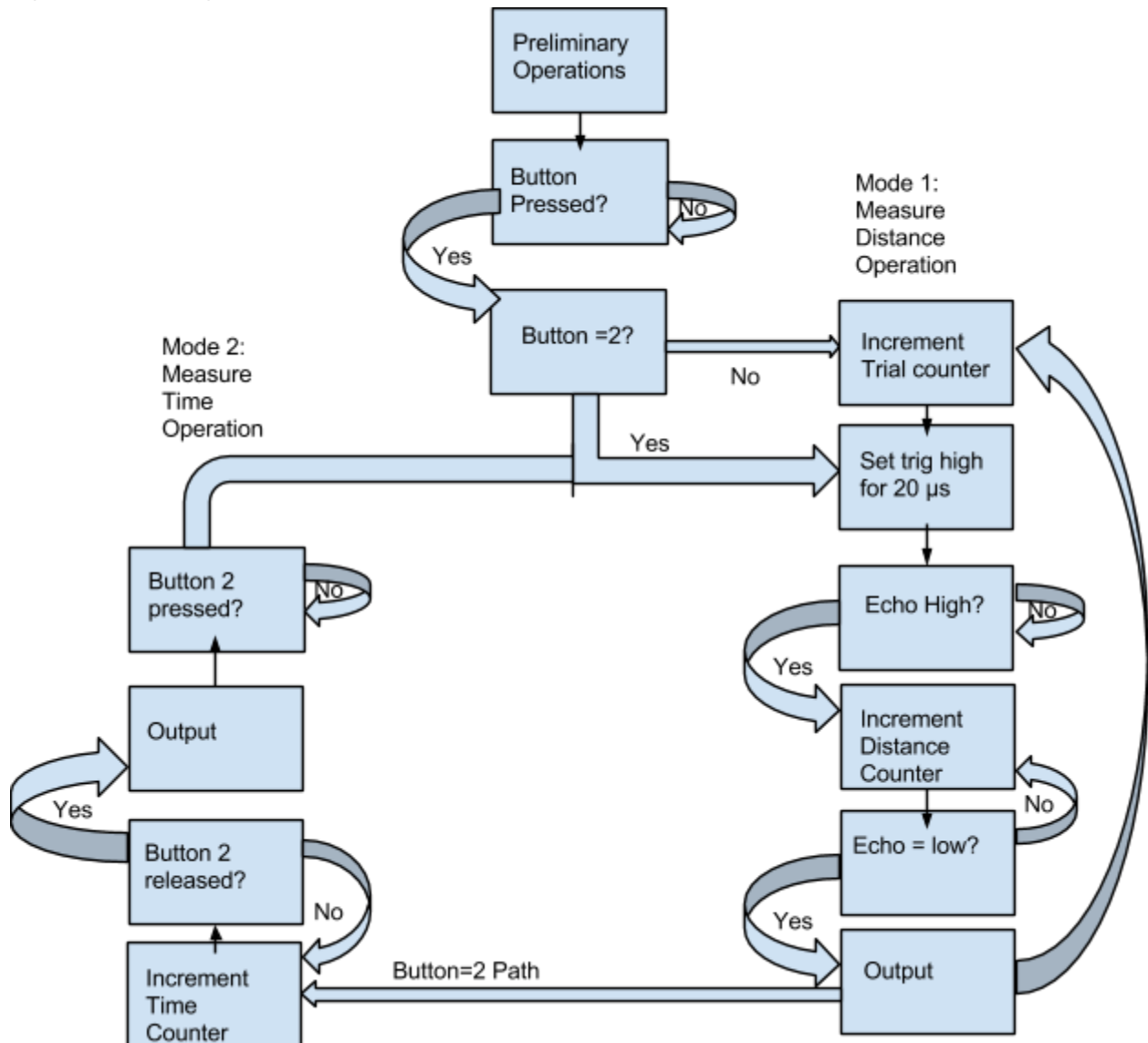
N.B Angle in this diagram is exaggerated.

The device can model the equation  $x(t) = A \sin(\omega t + \phi) + C$  i.e., the position equation for SHM; which is an important model in physics. The data has a small error, but not negligibly small. It also shows how much a simple measurement, such as the position, can do i.e., show conservation of energy, calculate amplitude, determine  $v(t)$ ,  $a(t)$ , etc. This is important to those just introduced to physics, as it has a stigma of being difficult; in reality most things are fundamentally simple. The data output of the rangefinder synergies well with Physica. The device is also simple to use, having only a few operation buttons. For these reasons, this device makes an ideal educational tool for introductory mechanical physics.

