

SCAD Soft

Structure CAD software system
for Windows 95/98/NT

SCAD **Structure**

K U S T

Oscillations, Stability, Statics
Version 1.1

User manual

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Team of authors

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«KUST». Oscillations Stability Statics. USER MANUAL. Version 1.1.

The manual contains a description of the functionality of the KUST software, its technologies, and recommendations on its usage.

The software is oriented at engineers and designers who have basic skills with personal computers.

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General information

The reference manual program **KUST** is developed by the **SCAD Soft** company and included in the **SCAD Office** software package. It solves particular classes of mechanical problems for which there exist analytical or sufficiently accurate approximate solutions published in literature on the subject.

Though the majority of these problems can be also solved by the SCAD software, involving KUST will enable one to get a solution without building any design finite-element models. Also, some of results obtained by KUST can be used to specify source data when building a finite-element model (such data as coefficients of effective length, estimates of natural frequencies etc.).

All problems which the program is capable of solving can be classified into the following categories:

- ◆ stability of equilibrium;
- ◆ frequencies of natural oscillations;
- ◆ other oscillation problems;
- ◆ static calculations;
- ◆ auxiliary calculations.

Formulations of most of the problems in question are quite clear, therefore for each problem this manual gives only brief statements, lists of source data needed, and results to be obtained by solving it. More details can be found in literature referred to in each section.

Interface

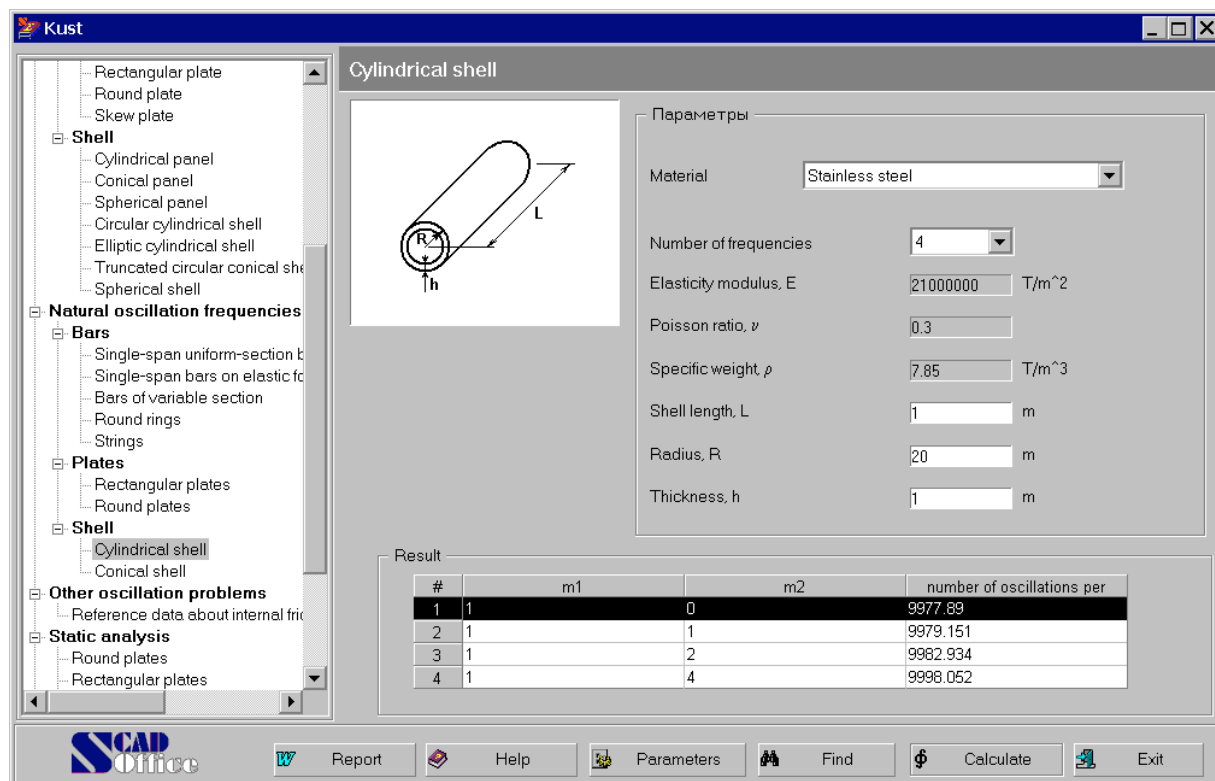


Fig. 1. The main window of the **KUST** program

The main window of the **KUST** program has the same set of controls in all working modes; these controls include:

- a tree of problems used to select a type of the analysis;
- edit fields to specify source data;
- fields where results of the analysis will be displayed;
- functional buttons to activate the analysis and invoke various control actions (start the analysis, form a report, open the reference help, ...).

Problem tree

The problem tree has three levels of hierarchy. The first, highest, level contains names of problem groups such as STABILITY OF EQUILIBRIUM or NATURAL OSCILLATION FREQUENCIES. The second level contains types of constructions such as Bars, Plates; the third level suggests particular problems. To invoke a problem type, place the mouse pointer onto its title and left-click.

Edit fields

When editing data in the edit fields, you can enter numbers as fixed-point values (such as 0.214) or in a scientific notation (such as 1.23e5). The integer and the fractional parts are separated by a period. A comma can be used, too, but this must be set up in the Windows environment settings. The data entered in the fields are checked when the analysis is activated.

Functional buttons

Functional buttons are used to invoke the following control actions:

Calculate to invoke actions of source data checking and performing the calculation itself;

Report to form a report containing results of the calculation/analysis;

Settings to activate a program setup mode (see below);

Help to get reference help information about **KUST**;

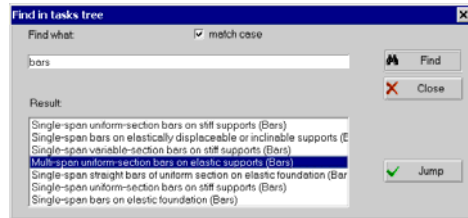


Fig. 2. The
Search the problem tree dialog box

Find to search the problem tree for a context in a problem's name. The search is done using the **Search the problem tree** dialog box (Fig. 2) where you should specify a text to search for and click the **Find** button. This will open a list of all problems the titles of which contain the specified text in the **Search results** list. Place the mouse pointer onto the desired problem and click the **Go to** button; the focus of the tree will switch to the problem pointed to. To proceed with the analysis, close the search dialog box.

Exit to end the active working session and exit the program.

Calculate

To perform the calculation, select a problem in the problem tree, specify source data for it in the edit fields, and click the **Calculate** button.

Controls

Principles of control implemented in the software are intended to provide the unified dialogue functions. This software uses a common dialog box technique. The following controls and ways of data access are used:

- ◆ functional buttons “clicking” which (by placing the mouse pointer onto a button and clicking the left mouse button) takes you to particular modes or actions;
- ◆ selection tools of various kinds which enable you to choose one or more of suggested options;
- ◆ data edit fields using which you specify source data for the analysis. Source data consist of numbers. If a non-integer number is entered, its integral and fractional parts are separated with a period or another separator. The separator is assigned by the user during the setup of the operating system (see **Settings | Regional Settings | Number**). Number can be entered also in the scientific notation, for example, as 1.56e-7;
- ◆ drop-down and static lists from which to select data;
- ◆ tables to enter or display tabular information;
- ◆ dynamically digitized diagrams that display values of functions for an argument pointed to by the mouse pointer on the screen.

Material properties

Many of the problems solved by **KUST** require you to specify physical properties of materials that a structure is made of. In most cases this information can be specified in a unified way. There is a drop-down list (see Fig. 3) from which you can choose the desired material.

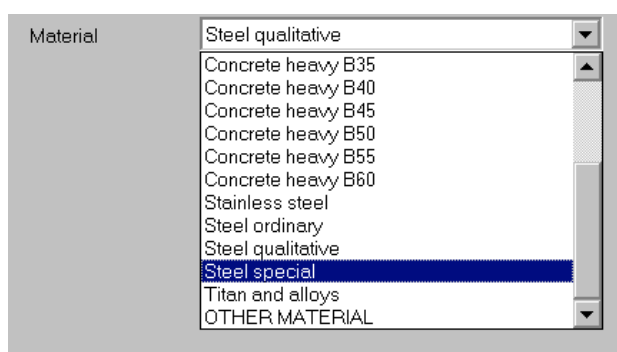



Fig. 3. The **Materials** drop-down list.

When you select a material in the list, all properties will be retrieved from a database shipped with the software. To check your selection, the program will display the properties of the selected material (such as the elasticity modulus, Poisson ratio etc.). If you select the bottom item of the list, “OTHER MATERIAL”, the respective edit fields will be enabled so that you can enter mechanical properties of the material absent in the database manually. Before doing the analysis, the program will check the correctness of the information entered (for example, no Poisson ratio greater than 0.5 can be specified).

Moments of inertia

In many cases (when a bar structure is under consideration) the source data for the analysis include moments of inertia of a cross-section. If the structure is made of standard rolled stock, the specification of those data is simple. There is a service activated by the button . This will open a dialog box (see Fig. 4) that contains a tree of rolled profiles. Having selected a desired profile, the user will get the information about the moments of inertia with respect to the Y and Z axes of the selected profile (the X axis is assumed to be collinear with the bar's axis). Clicking one of the **Apply** buttons located near I_y and I_z will put the moment of inertia information automatically to

the respective edit field.

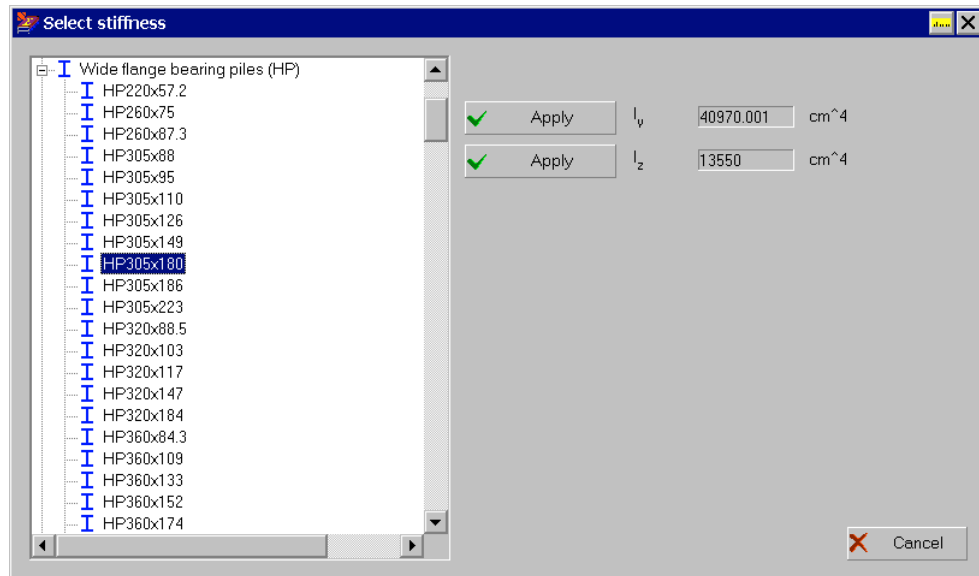


Fig. 4. The **Select stiffness** dialog box

Settings

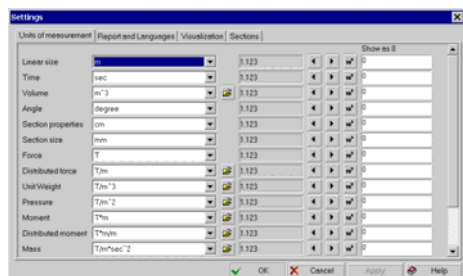






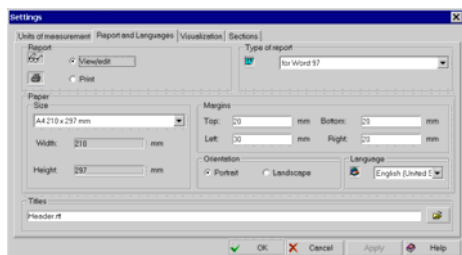
Fig. 5. The **Units of measurement** tab

This dialog can be invoked at any moment when working with **KUST**. It is used to set up general properties of the working environment. The dialog contains the following tabs: **Units of measurement**, **Reports and languages**, and **Visualization**.

Each of the tabs opens a page on which you can adjust certain types of the program settings.

The **Units of measurement** tab (Fig. 5) helps define units of measurements to be used in the analysis. It contains two groups of data. The first group is used to specify units that measure sizes of structures, forces, moments etc. For compound units (such as pressure), there is a possibility to define their component units (those for forces and for linear sizes) separately using the  button. The second group enables you to choose a representation and precision for numerical data. Special controls are used here to select data representation formats. Make sure to specify the amount of significant digits in either the fixed-point decimal representation or the floating-point scientific notation.

The precision of the data representation (the number of significant digits after the decimal point) can be assigned using the buttons  (decrease) and  (increase), while the scientific notation is turned on by the button . Also, you can specify in respective edit fields what value of a unit of measurement should be treated as “very small”, so quantities less than that by their absolute magnitudes will be displayed as 0 in all visualizations.

Fig. 6. The **Report and languages** tab

The **Report and languages** tab (Fig. 6) enables you to choose a language in which to represent all texts in dialog boxes and to generate a report.

Working with the report document can be done in one of two modes: **View/Edit** or **Print**.

When in the **View/Edit** mode, clicking the **Report** button in any active dialog will open the report on the screen and let you view/edit it. An application associated with **RTF** (Rich Text Format) files will be launched to serve this purpose, such as **WORDPAD** or **WORD**. Obviously, it is the user who is fully responsible for any changes made to the text of the report (note that even results of the calculation can be edited). There are differences in **RTF** formats used by **MS Word v.7** and **WordPad**, on one hand, and **MS Word 97 (2000)**, on the other hand. Because of this, the program lets the user choose one of the **RTF** formats in the **Report type** mode.

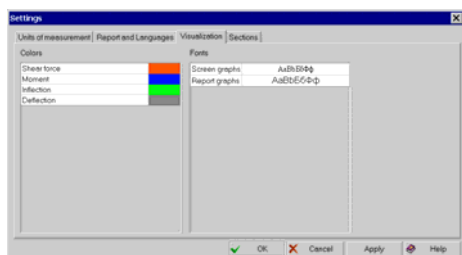
Clicking the **Print** button in the **Report** group will print the report in the form it has been generated by the editor.

Use the **Headers/Footers** edit field to specify (or to choose from the list after clicking the appropriate button) an **RTF** file containing headers and footers for pages of the report document.

Note. If you wish to modify the RTF file of headers/footers shipped with the editor using MS Word, remember it is not enough just to enter a new text; you need also to select the **Tools | Language | Set Language** menu item and set the language for the new text to *Russian*.

The **Paper size** control enables you to select a format for the paper on which to print the report (the size can be selected from a drop-down list).

In addition, you can set up the margins and the page orientation for the report document.

Fig. 7. The **Visualization** tab

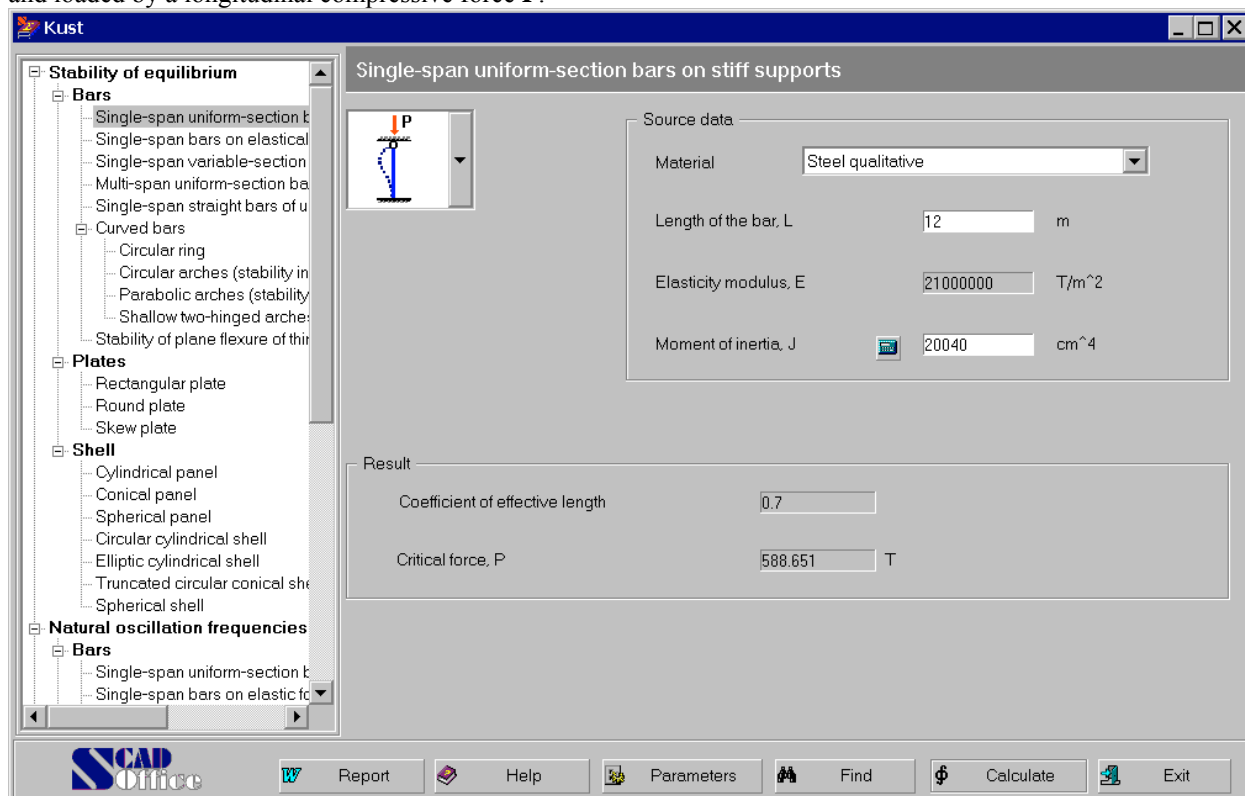
The **Visualization** tab (Fig. 7) contains two groups of controls, **Colors** and **Fonts**. Each of these include a list of controls with associated attributes (colors or fonts). Double-clicking with the right mouse button opens a standard Windows dialog for font or color selection.