## 1.2: The Program:

The program can be explained with the flowchart, figure 1.2.1. This device operates

Figure 1.2.1 Program Flowchart



N.B some checking and clearing steps are omitted for compactness.

The entire program appears as:

Rangefinder

;Effective angle 30 degrees

;Distance between 2cm-4m

;First, create a pulse

TRIG equ 1; Define Trigger and

ECHO equ 2; Echo channels incase  
; they change on board

Selector1 equ 0x26

THold equ 0x20

EHold equ 0x21

ECount1 equ 0x22

ECount2 equ 0x23

Graph1 equ 0x24

Graph2 equ 0x25

TimerC1 equ 0x27

TimerC2 equ 0x28

Bank1 ;Setting the Trigger

bcf TRISE,TRIG ; set channel trigger to an output

bsf TRISE,ECHO ; set channel Echo to input

Bank0; end of preliminary operations

Selector call Getkey; to select timer or distance

movwf Selector1

movf Selector1,W

sublw 7

btfsc STATUS,Z

goto Selector

movf Selector1,W

sublw 2; pushing 2 selects timer

btfsc STATUS,Z

goto Timer

clrf Graph1 ; clearing trial counters

clrf Graph2

;mode 1

Triggermovlw 250 ; This is for points per seconds, It is just to delay between data points  
call Wait

incf Graph1 ; increment LSD counter  
btfsc STATUS,Z ; if LSD = 0, increment  
incf Graph2 ; MSD counter  
movf Graph1 W  
iorwf Graph2 W ; Test for 0 state, omitted from flowchart  
btfsc STATUS,Z  
goto END; end operation if 0 state  
movf Graph1 W  
movwf WL ; move counter 1 value to WL register  
movf Graph2W  
movwf WH ; move counter 2 value to WH register  
call Bin2BCD  
movlw 4; this selects the amount of trials possible  
call BCD2TCL  
movlw 0x20  
call TxByte; at this point, the output is ready for a distance measurement

bsf PORTE,TRIG ; ;Need to set Trigger high for ~20us  
movlw 32 ; Delay device  
movwf THold

TWait decfsz THold; to delay signal deactivation  
goto TWait

clrf ECount1; clear counters  
clrf ECount2  
bcf PORTE,TRIG; Set trigger output low

;For Echo, we want distance to be in reasonable units  
;As distance =  $340/2 \cdot t$ , if we want dist. in mm then  $t = 5.8823\mu s$   
;therefore we want Echo clock to take 5880ns per cycle  
;but cycles only in intervals of 200ns, so 5800ns



```

TIH    movlw 3; this is to test if the echo input is high from the sensor
        movwf EHold
DELAY  decfsz EHold
        goto  DELAY
        nop
        btfss PORTE,ECHO; Test if high
        goto  TIH

```

;Distance counter begins now

```

Echo    movlw 5 ; For delay to make 5800ns
        movwf EHold; to store delay value
        nop; for delay
        incf   ECount1 ; increment LSD counter
        btfsc  STATUS,Z ; if LSD = 0, increment MSD counter
        incf   ECount2 ; MSD counter
        movf   ECount1 W
        iorwf  ECount2 W ; Test for 0 state
        btfsc  STATUS,Z
        goto   END; end if 0 state

```

```

EWait  decfsz EHold ;
        goto   EWait ; for delay
        nop
        btfss  PORTE,ECHO; Test if Echo is high, skip if yes
        goto   Output ; go to output if ECHO is low
        goto   Echo ; go to counter function 'Echo' if Echo input is high

```

```

Output movf   ECount1 W
        movwf WL    ; move counter 1 value to WL register
        movf   ECount2    W
        movwf WH    ; move counter 2 value to WH register
        call   Bin2BCD
        movlw  5
        call   BCD2TCL
        movlw  '\n'
        call   TxByte; new line, output ready for new trial
        goto   Trigger; loop to trial counter

```

; end of mode 1

;mode 2

```
Timer  call    Getkey; test to see if 2 is pressed
        sublw  2
        btfss  STATUS,Z
        goto   Timer
        clrf   TimerC1; clearing counters of data
        clrf   TimerC2;
```

; This is a repeat of the above distance counter

```
        bsf    PORTE,TRIG ; Set trigger output high
        movlw  32 ; Delay device
        movwf  THold
```

```
TWW decfsz THold; to delay signal deactivation
    goto  TWW
```

```
        clrf   ECount1; clear counters
        clrf   ECount2
        bcf    PORTE,TRIG; Set trigger output low
```