Stability of equilibrium

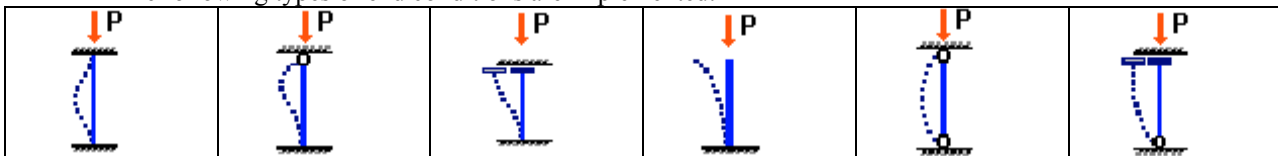
This section comprises problems related to the stability of equilibrium of various constructions (critical forces/stresses and effective length coefficients for bar elements). In the case of a shell-like structure, it is a rule to determine the *top* critical load (i.e. the maximum load up to which the basic equilibrium is stable against small disturbances; this is known as a stability in small).

1. Single-span uniform-section bars on stiff supports


The object of analysis is a single-span bar of a uniform section attached to stiff supports in various ways and loaded by a longitudinal compressive force P .



The following types of end conditions are implemented:



The source data for this analysis include the length of the bar, the moment of inertia of its cross-section in the plane where the buckling is expected, the elasticity modulus (this one can be specified by selecting a material from the database or by entering an explicit value if the OTHER MATERIAL option has been selected in the material list).

If the cross-section is a rolled profile, the moment of inertia can be retrieved from the profile database using the button  described earlier in the “Moments of inertia” section.

The result of the analysis will be the coefficient of effective length (the effective length to the actual bar's length ratio) and the critical force value.

References

[1] S. Timoshenko, D. Gere, *Mechanics of Materials*, St.-Petersburg—Moscow, “Lan” Publishers, 2002, 669 pp. In Russian.

2. Single-span bars on elastically displaceable or inclinable supports

The object of analysis is a single-span bar of a uniform cross-section placed on elastically displaceable or/and inclinable supports and attached to those in a variety of ways; the bar is loaded by a longitudinal compressive force P .

The screenshot shows the Kust software window titled "Single-span bars on elastically displaceable or inclinable supports". On the left is a tree view with categories: Stability of equilibrium (Bars, Curved bars, Plates, Shell), and Natural oscillation frequencies (Bars). The main area contains input fields for source data and stiffness, and a result section.

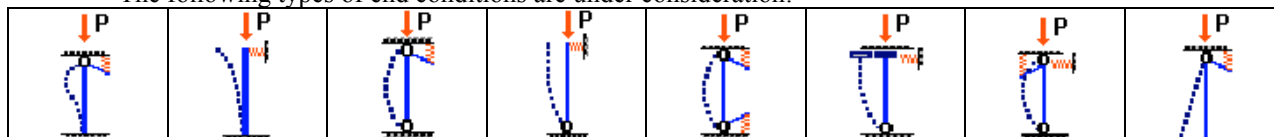
Source data	
Material	Steel ordinary
Length of the bar, L	2 m
Elasticity modulus, E	21000000 T/m ²
Moment of inertia, J	115 cm ⁴

Stiffness elastic support	
Top Cm	2265262.204 T*m
Bottom Cm	0 T*m
Top Cn	2000 T
Bottom Cn	0 T

Result	
Coefficient of effective length	2
Critical force, P	14.897 T


At the bottom, there is a toolbar with icons for Report, Help, Parameters, Find, Calculate, and Exit.

The following types of end conditions are under consideration:



The source data for this analysis include the length of the bar, the moment of inertia of its cross-section in the plane where the buckling is expected, the elasticity modulus (this one can be specified by selecting a material from the database or by entering an explicit value if the OTHER MATERIAL option has been selected in the material list). Also, you may be required to specify data about the stiffness of the supports depending on a model selected.

If the cross-section is a rolled profile, the moment of inertia can be retrieved from the profile database

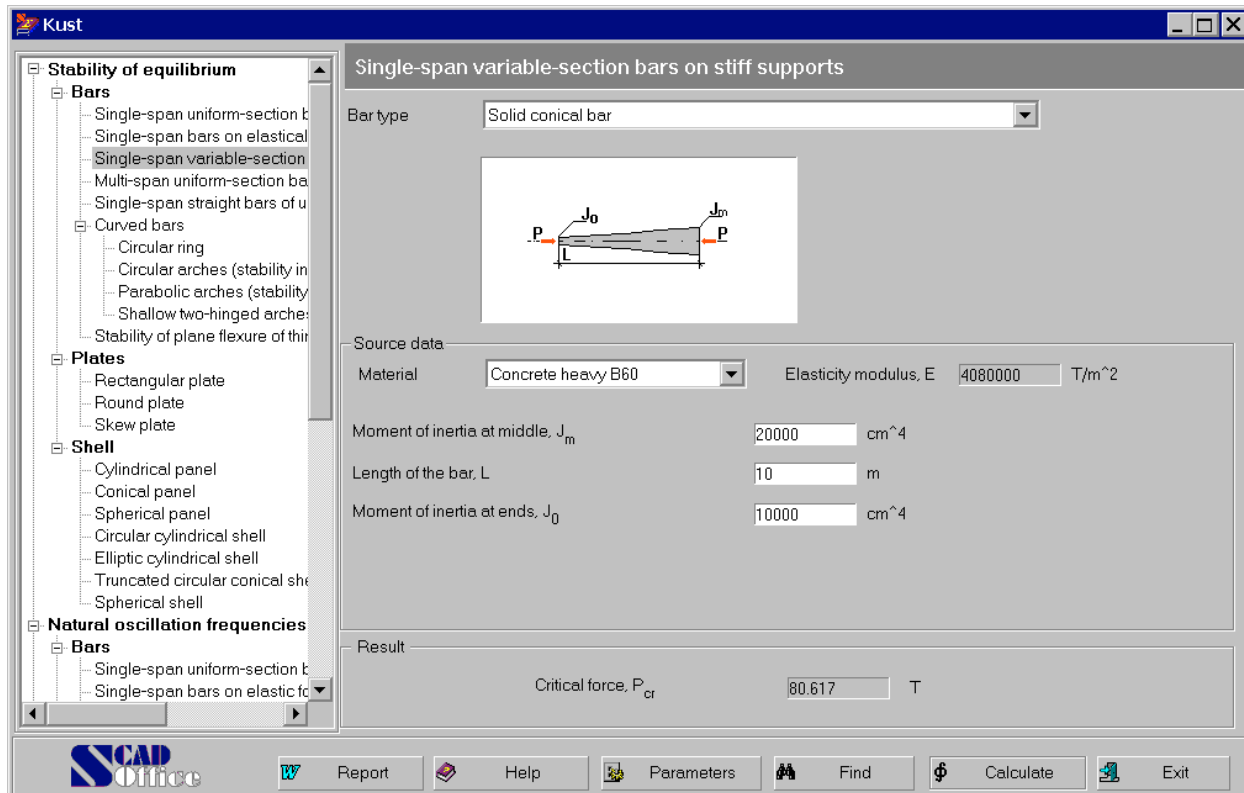
using the button  described earlier in the “Moments of inertia” section.

The result of the analysis will be the coefficient of effective length (the effective length to the actual bar's length ratio) and the critical force value.

References

[1] I.I. Goldenblatt, A.M. Sizov, *Reference manual on stability/vibration structural analysis*, State Publishing House of Civil Engineering and Architecture Books, Moscow-Leningrad, 1952, 251 pp. In Russian. (See Chapter 2.)

3. Single-span variable-section bars on stiff supports

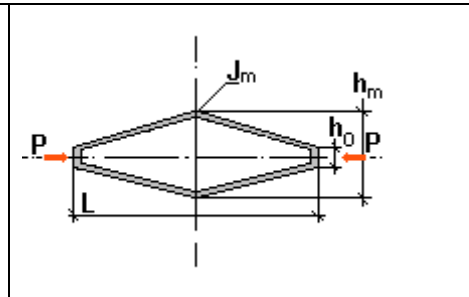


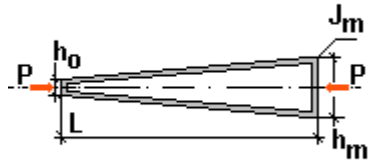
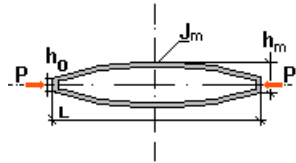

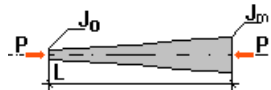
The screenshot shows the Kust software window with the title 'Single-span variable-section bars on stiff supports'. The left sidebar contains a tree view with categories: 'Stability of equilibrium' (Bars, Plates, Shell), and 'Natural oscillation frequencies' (Bars). The main area has a 'Bar type' dropdown set to 'Solid conical bar'. Below it is a diagram of a conical bar of length L with moments of inertia J_0 at the left end and J_m at the right end, subjected to compressive forces P . The 'Source data' section includes: 'Material' (Concrete heavy B60), 'Elasticity modulus, E' (4080000 T/m²), 'Moment of inertia at middle, J_m ' (20000 cm⁴), 'Length of the bar, L' (10 m), and 'Moment of inertia at ends, J_0 ' (10000 cm⁴). The 'Result' section shows 'Critical force, P_{cr} ' (80.617 T). The bottom toolbar includes buttons for Report, Help, Parameters, Find, Calculate, and Exit.

The object of consideration is the stability of equilibrium of a single-span variable-section bar placed on stiff supports and loaded by a longitudinal compressive force P .

The following types of structures are under consideration:

Symmetrical compressed bars with straight chords



Asymmetrical compressed bars with straight chords	
Symmetrical compressed bars with parabolic chords	
Column made of four angles	
Solid conical bar	

The source data to be specified for this analysis include the length of the bar and, depending on the structure's type, such data as the moment of inertia of the bar's cross-section, the thickness at the ends and in the middle.

The result of the analysis will be the critical force value.

References

- [1] F. Bleich, *Stability of steel structures*, Moscow, *Physmathgis*, 1959, 544 pp. *In Russian*. (See pp. 214-219.)
- [2] S.P. Timoshenko, *Stability of elastic systems*, State Publishing House of Technical Theoretical Books, Moscow, 1955, 567 pp. *In Russian*. (See pp. 148-151.)

4. Single-span straight bars of uniform section on elastic foundation

Kust

Stability of equilibrium

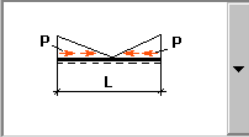
- Bars**
 - Single-span uniform-section bars
 - Single-span bars on elastic foundation
 - Single-span variable-section bars
 - Multi-span uniform-section bars
 - Single-span straight bars of uniform section
 - Curved bars
 - Circular ring
 - Circular arches (stability in the plane)
 - Parabolic arches (stability in the plane)
 - Shallow two-hinged arches
- Plates**
 - Rectangular plate
 - Round plate
 - Skew plate
- Shell**
 - Cylindrical panel
 - Conical panel
 - Spherical panel
 - Circular cylindrical shell
 - Elliptic cylindrical shell
 - Truncated circular conical shell
 - Spherical shell
- Natural oscillation frequencies**
 - Bars**
 - Single-span uniform-section bars
 - Single-span bars on elastic foundation

Single-span straight bars of uniform section on elastic foundation

Source data

Loads and fixation conditions

Free-ends bar under load distributed by triangular law



Material: Concrete heavy B50

Elasticity modulus, E : 3980000 T/m^2

Stiffness of the bar, J : 212.94 cm^4

Length of the bar, L : 6 m

Winkler's modulus of subgrade reaction, C_1 : 0.001 T/m^2

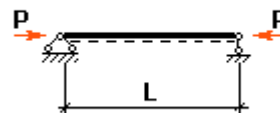
Result

Critical force, P_{cr} : 4.833 T

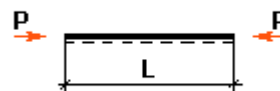
Report Help Parameters Find Calculate Exit

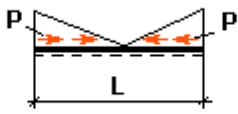

The object of consideration is the stability of a single-span bar of a uniform section placed on an elastic foundation, under the following loads and fixation conditions:

Simply supported bar on an elastic foundation




Free-end bar on an elastic foundation



Free-end bar with the load distributed according to a triangular law	
Simply supported bar with the load distributed according to a triangular law	

The source data to be specified for this analysis include the length of the bar, the moment of inertia of the bar's cross-section (which indicates the stiffness of the bar), the elasticity modulus (this one can be specified by selecting a material from the database or by entering an explicit value if the OTHER MATERIAL option has been selected in the material list), and the (Winkler's) modulus of subgrade reaction C_1 .

If the cross-section is a rolled profile, the moment of inertia can be retrieved from the profile database using the button  described earlier in the "Moments of inertia" section.

The result of the analysis will be the critical force value.

References

- [1] I.I. Goldenblatt, A.M. Sizov, *Reference manual on stability/vibration structural analysis*, State Publishing House of Civil Engineering and Architecture Books, Moscow-Leningrad, 1952, 251 pp. *In Russian*. (See p. 57, Paragraph 12).
- [2] *Structural designer's reference manual. Design theory and analysis* (ed. by A.A. Umansky), State Publishing House of Civil Engineering and Architecture Books, Moscow-Leningrad, 1960, 1040 pp. *In Russian*. (See p. 779, Paragraph 16.1.3).

5. Multi-span uniform-section bars on elastic supports

Kust

Stability of equilibrium

- Bars**
 - Single-span uniform-section bars on elastic supports
 - Single-span bars on elastic supports
 - Single-span variable-section bars on elastic supports
 - Multi-span uniform-section bars on elastic supports**
 - Single-span straight bars of uniform section
- Curved bars**
 - Circular ring
 - Circular arches (stability in the plane)
 - Parabolic arches (stability in the plane)
 - Shallow two-hinged arches
- Plates**
 - Rectangular plate
 - Round plate
 - Skew plate
- Shell**
 - Cylindrical panel
 - Conical panel
 - Spherical panel
 - Circular cylindrical shell
 - Elliptic cylindrical shell
 - Truncated circular conical shell
 - Spherical shell
- Natural oscillation frequencies**
 - Bars**
 - Single-span uniform-section bars on elastic supports
 - Single-span bars on elastic supports

Multi-span uniform-section bars on elastic supports

Source data

Material: Concrete heavy B40

Elasticity modulus, E: 3670000 T/m²

Moment of inertia, J: 55961.998 cm⁴

Length, L: 6 m

Spacing between the supports, a: 3 m

Coefficient of elasticity of particular supports, α : 1 T/m

Result

Critical force, P_{cr} : 564.278 T

Report Help Parameters Find Calculate Exit

The object of consideration is the stability of equilibrium of a multi-span uniform-section bar placed on elastic supports.

The source data for this analysis include the length of the bar, the moment of inertia of its cross-section (the stiffness), the modulus of elasticity (this one can be specified by selecting a material from the database or by entering an explicit value if the OTHER MATERIAL option has been selected in the material list), the spacing between the supports, and the coefficient of elasticity of particular supports.

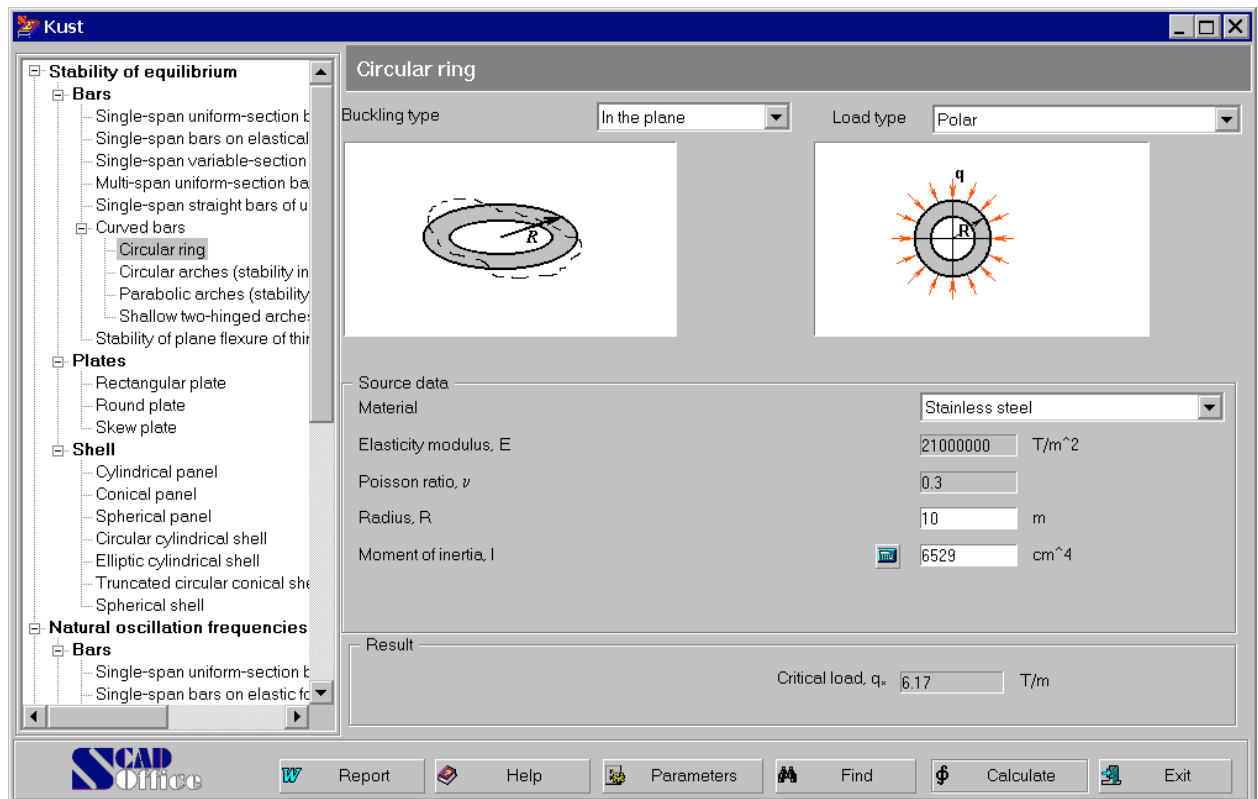
If the cross-section is a rolled profile, the moment of inertia can be retrieved from the profile database using the button described earlier in the “Moments of inertia” section.

The result of the analysis will be the critical force value.

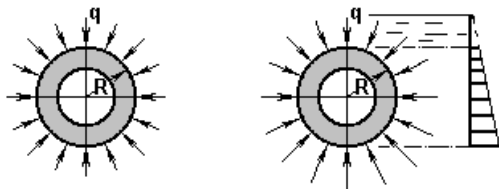
References

[1] S.P. Timoshenko, *Stability of elastic systems*, State Publishing House of Technical Theoretical Books, Moscow, 1955, 567 pp. *In Russian*. (See page 113.)

6. Circular ring

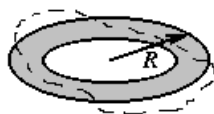


The object of consideration is a circular ring under a uniform external (polar) pressure or a hydrostatic load.



Of interest is a critical load under which the ring experiences buckling in its plane or out of its plane.

The buckling in the plane of the ring is defined by flexural displacements in this plane.




The buckling out of the plane of the ring consists of flexural displacements perpendicular to the plane.



The source data for this analysis include the buckling type (in/out the plane), the load type

(polar/hydrostatic), the radius of the ring, the moment of inertia of the ring's section, the elasticity modulus, and the Poisson ratio (the latter data can be specified by selecting a material from the database or by entering an explicit value if the OTHER MATERIAL option has been selected in the material list).

Depending on the selected buckling type (in the plane/out of the plane), you need to specify the moment of inertia of the ring either in its plane or in the direction orthogonal to the ring's plane.

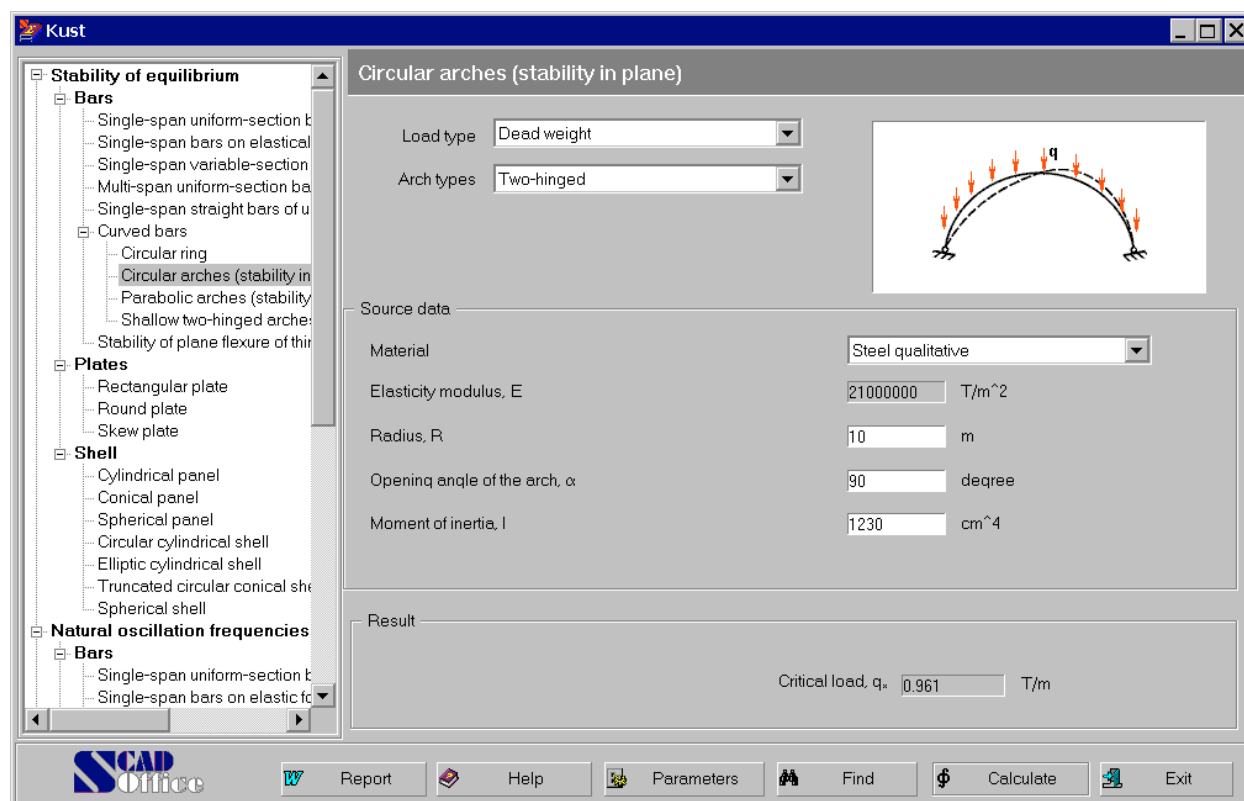
If the cross-section is a rolled profile, the moment of inertia can be retrieved from the profile database using the button  described earlier in the "Moments of inertia" section.

The result of the analysis will be the critical load value.

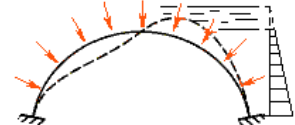
References

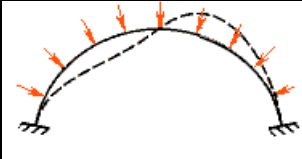
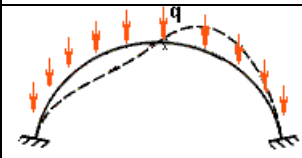
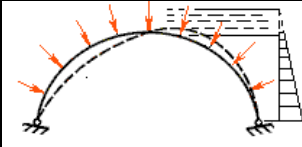
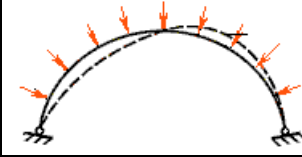
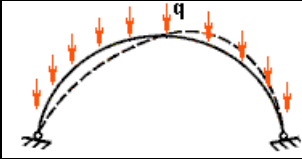
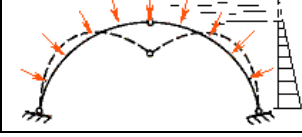
[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. In Russian. (See p. 254, Paragraph 17.12.2.)

7. Circular arches (stability in plane)



The object of consideration is the stability of a circular arch in its plane. The following combinations of loads and arch types can be analyzed.

Arch type		Load type
No-hinged		Hydrostatic

		Polar
		Dead weight
Two-hinged		Hydrostatic
		Polar
		Dead weight
Three-hinged		Hydrostatic

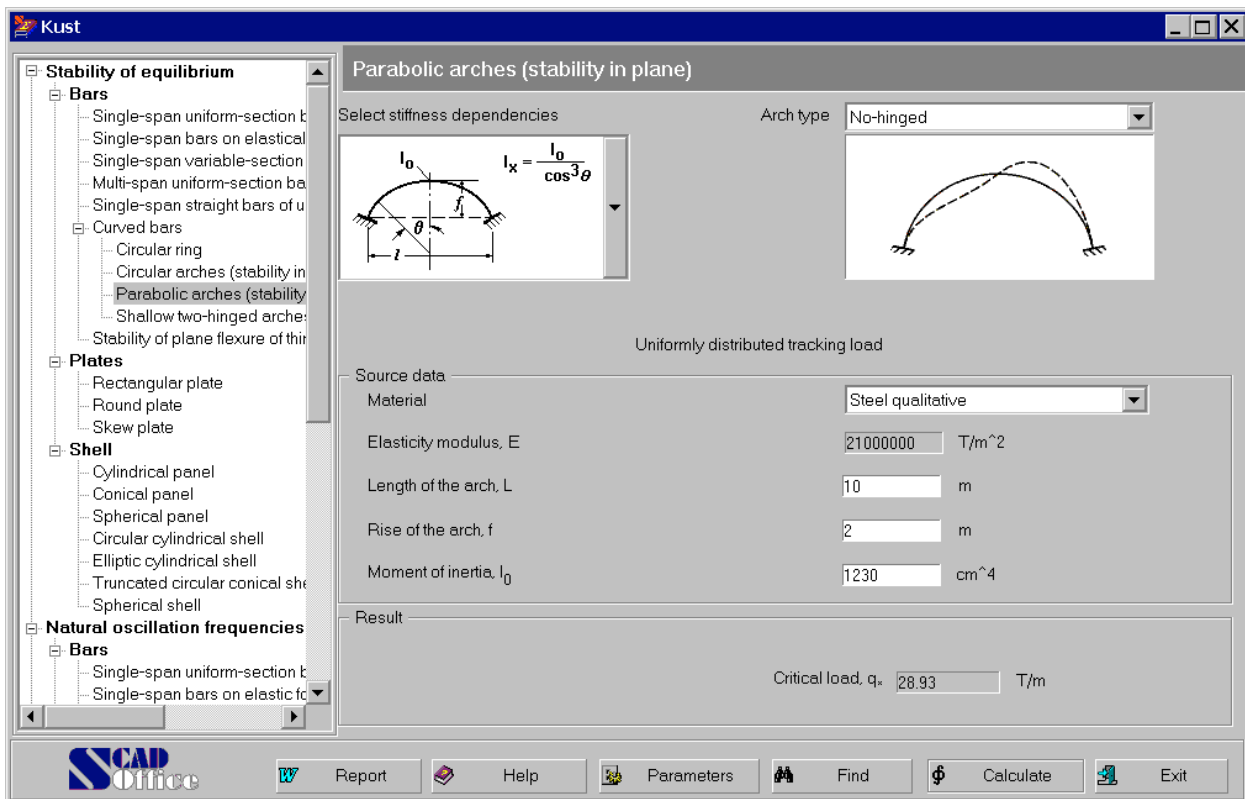
The source data for this analysis include the elasticity modulus (this can be specified by selecting a material from the database or by entering an explicit value if the OTHER MATERIAL option has been selected in the material list), the radius of the arch, the opening angle of the arch, and the moment of inertia of the arch's cross-section in its plane.

The result of the analysis will be the critical load value.

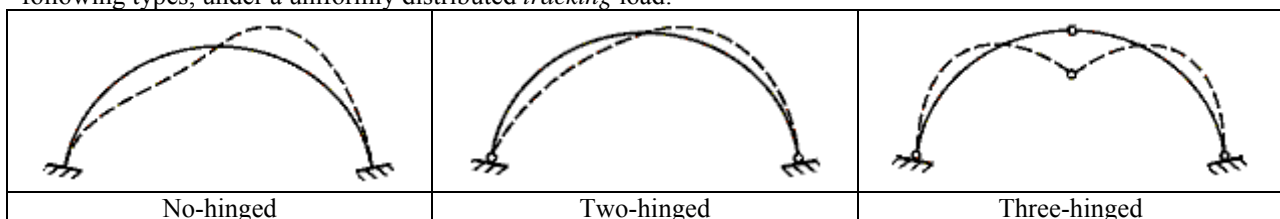
References

[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. *In Russian.* (See p. 255.)

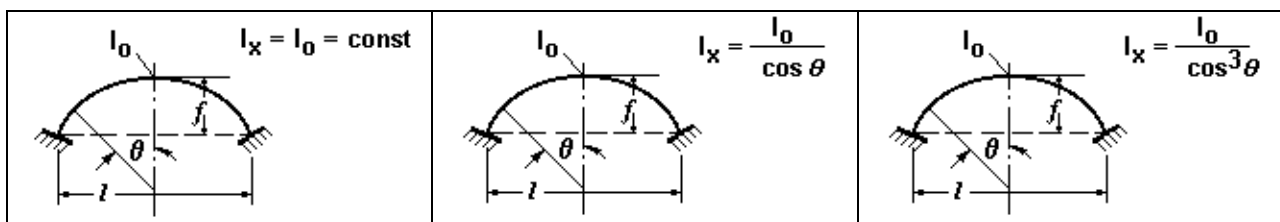
8. Parabolic arches (stability in plane)



The object of consideration is the stability of equilibrium of a parabolic arch (in its plane) of one of the following types, under a uniformly distributed *tracking* load:



The following stiffness dependencies are implemented:



The source data for this analysis include the elasticity modulus (this can be specified by selecting a material from the database or by entering an explicit value if the OTHER MATERIAL option has been selected in the material list), the length and the rise of the arch, the moment of inertia of the arch's cross-section in the middle of the arch (*in its plane*).

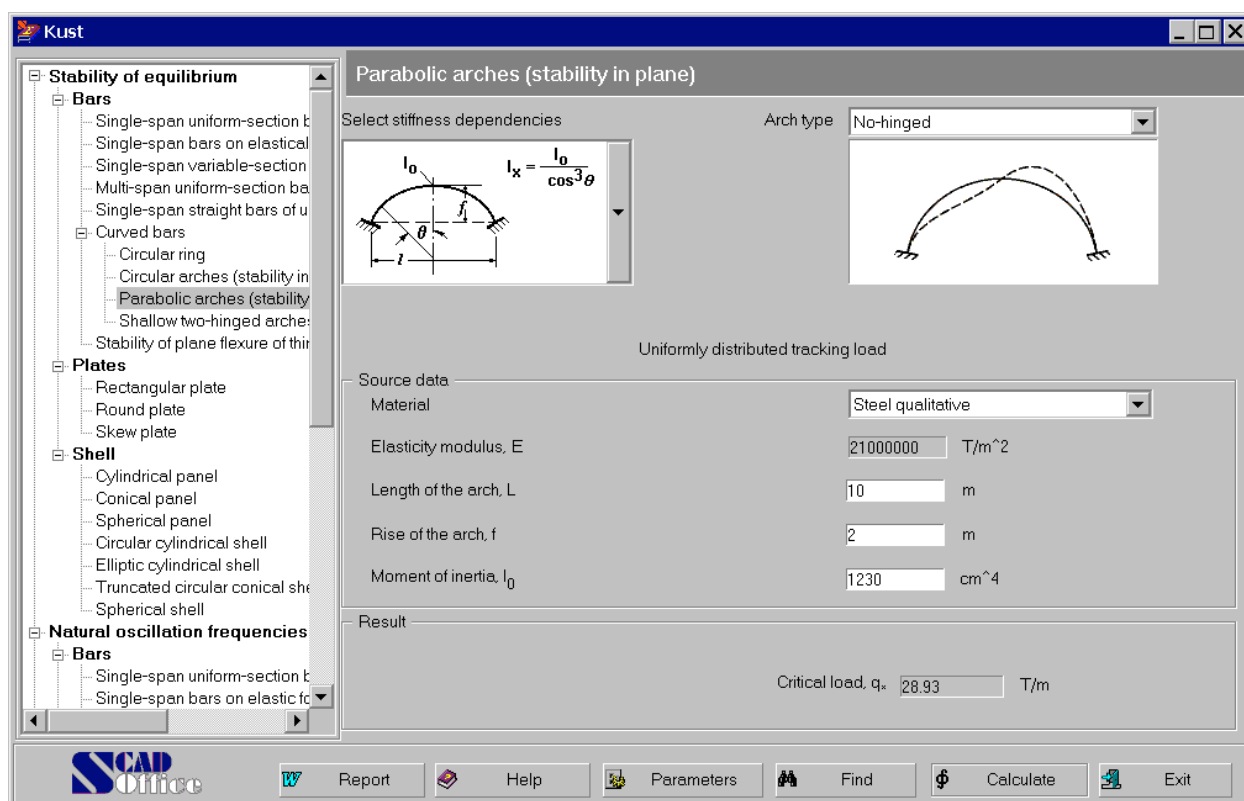
If a three-hinged arch is under consideration, where either a symmetric or antisymmetric buckling mode is possible, the program will analyze both cases and calculate the minimum value of the critical load.

The result of the analysis will be the critical load value.

References

[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. (See p. 256.)

9. Shallow two-hinged arches (stability in plane)



The object of consideration is the stability of equilibrium of a shallow two-hinged arch under a distributed load q or a concentrated force P applied to the key-stone.



The source data for this analysis include the elasticity modulus (this can be specified by selecting a material from the database or by entering an explicit value if the OTHER MATERIAL option has been selected in the material list), the length and the rise of the arch, the area of the arch's cross-section and its moment of inertia with respect to the axis perpendicular to the arch's plane.

The result of the analysis will be the critical load value.

References

[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. (See p. 256.)

10. Stability of plane flexure of thin-walled beams

The object of consideration is the stability of plane flexure experienced by a thin-walled I- or H-beam (either symmetric or asymmetric) under a uniformly distributed load or under a concentrated force.

The source data for this analysis include the type of the beam (symmetric or asymmetric), the type of the load (distributed or concentrated), the elasticity modulus, the Poisson ratio (the two latter pieces of data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list), the length of the span, and the dimensions of the section (thickness/width of the webs and legs). Also, you should specify the location of the load from a drop-down list (the options include the bottom chord, the top chord, and the section's mass center).