;total execution time between bsf and bcf is 10us. so  $x = (10000 - (5 \cdot 200)) / (200 \cdot 3) = 15$

;For Echo, we want distance to be in reasonable units

;As distance =  $340/2 \cdot t$ , if we want dist. in mm then  $t = 5.8823\mu s$

;therefore we want Echo clock to take 5880ns per cycle

;but cycles only in intervals of 200ns, so 5800ns

```
DLAY  movlw  3
```

```
        movwf  EHold
```

```
DELAY1 decfsz EHold
```

```
        goto   DELAY1
```

```
        btfss  PORTE,ECHO; Test if high
```

```
        goto   DLAY
```

```
Echo1 movlw  5 ; For delay
```

```
        movwf  EHold; to store delay value
```

```
        nop
```

```
        incf   ECount1 ; increment LSD counter
```

```
        btfsc  STATUS,Z ; if LSD = 0, increment
```

```
        incf   ECount2 ; MSD counter
```

```
        movf   ECount1 W
```

```

iorwf  ECount2 W ; Test for 0 state
btfsc  STATUS,Z
goto   END; error if 0 state

EWait1      decfsz EHold ;
            goto   EWait1 ; for delay
            nop
            btfss  PORTE,ECHO; Test if Echo is high, skip if yes
            goto   Output1 ; go to output if ECHO is set
            goto   Echo1 ; go to counter function 'Echo' if ECHO is low ;14

Output1      movf  ECount1 W
            movwf  WL    ; move counter 1 value to WL register
            movf  ECount2    W
            movwf  WH    ; move counter 2 value to WH register
            call   Bin2BCD
            movlw  5
            call   BCD2TCL
            movlw  0x20
            call   TxByte; move amplitude to graphing output
            goto   TTT

TTT          call   Getkey; test to see if 2 is released, stop counter if 2 released
            sublw  7
            btfsc  STATUS,Z
            goto   Output2; if yes output time
            incf   TimerC1 ; increment LSD counter 6
            btfsc  STATUS,Z ; if LSD = 0, increment
            incf   TimerC2 ; MSD counter
            movf   TimerC1 W
            iorwf  TimerC2 W ; Test for 0 state
            btfsc  STATUS,Z
            goto   END; error if 0 state
            nop ; for time delay
            movlw  89
            movwf  THold; 15 instruction cycles
; We want nice time units 1ms,(16+ 89*56)200ns =5(200)us=1ms

TW          movlw  17
            movwf  EHold
TWT          decfsz EHold
            goto   TWT;

```

```

nop; for missing goto cycle
decfsz THold
goto TW; one TW loop is 17*3 + 5 =56 instruction cycles
goto TTT; on last instruction, additional cycle here so 16 +89*56 cycles

```

```

Output2      movf  TimerC1 W
              movwf WL      ; move counter 1 value to WL registrar
              movf  TimerC2      W
              movwf WH      ; move counter 2 value to WH registrar
              call  Bin2BCD
              movlw 5
              call  BCD2TCL
              movlw '\n
              call  TxByte; ready for new data
              goto  Timer; loop to timer
;end of mode two

```

END return; for ending purposes

### **1.3: User Manual:**

1. load the program into the Picboard
2. Select a mode of operation. Switch 2 selects mode 2, any other button selects mode 1
3. If mode one is selected, press the reset button when the desired amount of trials are conducted and/or before the upper limit of trials is reached.
4. If mode 2 selected, hold down button 2 until desired time period is achieved, then release button 2.
5. Press button 2 again and repeat instruction 4 to conduct another trial. Press the reset button when the desired amount of trials have been conducted.

\*Device best operated within 30 degrees, operational range 2-400cm. For best performance, an object of area at least 0.5m<sup>2</sup>, not made of an acoustically absorbent material, should be used for detection.