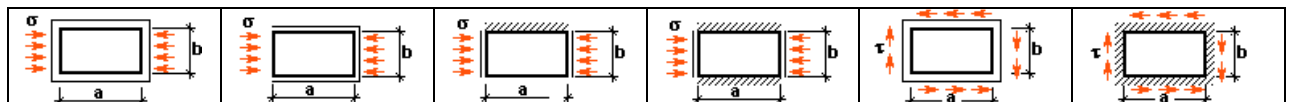
The result of the analysis will be the critical load value.

References

[1] F. Bleich, *Stability of steel structures*, Moscow, Physmathgis Publishing House, 1959, 544 pp. In Russian. (See p. 186.)

11. Rectangular plate

The object of consideration is a stability of a rectangular plate fixed/supported in a variety of ways and subjected to various loads (see the table below).



This table uses the following legend for fixation types:

Free edge	
Clamped edge	
Simple support	

The source data for this analysis include the dimensions of the plate (length, width, thickness); the elasticity modulus and the Poisson ratio of the material the plate is made of (the latter data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list).

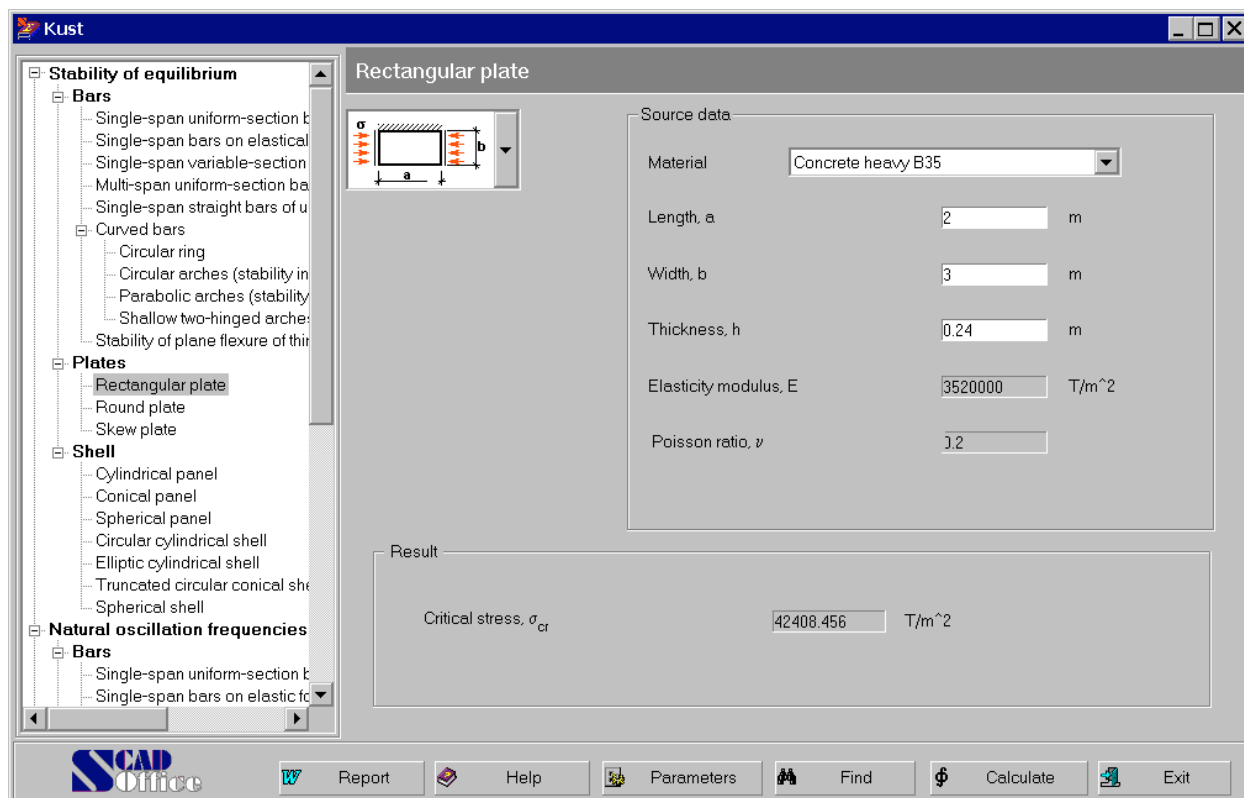
The result of the analysis will be the *critical stress* value (either the normal one σ or the tangential one τ ,

depending on the load pattern).

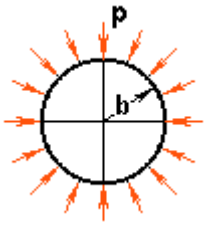
References


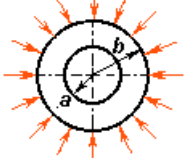
[1] *Reference manual on elasticity* (ed. by P.M. Varvak), Kiev, Budivelnyk Publishers, 1971, 416 pp. (See p. 411.)

12.Round plate



The object of consideration is the stability of equilibrium of round and annular plates under radial compressive loads. For annular plates, cases of loads along the exterior edge or both the exterior and interior edge are included. The table below lists all combinations of loads and boundary conditions available for the analysis.

Shape and load	Boundary conditions
 <p>Round plate under radial compression</p>	<ul style="list-style-type: none"> ♦ Simply supported edge ♦ Clamped edge

 <p>Annular plate under uniform radial compression on the exterior and interior contours</p>	<ul style="list-style-type: none"> ◆ Both edges clamped ◆ Both edges simply supported ◆ Exterior edge clamped, internal edge free but no slope ◆ Exterior edge simply supported, internal edge freely moving but no slope
 <p>Annular plate under radial compression uniformly distributed along the exterior edge</p>	<ul style="list-style-type: none"> ◆ Simply supported edges ◆ Clamped edges

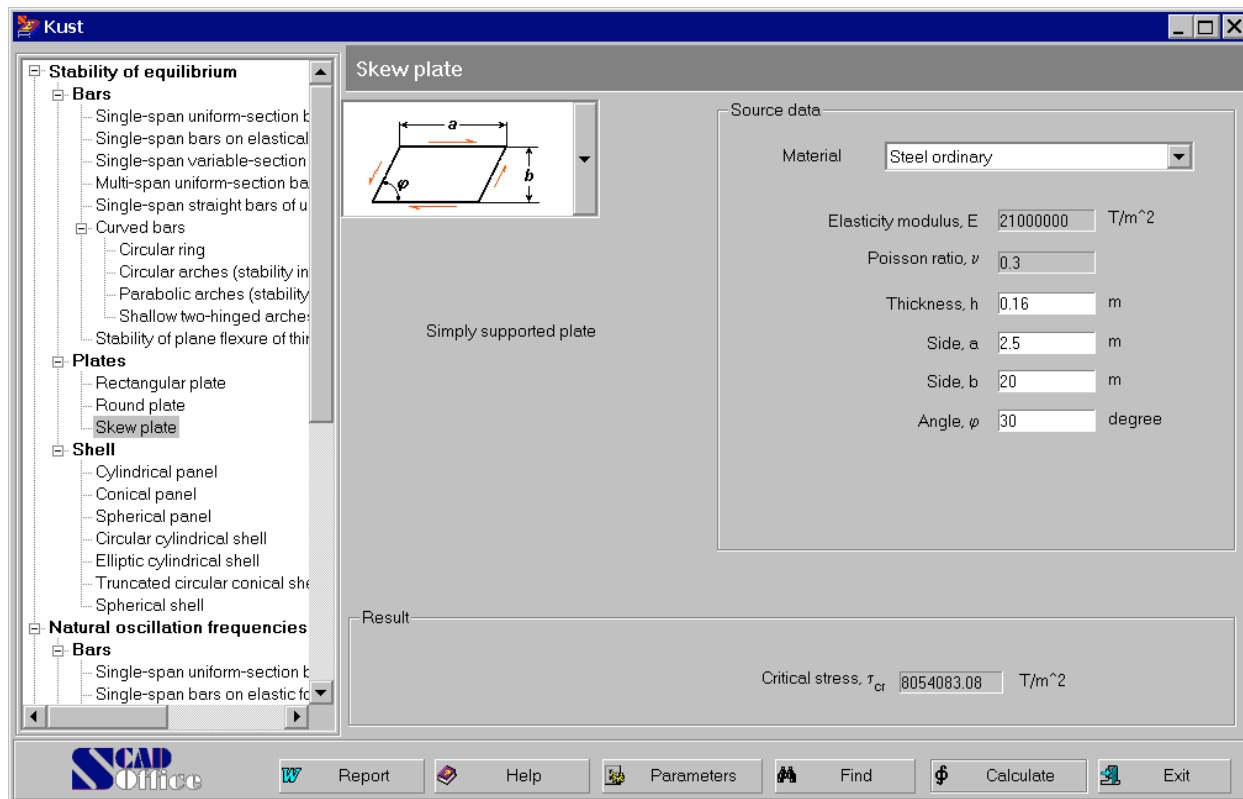
The source data for this analysis include the type of the plate (round or annular), load type, boundary conditions, sizes of the plate (external and internal radii, thickness), elasticity modulus and Poisson ratio of the material the plate is made of (the latter data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list).

The result of this analysis will be the *critical stress value*.

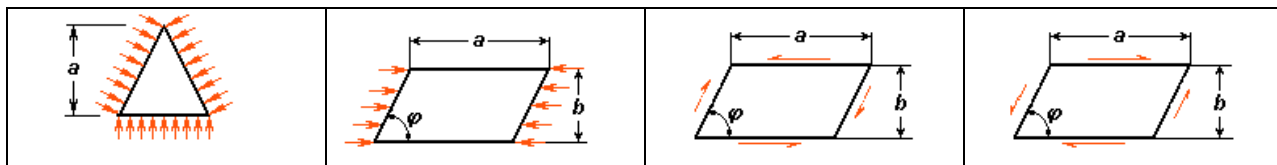
References

- [1] *Strength. Stability. Oscillations. Vol. 3* (eds. I.A. Birger, Y.G. Panovko), Moscow, Mashinostroyeniye Publishing House, 1968, 567 pp. (See p. 110.)
- [2] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. (See p. 278.)

13. Skew plate



The object of consideration is the stability of equilibrium of a simply supported plate shaped as an equilateral triangle or a parallelogram and subjected to various loads (see the table below).



The source data for this analysis include the sizes of the plate, the elasticity modulus and Poisson ratio of the material the plate is made of (the latter data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list).

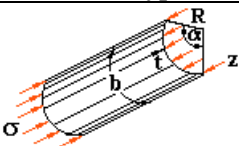
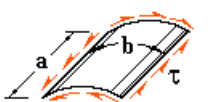
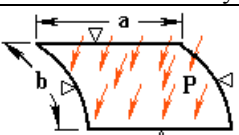
The result of the analysis will be the *critical stress* value (either normal one σ or tangential one τ depending on the load pattern).

References

[1] *Strength. Stability. Oscillations. Vol. 3* (eds I.A. Birger, Y.G. Panovko), Moscow, *Mashinostroyeniye* Publishing House, 1968, 567 pp. (See pp. 112.)

14. Cylindrical panel

The object of consideration is the stability of equilibrium of a cylindrical panel. The following cases of boundary conditions and loads are available for the analysis.

Load type	Boundary conditions
 <p>Compressive forces distributed uniformly along the edges</p>	<ul style="list-style-type: none"> ◆ All edges of the panel simply supported ◆ All edges of the panel clamped
 <p>Tangential loads distributed uniformly along the edges</p>	<ul style="list-style-type: none"> ◆ All edges of the panel simply supported ◆ All edges of the panel clamped
 <p>Uniform external pressure</p>	<ul style="list-style-type: none"> ◆ All edges of the panel simply supported

The source data for this analysis include the sizes of the panel (its radius, thickness, length, and arc length),

the elasticity modulus and Poisson ratio of the material the panel is made of (the latter data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list).

The result of the analysis will be the *critical load* value.

References

[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. (See p. 279.)

15. Conical panel

The object of consideration is the stability of equilibrium of a conical panel under a uniform external pressure (the edges of the panel are constrained in their normal directions).

The source data for this analysis include the geometrical sizes of the panel (its radius, wall thickness, cone angle, arc length, and the panel's length itself). Also, you need to provide the elasticity modulus and Poisson ratio of the material the panel is made of (the latter data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list).

The result of the analysis will be the *top critical pressure* value.

References

[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. (See p. 281.)

16. Spherical panel

Kust

Spherical panel

Spherical panel subjected to a uniform external pressure

The contour is clamped and cannot move in any way

Source data

Material: Steel qualitative

Elasticity modulus, E : 210000000 T/m²

Poisson ratio, ν : 0.3

Height H : 6 m

Wall thickness, t : 0.12 m

Radius, a : 12 m

Result

Upper critical pressure, p_{cr} : 28536.273 T/m²

SCAD Office

Report Help Parameters Find Calculate Exit

The object of consideration is the stability of equilibrium of a spherical panel subjected to a uniform external pressure and fixed in one of the following ways:

- ◆ simply supported along its contour that can move in its plane (no thrust);
- ◆ simply supported along its contour that cannot move in its plane;
- ◆ the contour is clamped, but there is no thrust;
- ◆ the contour is clamped and cannot move in any way.

The source data for this analysis include the rise of the panel, its radius, and the thickness of its wall. Also, you need to specify the elasticity modulus and Poisson ratio of the material the panel is made of (the latter data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list).

The result of the analysis will be the *critical pressure* value.

References

[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. (See p. 281.)

17. Circular cylindrical shell

Kust

Stability of equilibrium

- Bars**
 - Single-span uniform-section bars
 - Single-span bars on elastic supports
 - Single-span variable-section bars
 - Multi-span uniform-section bars
 - Single-span straight bars of uniform section
 - Curved bars**
 - Circular ring
 - Circular arches (stability in the plane)
 - Parabolic arches (stability in the plane)
 - Shallow two-hinged arches
 - Stability of plane flexure of thin-walled bars
- Plates**
 - Rectangular plate
 - Round plate
 - Skew plate
- Shell**
 - Cylindrical panel
 - Conical panel
 - Spherical panel
 - Circular cylindrical shell**
 - Elliptic cylindrical shell
 - Truncated circular conical shell
 - Spherical shell
- Natural oscillation frequencies**
 - Bars**
 - Single-span uniform-section bars
 - Single-span bars on elastic supports

Circular cylindrical shell

Action of bending force couples lying in the diametral plane (simply supported ends)

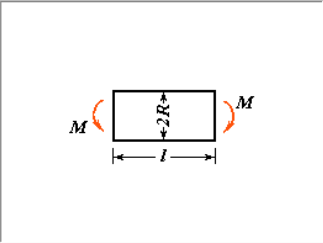
Source data

Material: Concrete heavy B50 Elasticity modulus, E: 39800000 T/m²

Poisson ratio, ν : 0.2

Radius, R: 4 m

Wall thickness, t: 0.1 m

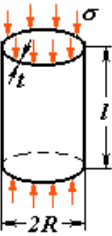
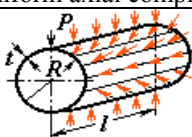


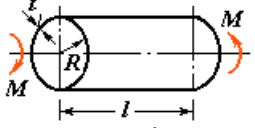
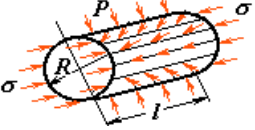
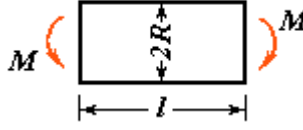

Result

Upper critical stress $\sigma_{cr,u}$: 58630.937 T/m²

SCAD Office Report Help Parameters Find Calculate Exit

The object of consideration is the stability of equilibrium of a circular cylindrical shell under the following combinations of loads and boundary conditions.

Load type	Boundary conditions
 <p>Uniform axial compression</p>	Both edges simply supported
 <p>Uniformly distributed external pressure</p>	Both edges simply supported

 <p>Torques at ends</p>	<ul style="list-style-type: none"> ◆ Edges clamped ◆ Edges simply supported
 <p>Combined action of uniform axial compression and external uniform lateral load</p>	<p>Simply supported ends</p>
 <p>Action of bending force couples lying in the diametral plane</p>	<p>Simply supported ends</p>
 <p>Flexure under lateral force</p>	<p>One end clamped, the other free</p>

The source data for this analysis include the sizes of the shell (radius, thickness, length). Also, you need to specify the elasticity modulus and Poisson ratio of the material the shell is made of (the latter data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list).

The result of the analysis will be the *critical load* value.

References

[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Sroizdat Publishing House, 1973, 415 pp. (See p. 281.)

18. Elliptic cylindrical shell

The object of consideration is the stability of equilibrium of an elliptic cylindrical shell having a small eccentricity, under a uniform axial compression; the edges of the shell are simply supported.

The source data for this analysis include the greater and smaller semi-axes and the thickness of the shell; the elasticity modulus and Poisson ratio of the material the shell is made of (the latter data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list).

The result of the analysis will be the *top critical stress value* $\sigma_{cr,t}$ and the *top critical pressure* $P_{cr,t}$ (which is the product of $\sigma_{cr,t}$ and the area of the shell's cross-section).

References

[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. (See p. 285.)

19. Truncated circular conical shell

Stability of equilibrium

- Bars
 - Single-span uniform-section bars
 - Single-span bars on elastic supports
 - Single-span variable-section bars
 - Multi-span uniform-section bars
 - Single-span straight bars of uniform section
- Curved bars
 - Circular ring
 - Circular arches (stability in the plane)
 - Parabolic arches (stability in the plane)
 - Shallow two-hinged arches
 - Stability of plane flexure of thin-walled arches
- Plates
 - Rectangular plate
 - Round plate
 - Skew plate
- Shell
 - Cylindrical panel
 - Conical panel
 - Spherical panel
 - Circular cylindrical shell
 - Elliptic cylindrical shell
 - Truncated circular conical shell
 - Spherical shell

Natural oscillation frequencies

- Bars
 - Single-span uniform-section bars
 - Single-span bars on elastic supports

Truncated circular conical shell

Uniform external pressure

The smaller base clamped, the bigger one simply supported

Source data

Material: Concrete heavy B55 Elasticity modulus, E: 4030000 T/m²

Poisson ratio, ν : 0.2

Radius bigger bases, r_1 : 12 m

Radius smaller bases, r_0 : 6 m

Height H: 7 m

Shell thickness, t: 0.1 m

Result

Upper critical pressure, $p_{cr,u}$: 28.184 T/m²

Diagram: A truncated circular conical shell with radius r_0 at the top, radius r_1 at the bottom, height H , and thickness t . Red arrows indicate uniform external pressure.