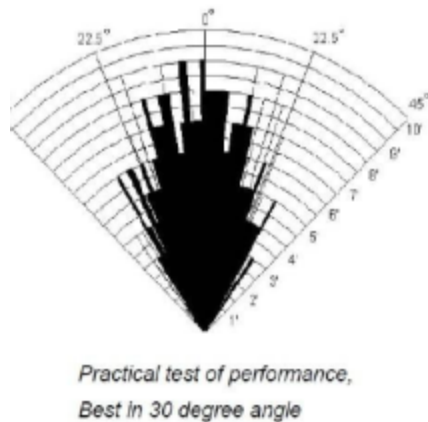
\*Taken from Cytron Technologies: *HC-SR04 User's\_Manual*

## **1.4: Device Properties and Limitations**

When tested on a reasonably sized object (a picboard), the operational range of the rangefinder is greatly reduced. An object of similar size to a picboard should surpass no more than 50cm from the rangefinder and should not come closer than 2cm.

From the manufacturer, the performance vs angle measurement is shown in figure 1.4.1. It can be said that the device operates most effectively within 15° from the axis of measurement.

*Figure 1.4.1 Performance vs Angle*



Taken from Cytron Technologies: *HC-SR04 User's Manual*

The precision and accuracy of distance measurements is quite high, typically varying  $\pm 1\text{mm}$ , as shown in figure 1.4.2. The measurement listed in figure 1.4.2 is of a distance  $\approx 30\text{cm}$ . Due to disciples in the origin i.e., it is difficult to determine the actual location of the sensor, all that may be said of the accuracy of the device is that it is accurate to within 5mm w.r.t. the picboard. When analysing the accuracy of the device, the resolution of the counter should be considered. The test, for the echo output to go high, has an associated resolution of 13 instruction cycles. Also, the counter itself has an associated resolution of 29 instruction cycles. This creates an error of about  $\pm 1.428\text{mm}((13+29)*200*10^{-9}*340/2)$ . In addition, the device has associated errors with the speed of sound in air, as this is variable and dependant on environment. Additionally, there is a rounding error associated with the counter cycle. The actual period of the cycle should be  $5.8823\mu\text{s}$  ( $d=v/2*t \rightarrow t=2*10^{-3}/340$ ). This implies that the counter has an overestimation of about 1.42%( $5.8823/5.8$ ).

*Figure 1.4.2: PICLab Output Data at 30cm*

Read PIC	Open	Clear	Save
1056	301		
1057	302		
1058	302		
1059	302		
1060	302		
1061	300		
1062	302		
1063	301		
1064	302		
1065	301		
1066	302		
1067	302		
1068	301		
1069	302		
1070	301		
1071	302		
1072	301		
1073	302		
1074	301		
1075	302		
1076	301		
1077	302		
1078	302		
1079	302		
1080	302		
1081	300		
1082	302		
1083	301		
1084	302		
1085	300		
1086	302		
1087	301		
1088	302		
1089	302		
1090	300		
1091	302		
1092	301		
1093	302		
1094	301		
1095	302		
1096	301		
1097	302		
1098	302		
1099	302		
1100	302		
1101	301		

The time resolution of the device, in the distance measuring mode, is variable and may be approximated by  $38.75\text{ms} + (5.8\mu\text{s} \times \text{distance})$ . The constant term is due to the wait function applied at the beginning of the program. The variable term is the time required to count to a specific distance. This gives a minimum time resolution of about 38.9ms and a maximum of 0.419s.

It should be noted that the maximum distance, time and trial values which may be obtained is  $2^{16}-1$ . However, for the applicational purposes of the device, these values would never be obtained. In practice, the distance values should never surpass 4m and 9999 trials is sufficient for any sized pendulum or oscillator.