The object of consideration is the stability of equilibrium of a shell having the shape of a truncated circular cone. The following two cases are under consideration.

	<p>Uniform longitudinal compression. Exterior edges simply supported.</p>
	<p>Uniform external pressure. The smaller base clamped, the bigger one simply supported.</p>

The source data for this analysis include the radii of the smaller and bigger bases; the thickness and the height of the shell. Also, you need to specify the elasticity modulus and Poisson ratio of the material the shell is made of (the latter data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list).

The result of the analysis will be the *top critical pressure* value.

References

[1] *Strength. Stability. Oscillations. Vol. 3* (eds. I.A. Birger, Y.G. Panovko), Moscow, Mashinostroyeniye Publishing House, 1968, 567 pp. (See pp. 146, 168-173.)

20. Spherical shell

The screenshot shows the 'Kust' software window with the 'Spherical shell' analysis module selected. The left sidebar lists various structural analysis options under 'Stability of equilibrium', 'Plates', 'Shell', and 'Natural oscillation frequencies'. The 'Spherical shell' option is highlighted. The main window displays the 'Uniform external pressure' analysis setup. The 'Source data' section includes a material selection dropdown set to 'Steel ordinary', and input fields for Elasticity modulus, E (210000000 T/m²), Poisson ratio, ν (0.3), Radius, R (6 m), and Wall thickness, t (0.3 m). A diagram of a spherical shell under uniform external pressure is shown. The 'Result расчёта' section displays the 'Critical pressure, p_{cr} ' as 63548.891 T/m². The bottom toolbar contains icons for Report, Help, Parameters, Find, Calculate, and Exit.

The object of consideration is the stability of equilibrium of a spherical shell under a uniform external pressure.

The source data for this analysis include the radius and the thickness of the shell. Also, you need to specify the elasticity modulus and Poisson ratio of the material the shell is made of (the latter data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list).

The result of the analysis will be the *critical pressure* value.

References

[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. (See p. 287.)

Natural oscillation frequencies

21. Single-span uniform-section bars on stiff supports

The screenshot shows the Kust software window with the title "Single-span uniform-section bars on stiff supports". The left sidebar contains a tree view with categories: "Stability of equilibrium" (Bars, Plates, Shell), "Natural oscillation frequencies" (Bars), and "Other". The main area is divided into "Source data" and "Result".

Source data:

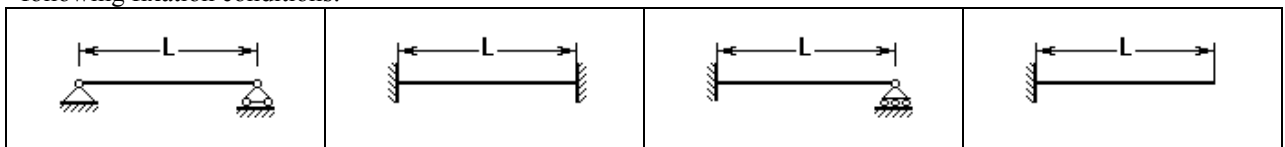
- Material: Steel ordinary
- Number of frequencies: 14
- Length, L: 20 m
- Weight of its running meter, m: 0.079 T/m
- Elasticity modulus, E: 21000000 T/m²
- Moment of inertia, J: 39726.999 cm⁴

Result:

#	Number of oscillations per second	Circular frequency
1	8.994	56.51
2	24.983	156.973
3	48.967	307.667
4	80.945	508.593
5	120.918	759.75
6	168.885	1061.138
7	224.847	1412.758

The bottom of the window has a toolbar with buttons: Report, Help, Parameters, Find, Calculate, and Exit.

The object of consideration is an oscillating bar of a uniform section placed on stiff supports under the following fixation conditions:



The source data for this analysis include the length of the bar, the weight of its running meter, the moment of inertia of the bar's cross-section, and the elasticity modulus of the material the bar is made of (this datum can be specified by selecting a material from the database or by entering an explicit value if the OTHER MATERIAL option has been selected in the material list). Also, you need to specify the desired number of natural frequencies the program is to calculate.

If the cross-section is a rolled profile, the moment of inertia can be retrieved from the profile database using the button described earlier in the "Moments of inertia" section.

The result of the analysis will be values of the *frequency of oscillations in Hz* (measured as the number of oscillations per second) and the *circular frequency in rad/s* corresponding to the specified number of natural oscillation modes.

References

- [1] *Reference manual on stability/vibration structural analysis* (ed. by I.I. Goldenblat), State Publishing House of Civil Engineering and Architecture Books, Moscow, 1952, 251 pp. (See p. 104.)
- [2] R.D. Blevins, *Formulas for natural frequency and mode shape*, Malabar Florida, Krieger Publishing Company, 2001. — 492 c. (See p. 106.)

22. Single-span bars on elastic foundation

The screenshot shows the Kust software window titled 'Single-span bars on elastic foundation'. On the left is a tree view with categories: Natural oscillation frequencies, Bars, Plates, Shell, Other oscillation problems, Static analysis, and Auxiliary calculations. The 'Bars' category is expanded, showing 'Single-span bars on elastic foundation' as the selected item. The main area contains a diagram of a bar of length L fixed at the left end. To the right is a 'Source data' section with the following fields:

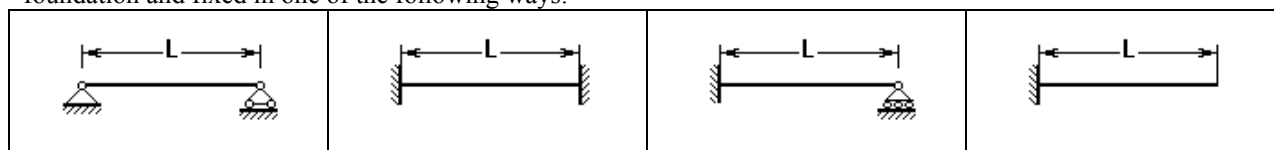
- Material: Concrete heavy B60
- Number of frequencies: 15
- Length, L: 6 m
- Weight of its running meter, m: 0.079 T/m
- Elasticity modulus, E: 4080000 T/m²
- Moment of inertia, J: 1043 cm⁴ (with a button to open a database)
- Stiffness of the foundation, E_f: 4.51 T/m²

Below the source data is a 'Result' section containing a table:

#	number of oscillations per second	Circular frequency
1	7.162	45.002
2	19.834	124.624
3	38.862	244.18
4	64.237	403.614
5	95.957	602.915

At the bottom of the window is a toolbar with icons for Report, Help, Parameters, Find, Calculate, and Exit.

The object of consideration is an oscillating single-span bar of a uniform section placed on an elastic foundation and fixed in one of the following ways:



The source data for this analysis include the length of the bar, the weight of its running meter, the moment of inertia of the bar's cross-section, the stiffness of the foundation, and the elasticity modulus of the material the bar is made of (the latter can be specified by selecting a material from the database or by entering an explicit value if the OTHER MATERIAL option has been selected in the material list). Also, you need to specify the number of natural frequencies the program is to calculate.

If the cross-section is a rolled profile, the moment of inertia can be retrieved from the profile database using the button described earlier in the "Moments of inertia" section.

The result of the analysis will be values of the *frequency of oscillations in Hz (measured as the number of oscillations per second)* and the *circular frequency in rad/s* corresponding to the specified number of lower natural

oscillation modes.

References

[1] *Reference manual on stability/vibration structural analysis* (ed. by I.I. Goldenblat), State Publishing House of Civil Engineering and Architecture Books, Moscow, 1952, 251 pp.

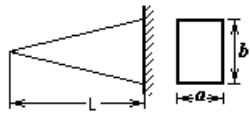
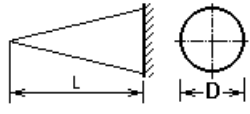
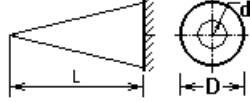
23. Bars of variable section

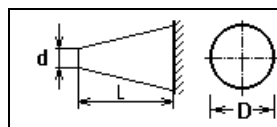
The screenshot shows the 'Kust' software window with the 'Bars of variable section' module selected. The left sidebar lists various structural analysis options, including 'Natural oscillation frequencies', 'Bars', 'Plates', 'Shell', 'Other oscillation problems', 'Static analysis', and 'Auxiliary calculations'. The main panel displays a diagram of a cantilever bar with a variable cross-section, showing length L , width a , and height b . The 'Source data' section includes a material dropdown set to 'Concrete heavy B60' and input fields for: Number of frequencies (4), Length L (3 m), Specific weight ρ (2.5 T/m³), Elasticity modulus E (4080000 T/m²), Poisson ratio ν (0.2), Width a (1 m), and Height b (3 m). The 'Result' table shows the following data:

#	number of oscillations per second	Circular frequency
1	163.633	1028.138
2	465.874	2927.17
3	920.197	5781.765
4	1530.868	9618.725

The bottom toolbar contains buttons for Report, Help, Parameters, Find, Calculate, and Exit.

The object of consideration is an oscillating cantilever bar of a variable cross-section. The oscillation frequencies can be calculated for the following situations:

	A wedge-shaped cantilever: the height of the section is proportional to the distance to the vertex, the width is uniform
	A cantilever shaped as a circular cone
	A hollow cone with its wall's thickness varying by a linear law



A cantilever shaped as a truncated circular cone

The source data for this analysis include the length of the bar, the dimensions of the cross-section at the clamped end, the specific weight, the elasticity modulus and Poisson ratio of the material the bar is made of (the latter two pieces of data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list). In the case of a truncated cone, you should specify the diameter of the cone at the free end. Also, you need to specify the number of natural frequencies the program is to calculate.

The result of the analysis will be values of the *frequency of oscillations in Hz* (measured as the number of oscillations per second) and the *circular frequency in rad/s* corresponding to the specified number of lower natural oscillation modes.

References


[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. (See p. 366.)

24. Round rings

#	number of oscillations per second	Circular frequency
1	0	0
2	0.279	1.756
3	0.79	4.965
4	1.515	9.521
5	2.45	15.397
6	3.595	22.587

The object of consideration is an oscillating round ring of a uniform cross-section. One of the principal axes of inertia of the ring must lie in its axis' plane. Two cases are available for the analysis: a circular ring and an incomplete one where a part of it measured by the angle α is clamped at both ends. Flexural oscillations in the plane of the ring are under consideration.

The source data for this analysis include the radius of the ring's centerline, the weight of its running meter, the moment of inertia of the ring's cross-section with respect to the principal axis of the ring's orthogonal projection, the opening angle (in the case of an incomplete ring), and the elasticity modulus of the material the ring is made of (the latter can be specified by selecting a material from the database or by entering an explicit value if the OTHER MATERIAL option has been selected in the material list). Also, you need to specify the desired number of natural frequencies (only the first frequency is calculated for an incomplete ring).

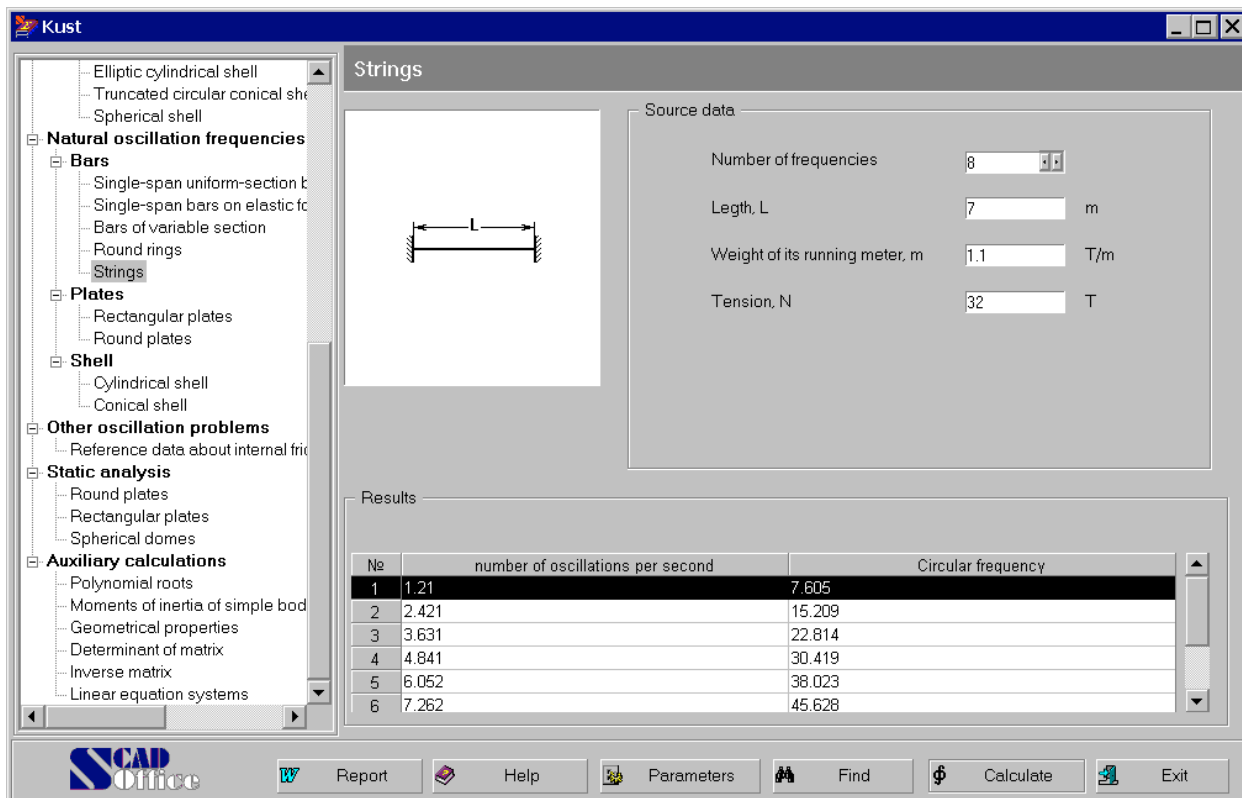
If the cross-section is a rolled profile, the moment of inertia can be retrieved from the profile database using the button  described earlier in the "Moments of inertia" section.

The result of the analysis will be values of the *frequency of oscillations in Hz* (measured as the number of oscillations per second) and the *circular frequency in rad/s* corresponding to the specified number of lower natural oscillation modes.

References

[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. (See p. 362)

25. Strings



No	number of oscillations per second	Circular frequency
1	1.21	7.605
2	2.421	15.209
3	3.631	22.814
4	4.841	30.419
5	6.052	38.023
6	7.262	45.628

The object of consideration is a string with fixed ends that experiences lateral oscillations.

The source data for this analysis include the length of the string, the weight of its running meter, its tension, and the desired number of natural frequencies.

The result of the analysis will be values of the *frequency of oscillations in Hz* (measured as the number of oscillations per second) and the *circular frequency in rad/s* corresponding to the specified number of lower natural oscillation modes.

References

[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. (See p. 369.)

26. Rectangular plates

Kust

Rectangular plates

Source data

Material: Concrete heavy B60

Number of frequencies: 10

☐ Include zero frequencies

Length, a: 4 m

Width, b: 5 m

Thickness, h: 0.3 m

Elasticity modulus, E: 4080000 T/m²

Poisson ratio, ν : 0.2

Specific weight, ρ : 2.5 T/m³

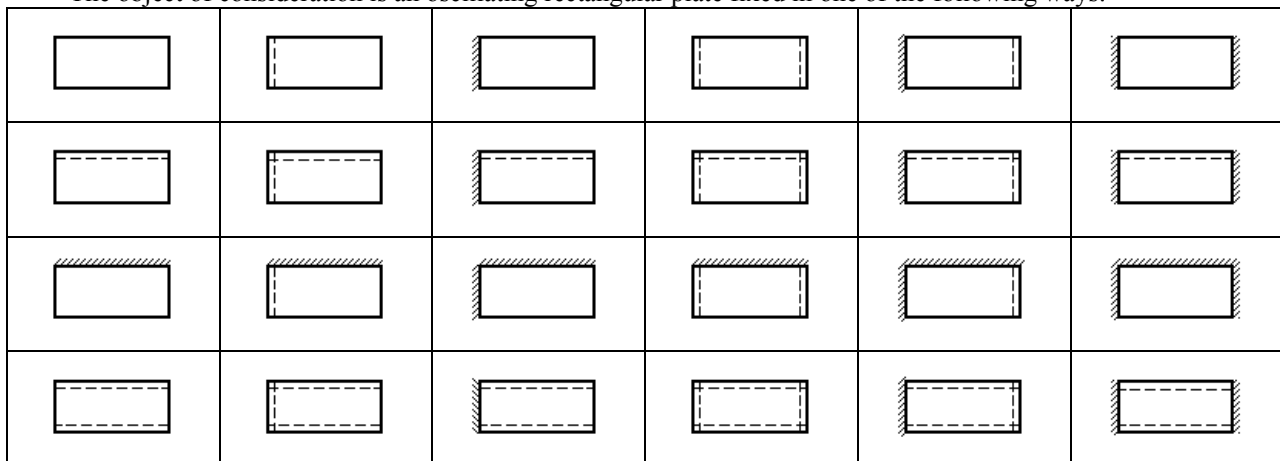
Result

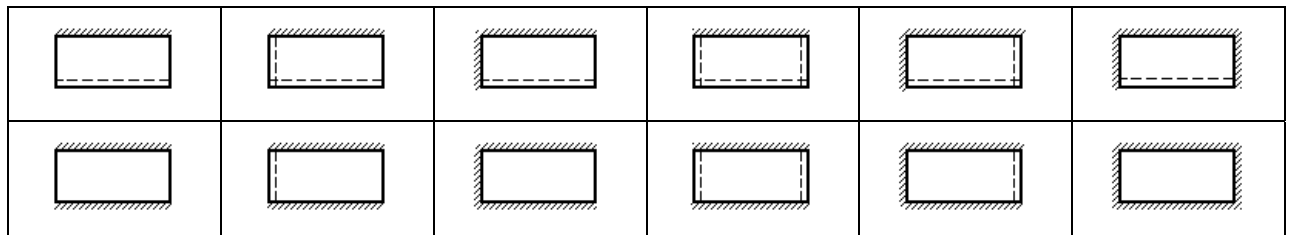
#	number of oscillations per second	Circular frequency
1	454.522	2855.848
2	843.463	5299.637
3	1226.298	7705.059
4	1526.975	9594.265

SCAD Office

Report Help Parameters Find Calculate Exit

The object of consideration is an oscillating rectangular plate fixed in one of the following ways:





The following legend is used to designate methods of fixation:

Free edge	
Clamped edge	
Simple support	

The source data for this analysis include the sizes of the plate (length, width, thickness); the elasticity modulus, Poisson ratio, and specific weight of the material the plate is made of (the latter data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list). Also, you need to specify the desired number of natural frequencies. Some boundary conditions cause zero frequencies to appear, therefore you need to use the **Include zero frequencies** checkbox to define whether you want to obtain such or not.

The result of the analysis will be values of the *frequency of oscillations in Hz* (measured as the number of oscillations per second) and the *circular frequency in rad/s* corresponding to the specified number of lower natural oscillation modes.

References

[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. (See p. 363.)

27. Round plates

Source data

Material: Concrete heavy B55

Elasticity modulus, E : 4030000 T/m²

Poisson ratio, ν : 0.2

Radius, r : 1 m




Thickness, h : 0.2 m

Specific weight, ρ : 2.5 T/m³

Result

n	number of oscillations per second	Circular frequency
1	373.777	2348.509
2	776.835	4880.998
3	1275.46	8013.954
4	1456.273	9150.032
5	2232.705	14028.501
6	3734.178	23370.678

The object of consideration is an oscillating round plate fixed in one of the following ways:

	Stiffly clamped edge
	Simple support with restrained horizontal displacements
	Stiffly clamped center of the plate

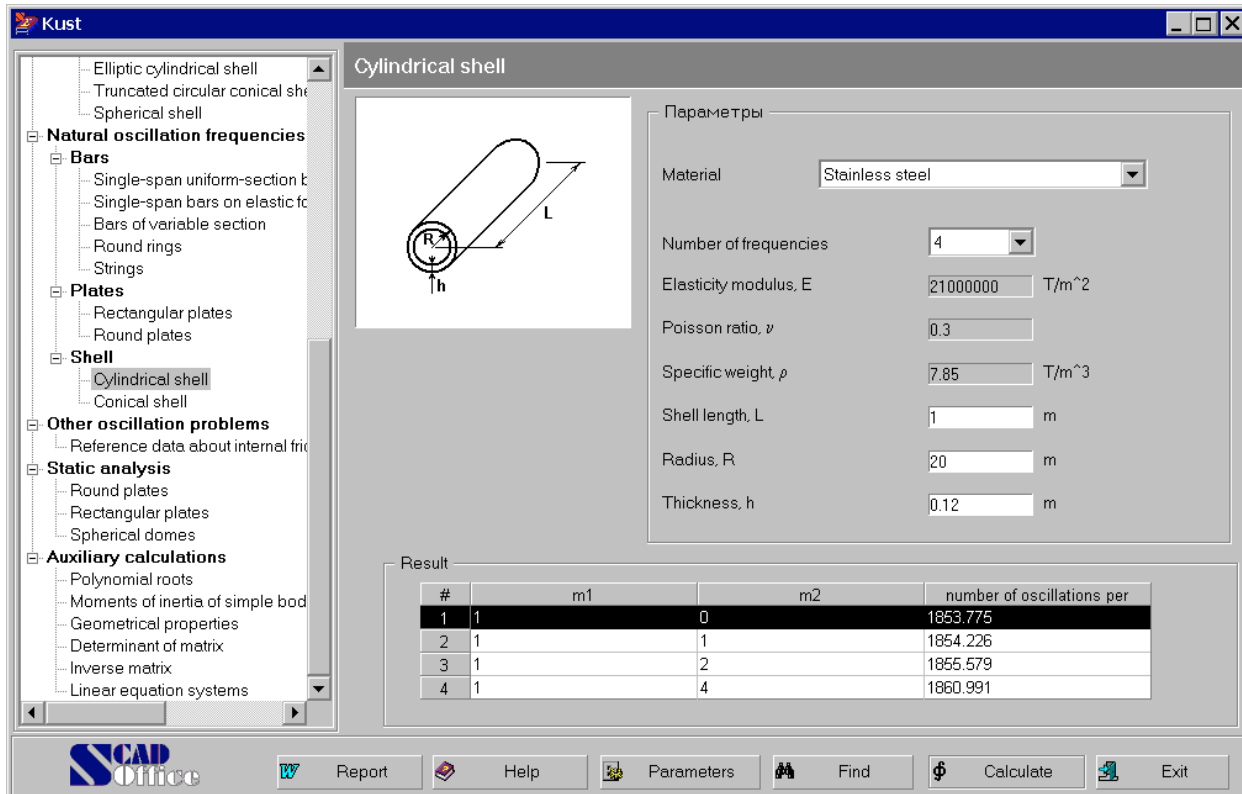
The source data for this analysis include the radius and the thickness of the plate, its specific weight, the elasticity modulus and Poisson ratio of the material the plate is made of (the latter two values can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list).

The result of the analysis will be values of the *frequency of oscillations in Hz (measured as the number of oscillations per second)* and the *circular frequency in rad/s* for a few lower natural oscillation modes.

References

[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. (See p. 365.)

28. Cylindrical shell



Куст

Cylindrical shell

Elliptic cylindrical shell
Truncated circular conical shell
Spherical shell

Natural oscillation frequencies

Bars

- Single-span uniform-section bars
- Single-span bars on elastic supports
- Bars of variable section
- Round rings
- Strings

Plates

- Rectangular plates
- Round plates

Shell

- Cylindrical shell**
- Conical shell

Other oscillation problems

- Reference data about internal friction

Static analysis

- Round plates
- Rectangular plates
- Spherical domes

Auxiliary calculations

- Polynomial roots
- Moments of inertia of simple bodies
- Geometrical properties
- Determinant of matrix
- Inverse matrix
- Linear equation systems

Diagram of a cylindrical shell with radius R , thickness h , and length L .

Параметры

Material: Stainless steel

Number of frequencies: 4

Elasticity modulus, E : 21000000 T/m²

Poisson ratio, ν : 0.3

Specific weight, ρ : 7.85 T/m³

Shell length, L : 1 m

Radius, R : 20 m

Thickness, h : 0.12 m

Result

#	m_1	m_2	number of oscillations per second
1	1	0	1853.775
2	1	1	1854.226
3	1	2	1855.579
4	1	4	1860.991

SCAP Office

Report Help Parameters Find Calculate Exit

The object of consideration is a natural oscillation of a cylindrical shell with freely supported ends.

The source data for this analysis include the radius and the thickness of the shell; the elasticity modulus, Poisson ratio, and the specific weight of the material the shell is made of (the latter data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list); the desired number of frequencies.

The result of the analysis will be values of the *frequency of oscillations in Hz (measured as the number of oscillations per second)* and the *circular frequency in rad/s* for a few lower natural oscillation modes. Also, the table of results will list wave numbers (m_1 , m_2) for the respective natural modes.

References

[1] *Strength. Stability. Oscillations. Vol. 3* (eds. I.A. Birger, Y.G. Panovko), Moscow, Mashinostroyeniye Publishing House, 1968, 567 pp. (See p. 429.)

29. Conical shell

Conical shell

Source data

Material: Steel special

Number of frequencies: 5

Specific weight, ρ : 7.85 T/m³

Elasticity modulus E: 21000000 T/m²

Poisson ratio, ν : 0.3

Shell height, L: 5 m

Radius, R: 6 m

Thickness, h: 0.2 m

Half-opening angle, α : 60 degree

Result

#	m1	m2	number of oscillations per
1	1	3	428.246
2	1	2	473.46
3	2	3	495.204
4	1	4	514.746
5	2	2	533.335

The object of consideration is a natural oscillation of a conical shell with freely supported ends.

The source data for this analysis include the radius, height, and thickness of the shell; its half-opening angle; the elasticity modulus, Poisson ratio, and the specific weight of the material the shell is made of (the latter can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected in the material list); the desired number of frequencies.

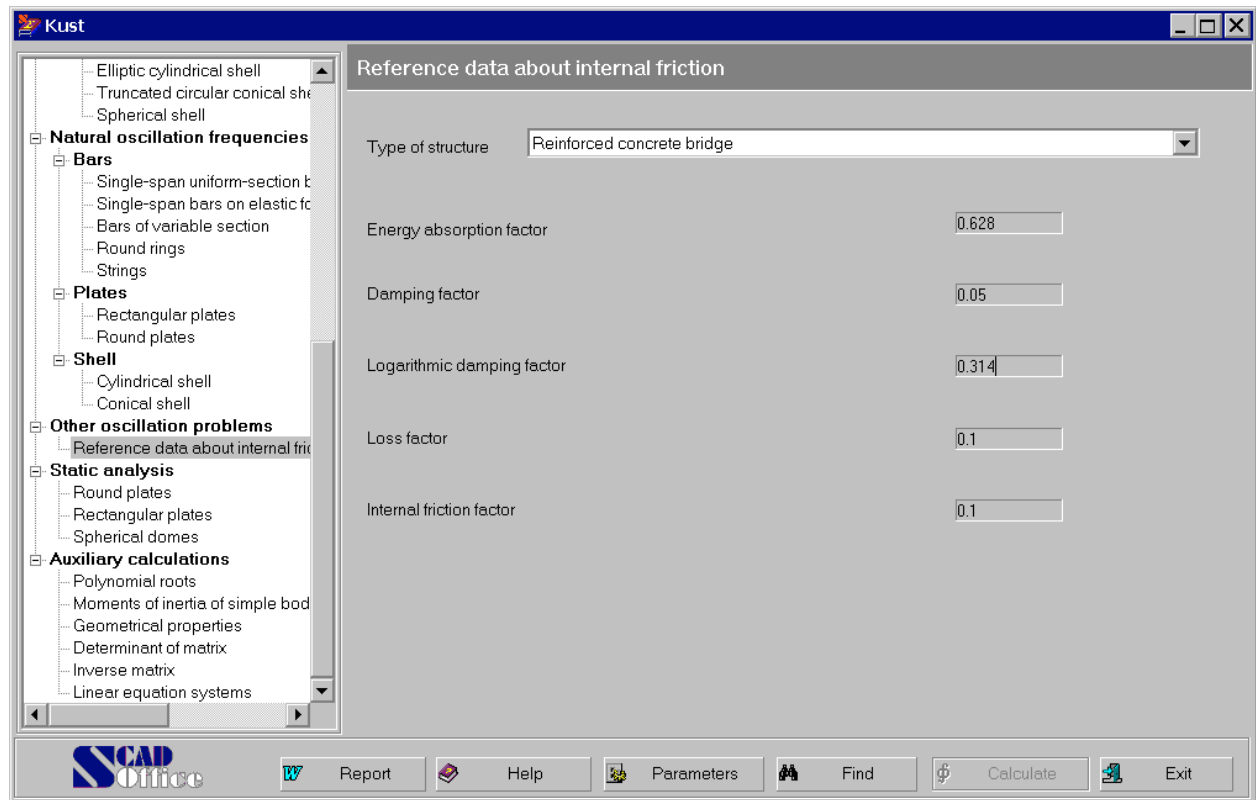
The result of the analysis will be values of the *frequency of oscillations in Hz (measured as the number of oscillations per second)* and the *circular frequency in rad/s* for a few lower natural oscillation modes. Also, the table of results will list wave numbers (m_1 , m_2) for the respective natural modes.

References

[1] *Strength. Stability. Oscillations. Vol. 3* (eds I.A. Birger, Y.G. Panovko), Moscow, Mashinostroyeniye Publishing House, 1968, 567 pp. (See p. 457.)

Other oscillation problems

30. Reference data about internal friction



Various design codes use different forms of representation to describe the internal energy loss, such as:

- ◆ energy absorption factor;
- ◆ damping factor;
- ◆ logarithmic damping factor;
- ◆ loss factor;
- ◆ internal friction factor.

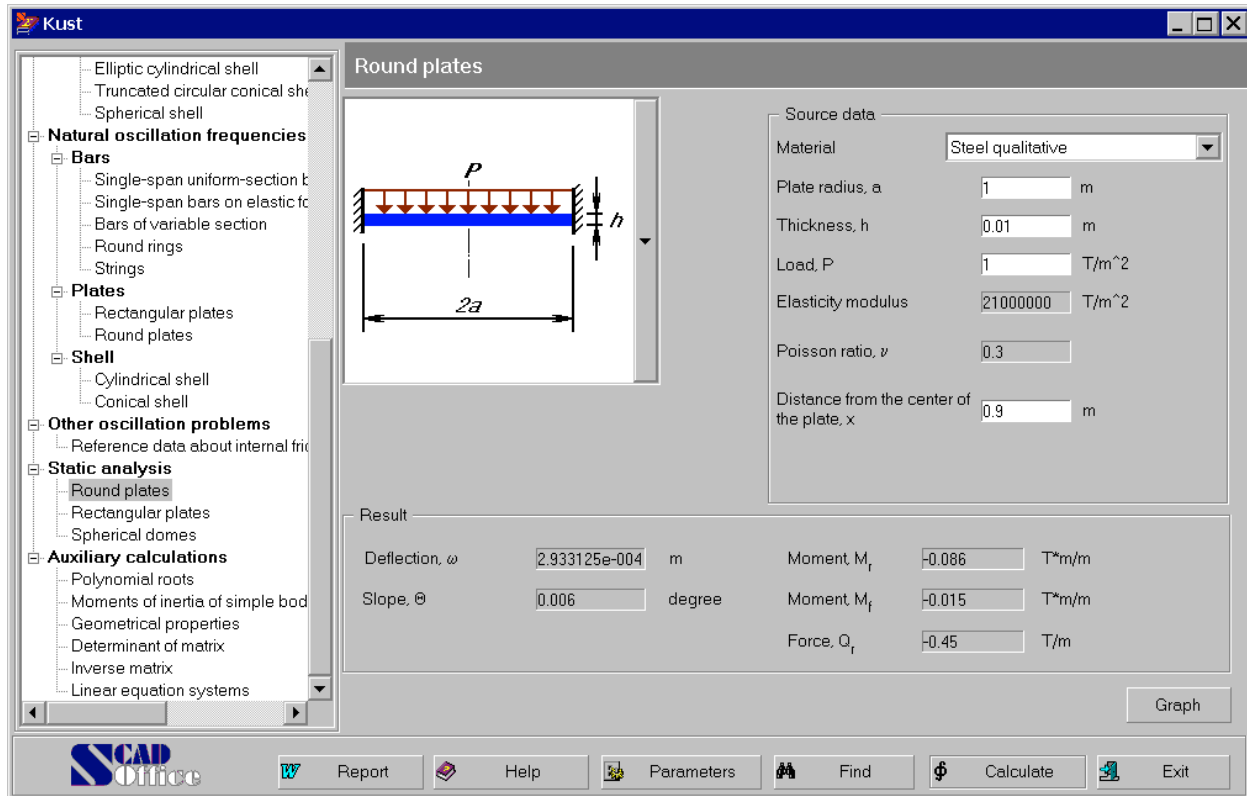
This mode lets you obtain all listed values by selecting a type of structure from the drop-down list. If the OTHER CONSTRUCTION TYPES option has been selected in the construction list, you can enter a value for one of the quantities and obtain all the other ones by clicking the **Calculate** button.

References

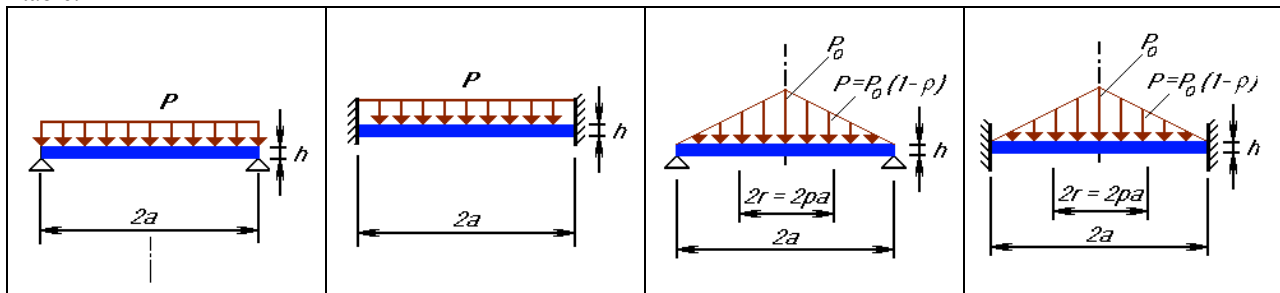
[1] *Dynamical structural analysis* (Designer's reference manual), Moscow, *Stroyizdat* Publishing House, 1984, 303 pp. (See Section 3.)