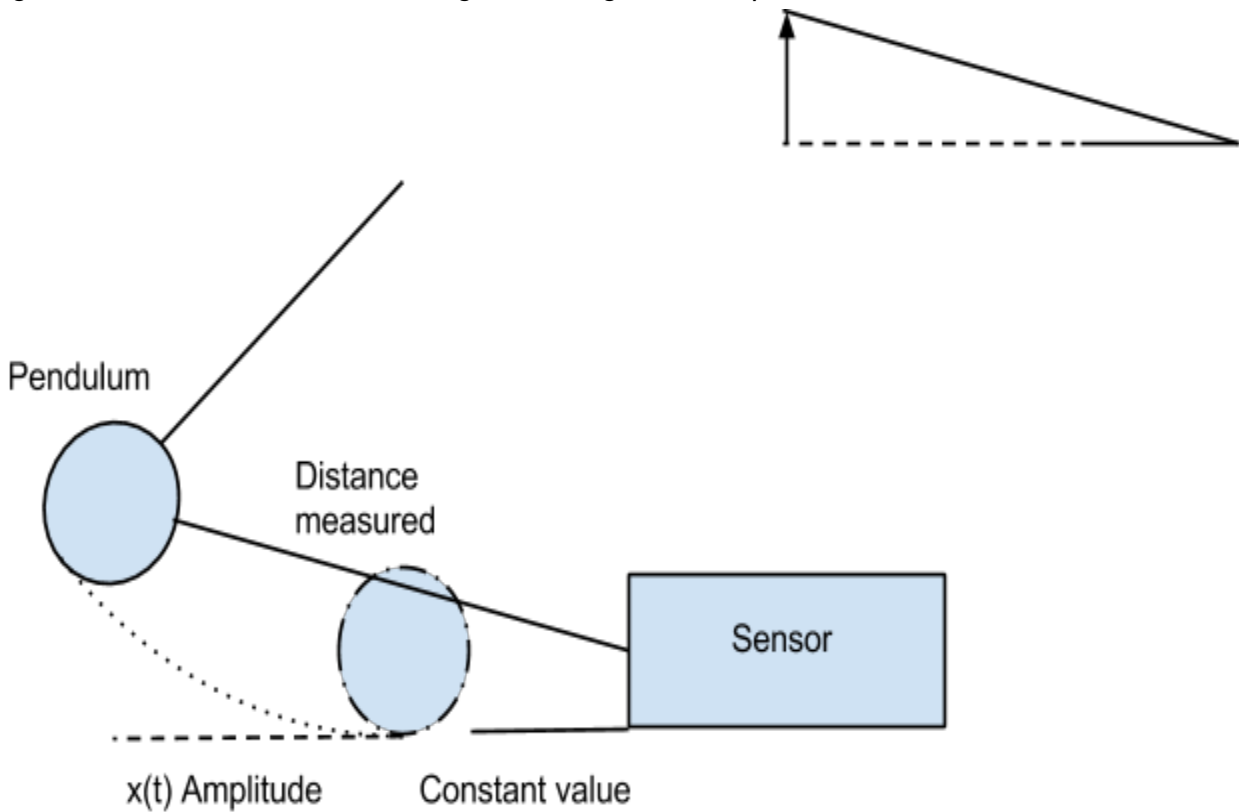
The accuracy and precision of mode 2, the timing mode, is not determinable; due to the dependance of a human input (pressing and releasing the button). Thus, it is not viable to use the measurements obtained for qualitative purposes. The feature was included only to show the independance of period from amplitude for the linear pendulum (i.e., to be able to change the amplitude in the same data set). To calculate the actual period, it is advised that one uses mode 1 to acquire distance data and utilize a graphing program capable of fitting functions to data (e.g., Physica).

### **1.5: Pendulum Demo:**

The equation of a linear pendulum,  $x(t) = A \sin(\omega t + \phi) + C$ , is only applied for linear pendulums. For the purpose of a demonstration of mode one, small angle approximation will be used; so that the data will approximate a linear pendulum well. In addition, if the amplitude of the pendulum is too large, the rangefinder will not be able to detect it, as it will pass the optimal angle threshold.

The period of a linear pendulum can be found with the following equation:  $T = 2\pi(l/mgL)^{1/2}$ . in the case of a simple pendulum, this reduces to  $T = 2\pi(L/g)^{0.5}$ . The period of a non-linear, simple pendulum is  $T = 2\pi(L/g)^{0.5} \sin(\theta)$  (Period equation taken from Georgia State University, HyperPhysics). This implies the period should remain constant, within experimental error, until a sufficient amplitude is exceeded. This will be tested by the second mode of operation. Note that the amplitude values obtained in mode two will not reflect actual amplitude values. This is especially true once the amplitude begins to affect the period, as this is when the small angle approximation is no longer valid. This is shown in figure 1.5.1. As the sum of the vectors is not zero, the amplitude measurements would be off if the constant value method was used, hence the data the rangefinder gives is a magnitude only.

Figure 1.5.1 The Effect of Exceeding Small Angles on Amplitude



## 1.6: References:

Cytron Technologies: *HC-SR04 User's Manual*,

[https://docs.google.com/document/d/1Y-yZnNhMYy7rwhAgyL\\_pfa39RsB-x2qR4vP8saG73rE/e/dit?pli=1](https://docs.google.com/document/d/1Y-yZnNhMYy7rwhAgyL_pfa39RsB-x2qR4vP8saG73rE/e/dit?pli=1)

Georgia State University, HyperPhysics, *Mechanics: Periodic Motion*;

<http://hyperphysics.phy-astr.gsu.edu/hbase/permot.html#permot>