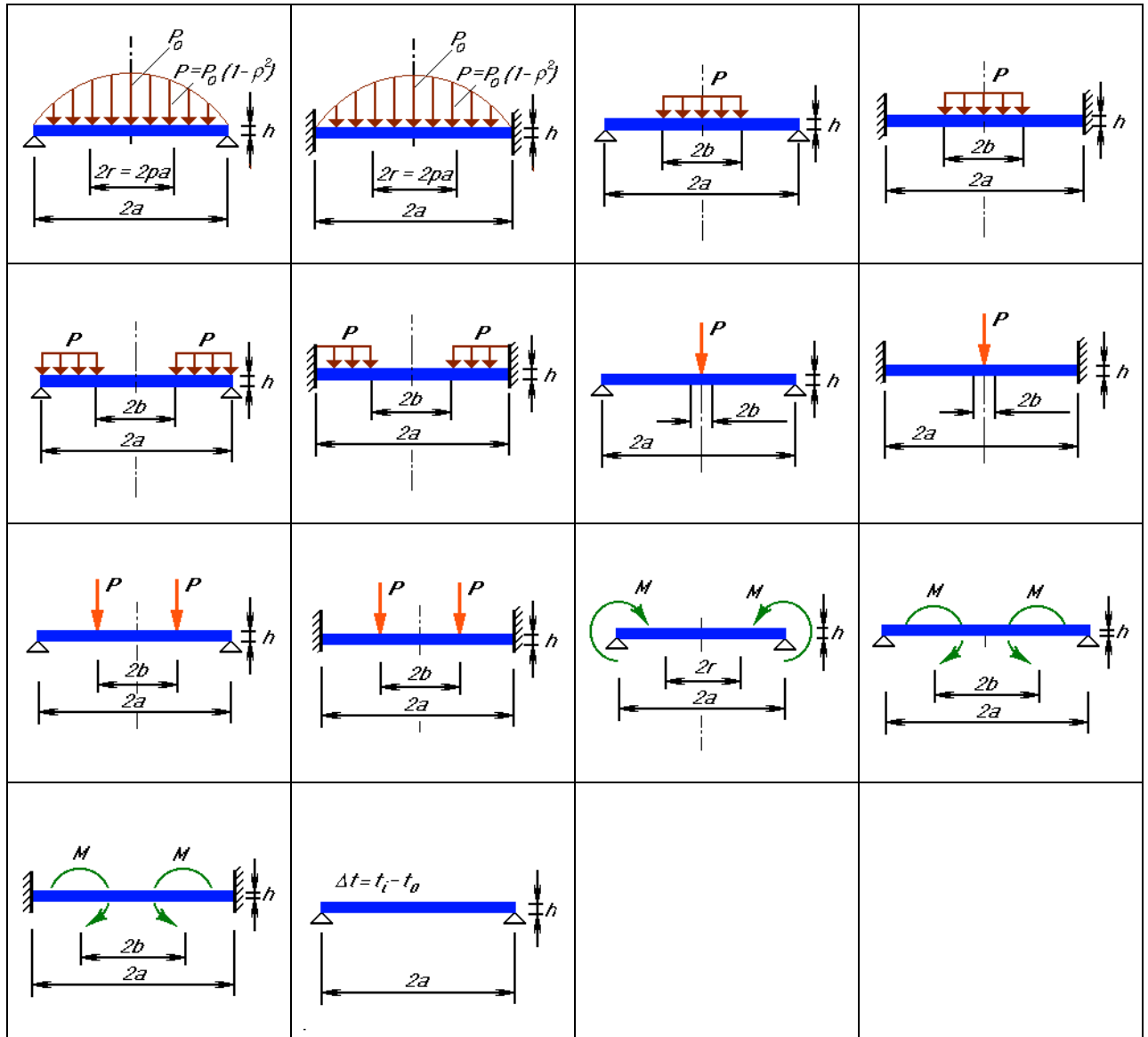
Static analysis

31. Round plates



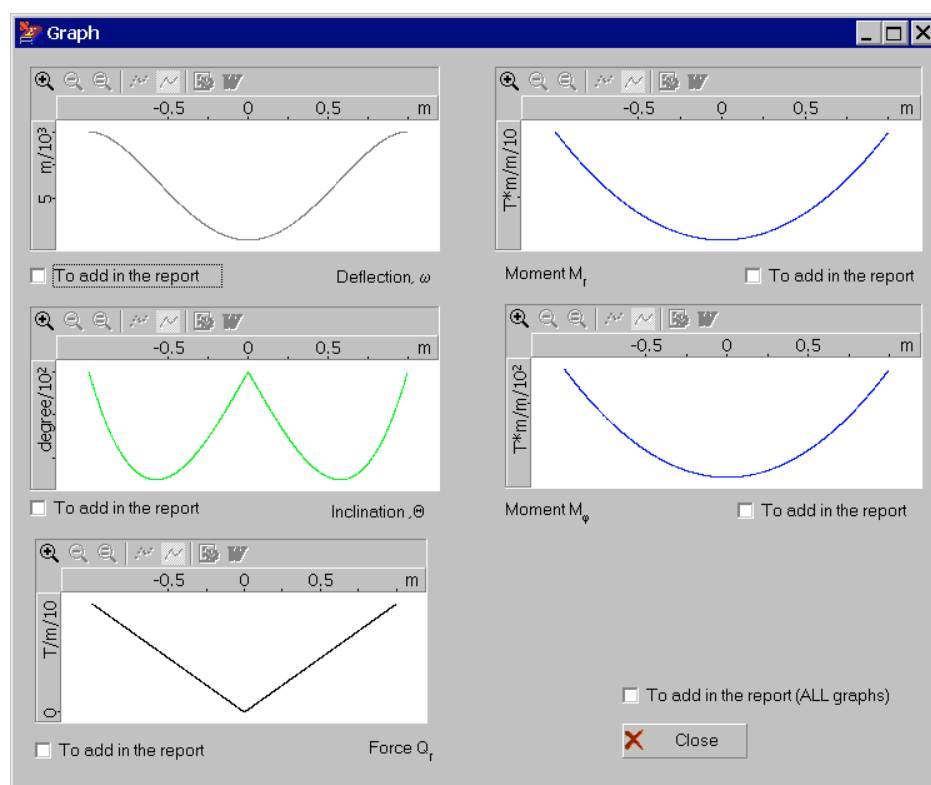
The object of consideration is a round plate supported in a variety of ways and loaded according to various symmetrical patterns. All situations where the static analysis can be performed by the program are listed below in a table.





The source data for this analysis include the radius of the plate and its thickness; also, the value of the load (and its position if necessary) must be specified. Together with those, you specify the elasticity modulus and the Poisson ratio of the material the plate is made of (these data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected from the material list).

If a point is specified by the user at the distance x from the center of the plate (optionally), the program can calculate the deflection, slope, shear force, and both tangential and radial moments. Also, clicking the **Plots** button will show plotted curves of the listed values.



The **Plots** dialog box lets you include any of the curves in the report document by setting or dropping the respective checkboxes.

References

[1] *Reference manual on elasticity* (ed. by P.M. Varvak), Kiev, Budivelnik Publishers, 1971, 416 pp. (See p. 335.)

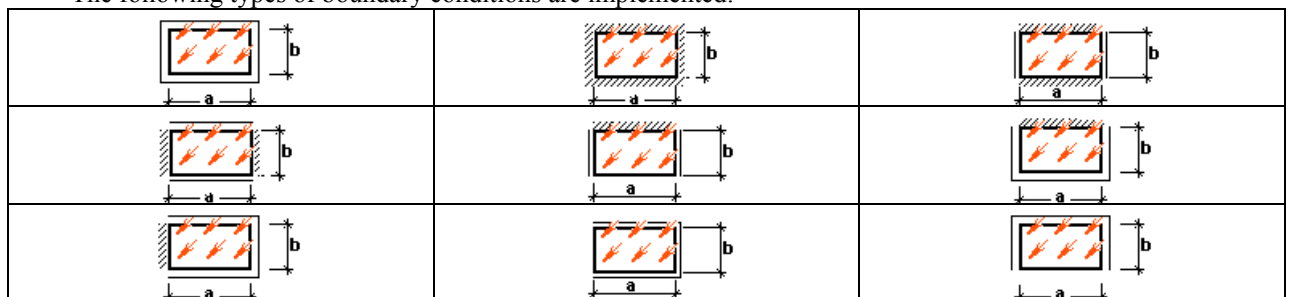
32. Rectangular plates

The screenshot shows the Kust software interface for analyzing rectangular plates. The left sidebar contains a tree view with categories: Natural oscillation frequencies, Bars, Plates, Shell, Other oscillation problems, Static analysis, and Auxiliary calculations. The 'Rectangular plates' option is selected under the 'Plates' category. The main window displays the 'Rectangular plates' analysis form. It includes a diagram of a rectangular plate with dimensions 'a' and 'b' and a uniformly distributed load 'P'. The 'Source data' section contains input fields for Material (Concrete heavy B60), Elasticity modulus, E (4080000 T/m²), Poisson ratio, ν (0.2), Thickness, h (0.2 m), Length, a (3 m), Width, b (5.2 m), and Load, P (23.4 T/m²). The 'Result' section shows the Maximum stress, σ_{\max} (1247.695 T/m²) and Deflection, y_{\max} (0.198 m). The bottom of the window features a toolbar with buttons for Report, Help, Parameters, Find, Calculate, and Exit.




The object of consideration is a rectangular plate fixed at its edges in a variety of ways and loaded by a uniformly distributed pressure orthogonal to the surface of the plate.

The source data for this analysis include the planar sizes of the plate and its thickness, and the intensity of the load. Also, the elasticity modulus and the Poisson ratio must be specified for the material the panel is made of (these data can be specified by selecting a material from the database or by entering explicit values if the OTHER MATERIAL option has been selected from the material list).

The following types of boundary conditions are implemented:



The schemes above use the following notation for edge fixation types:

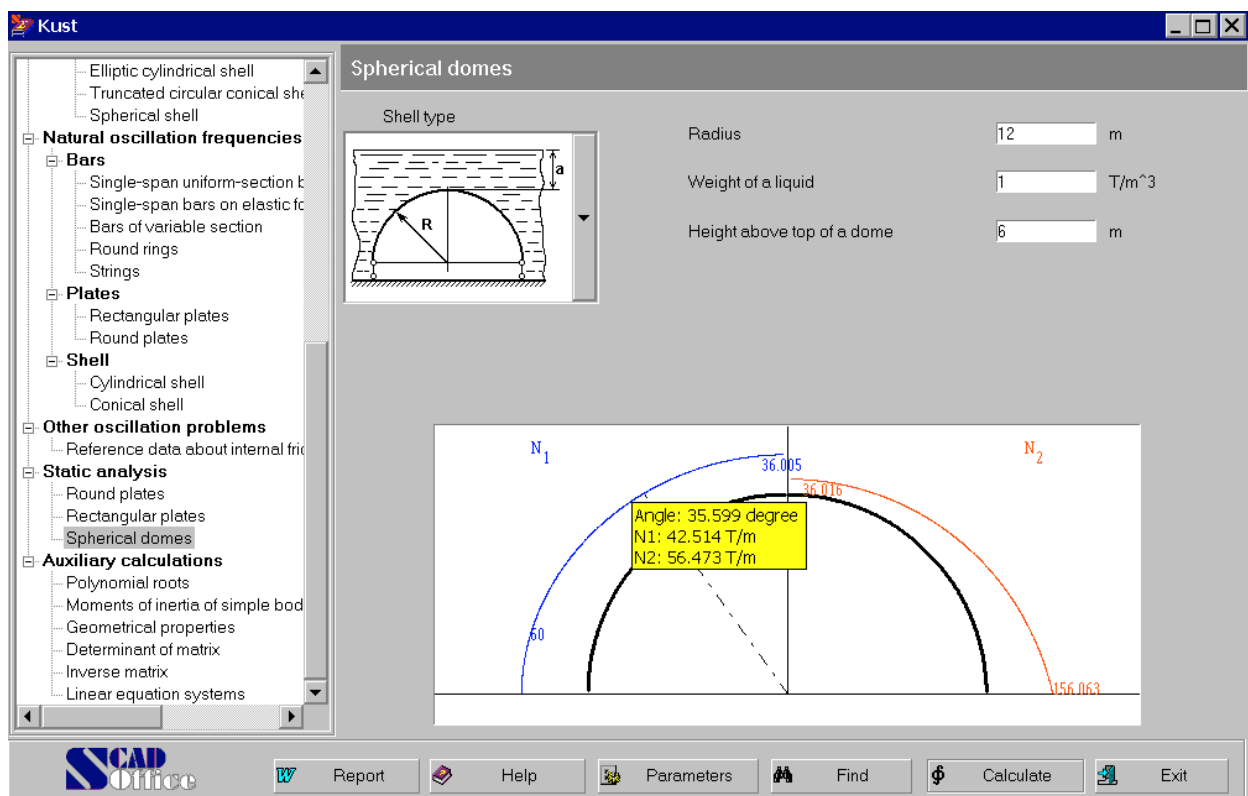
Free edge	
Clamped edge	
Simply supported edge	

The result of this analysis will be the *maximum stress* σ and the *maximum deflection*.

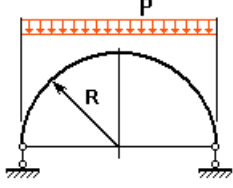
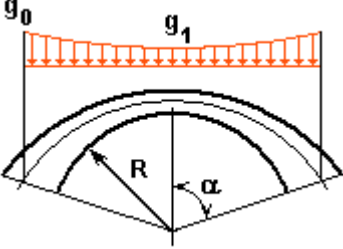
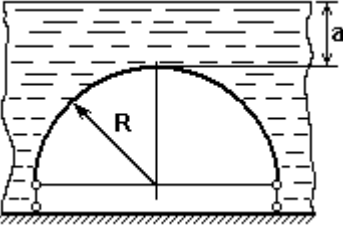
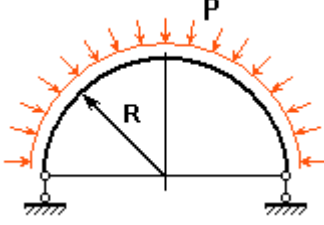
References

[1] *Reference manual on elasticity* (ed. by P.M. Varvak), Kiev, Budivelnik Publishers, 1971, 416 pp. (See p. 376.)

33. Spherical domes



The object of consideration is a spherical dome simply supported at its edge and subjected to the following types of loads:

	Uniform load on the horizontal projection
	Dead weight load
	Water load
	Uniform external pressure

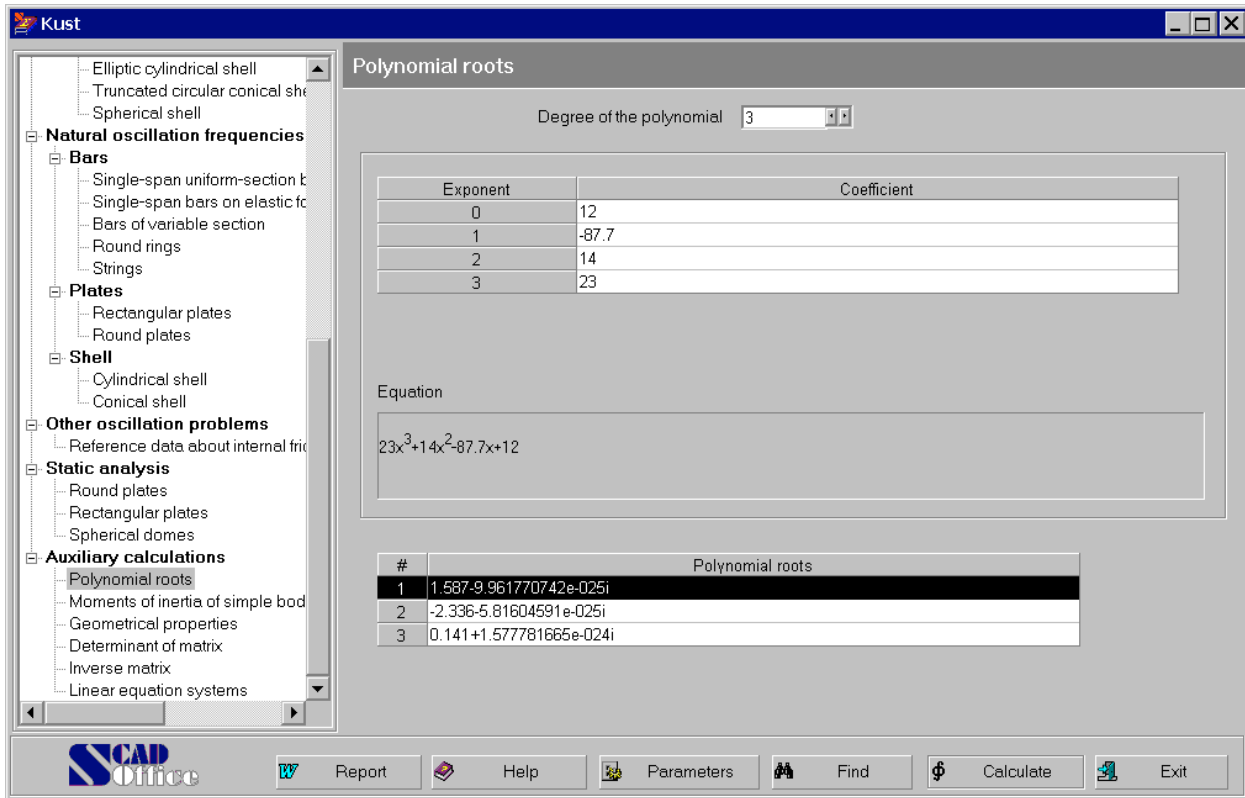
The source data for the analysis include the radius of the dome and the load's intensity. Clicking the **Calculate** button will display diagrams of tangential stress components in the meridional and annular directions (N_1 , N_2). These diagrams suggest a dynamic digitizing feature: point at a location, and the corresponding values of the functions will be displayed immediately.

References

[1] *Structural designer's reference manual. Design theory and analysis Vol. 2* (ed. by A.A. Umansky), Moscow, Stroyizdat Publishing House, 1973, 415 pp. (See p. 95.)

Auxiliary calculations

34. Polynomial roots



Here the problem is to find all solutions to the equation

$$\sum_{i=0}^n a_i x^i = 0,$$

having real-value coefficients $a_i, i = 0, \dots, n$.

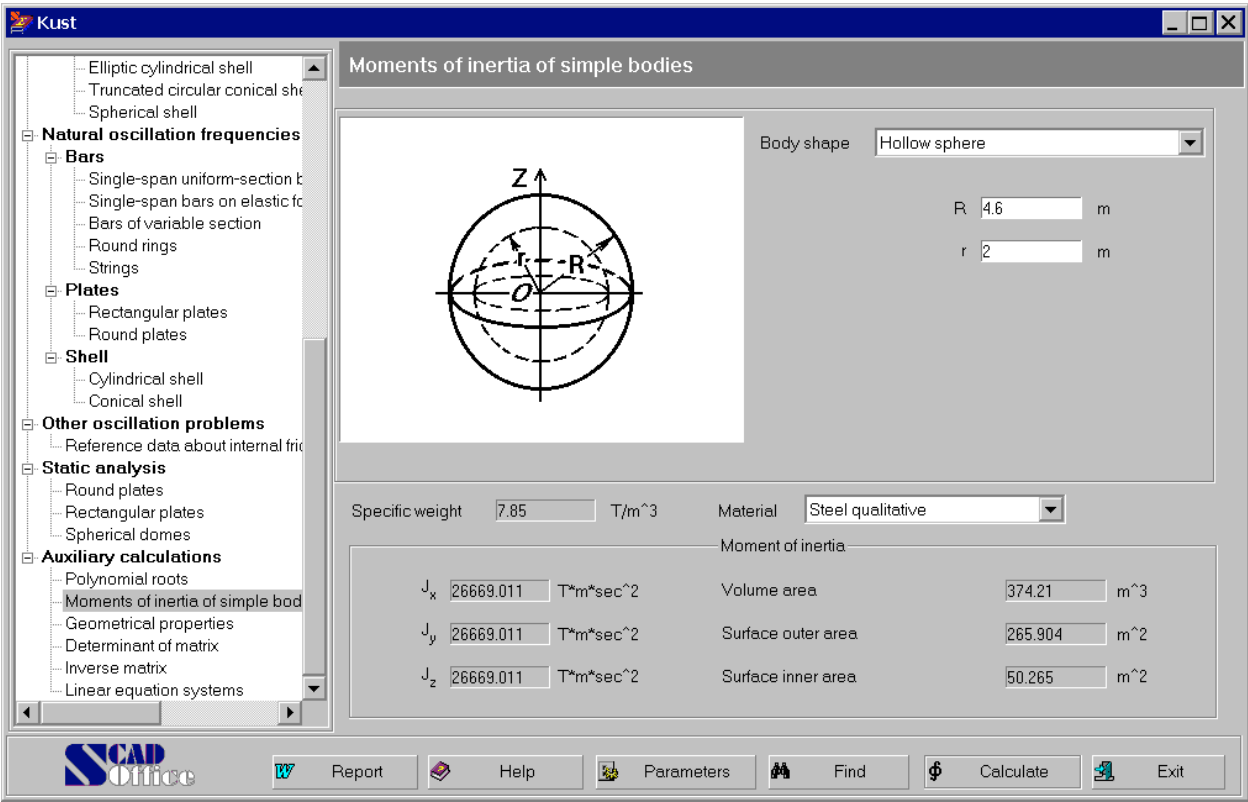
To have this problem solved, specify the degree of the polynomial and fill in the table of its coefficients. After the equation gets solved, the table at the bottom of the window will display all (both real and complex) roots of the given polynomial.

The solution is obtained by Muller's method of iterations.

References

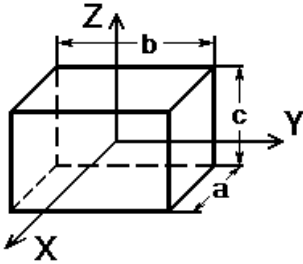
[1] W.H. Press, B.P. Flannery, S.A. Teukolsky, W.T. Vetterling, *Numerical Recipes in C: The Art of Scientific Computing, 2nd ed.* Cambridge, England: Cambridge University Press, 1992. (See [1, Section 9.5].)

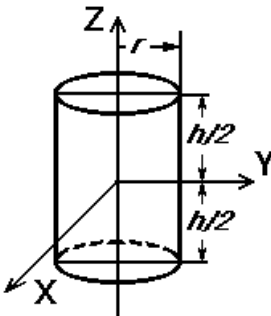
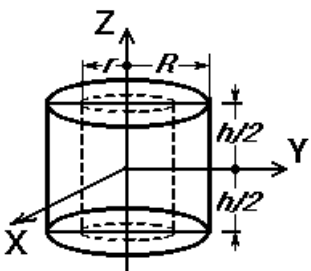
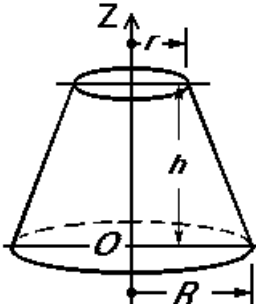
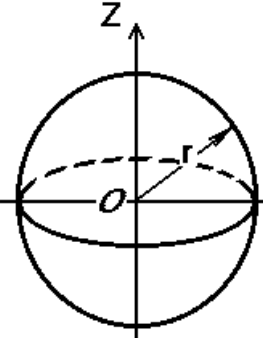
35. Moments of inertia of simple bodies

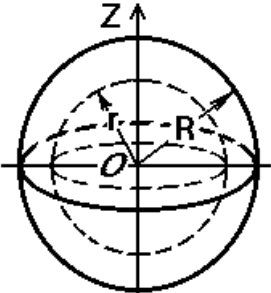
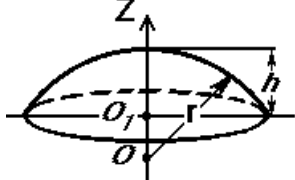
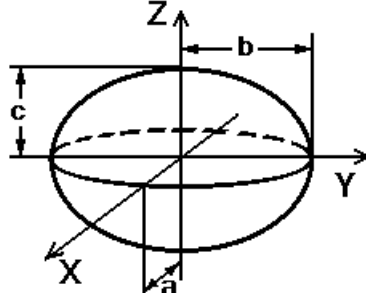


This mode lets you calculate the *moments of inertia* of bodies of simple geometrical shapes, together with their *volume* and *surface area(s)*. The available shapes are listed below. The source data for this calculation include the specific weight (density) of the material. This data can be specified by choosing a material from the database or by explicitly entering the number if the OTHER MATERIAL option has been selected from the material list. Also, you may be required to specify some geometrical sizes depending on the selected shape.

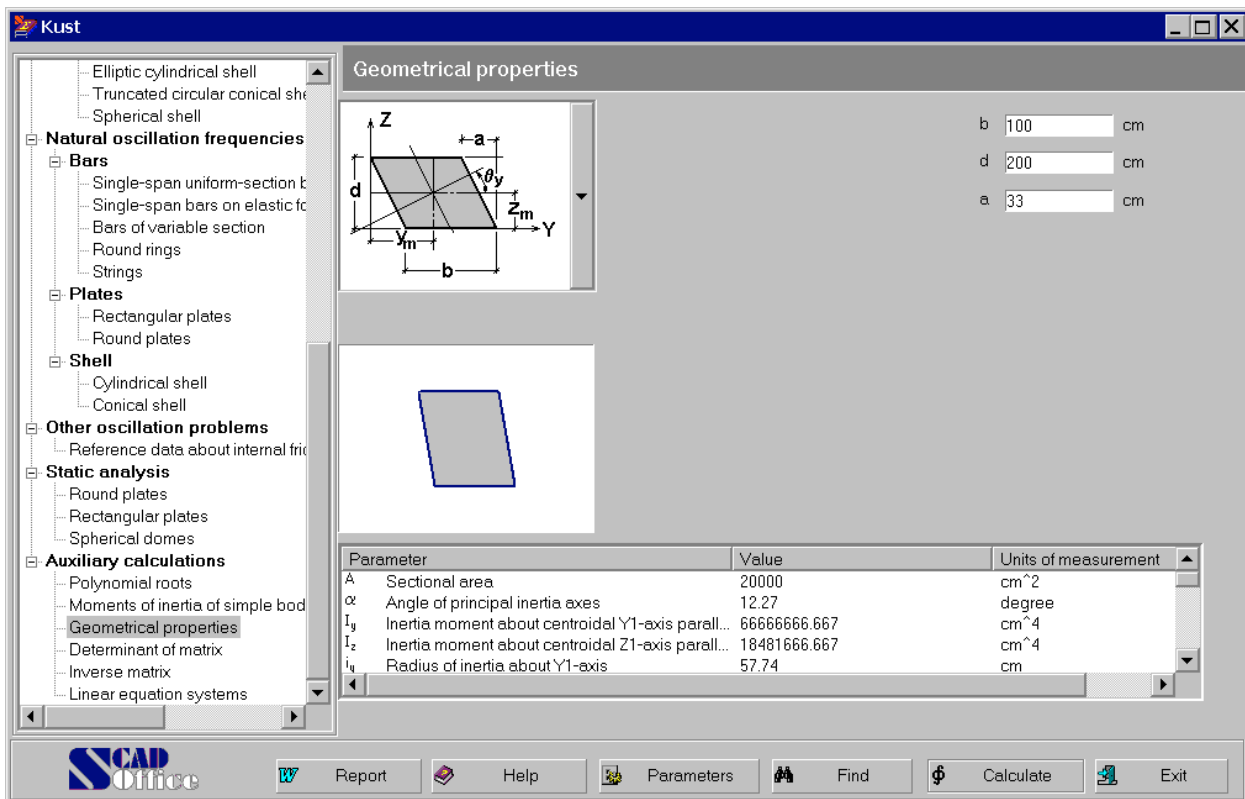
Rectangular parallelepiped



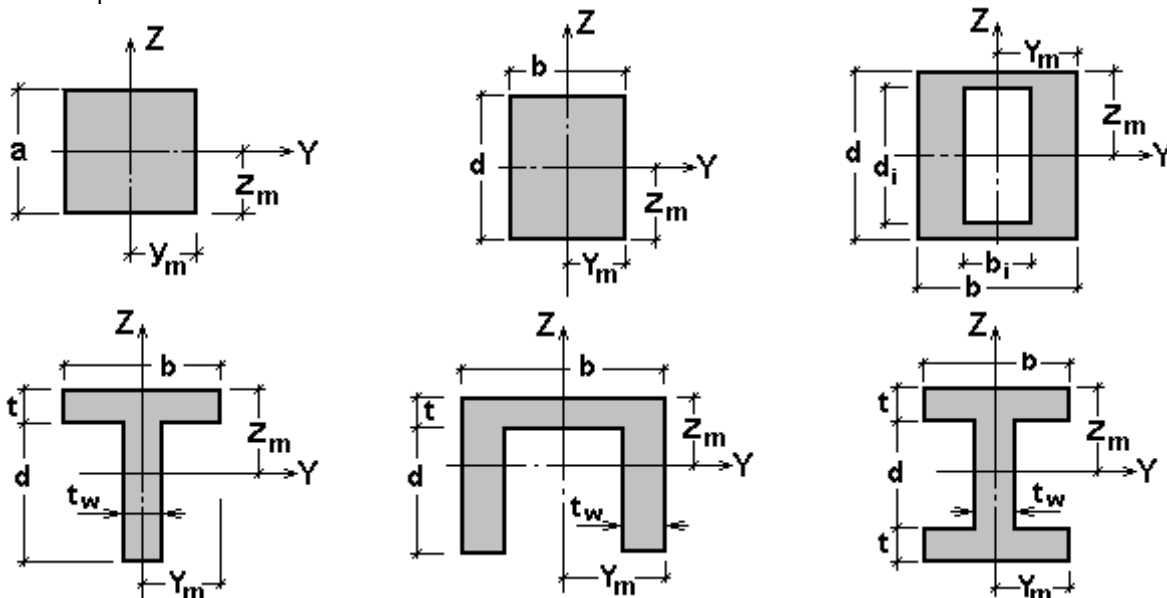
Cylinder	
Quill cylinder	
Straight truncated cone	
Sphere	

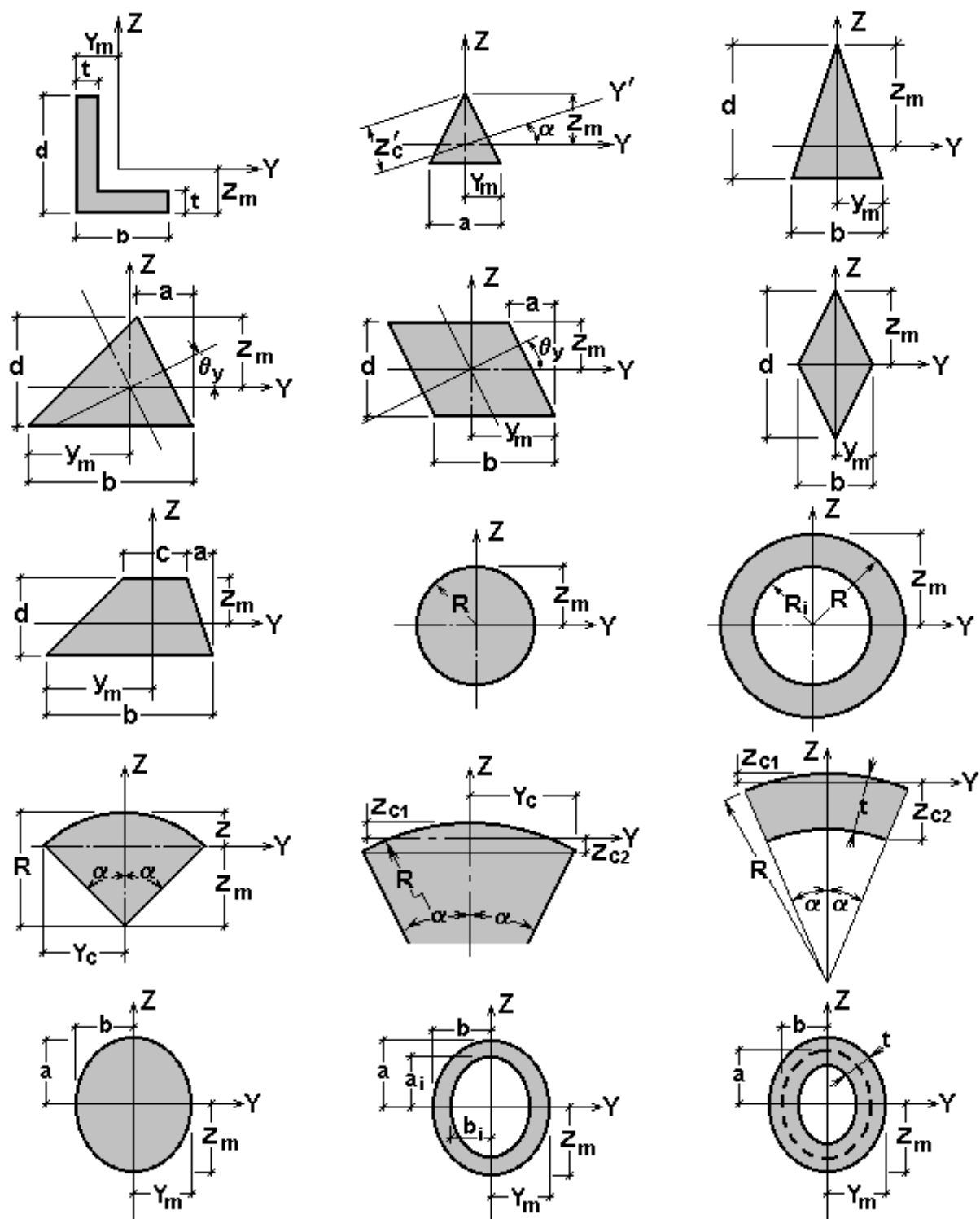
Hollow sphere	 <p>A diagram of a hollow sphere centered at point O. It has an inner radius r and an outer radius R. A vertical Z-axis passes through the center. Dashed lines represent the hidden parts of the sphere's equator and the inner surface.</p>
Sphere segment	 <p>A diagram of a sphere segment. The center of the sphere is O, and the center of the flat base is O_1. The radius of the sphere is r, and the height of the segment is h. A vertical Z-axis passes through O. Dashed lines show the hidden part of the sphere's equator.</p>
Ellipsoid	 <p>A diagram of an ellipsoid centered at the origin of a 3D coordinate system with axes X, Y, and Z. The semi-axes are labeled a (along the X-axis), b (along the Y-axis), and c (along the Z-axis). Dashed lines represent the hidden parts of the ellipsoid's equator and the Y-axis.</p>

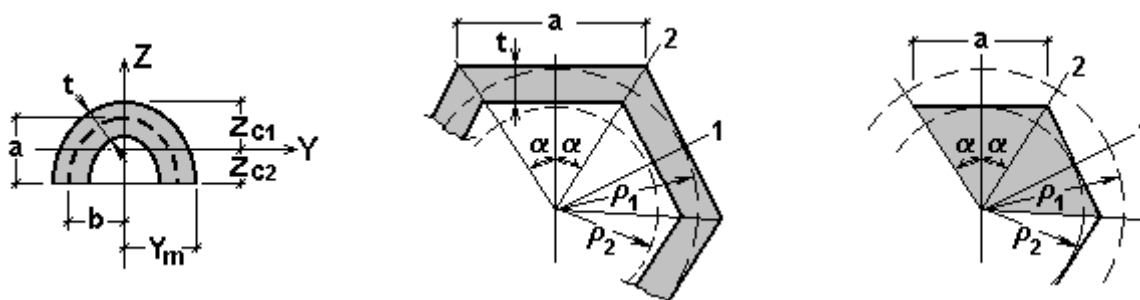
36. Geometrical properties



This mode helps you calculate geometrical properties (such as the area, moments and radii of inertia, ...) of various shapes shown in the table below.





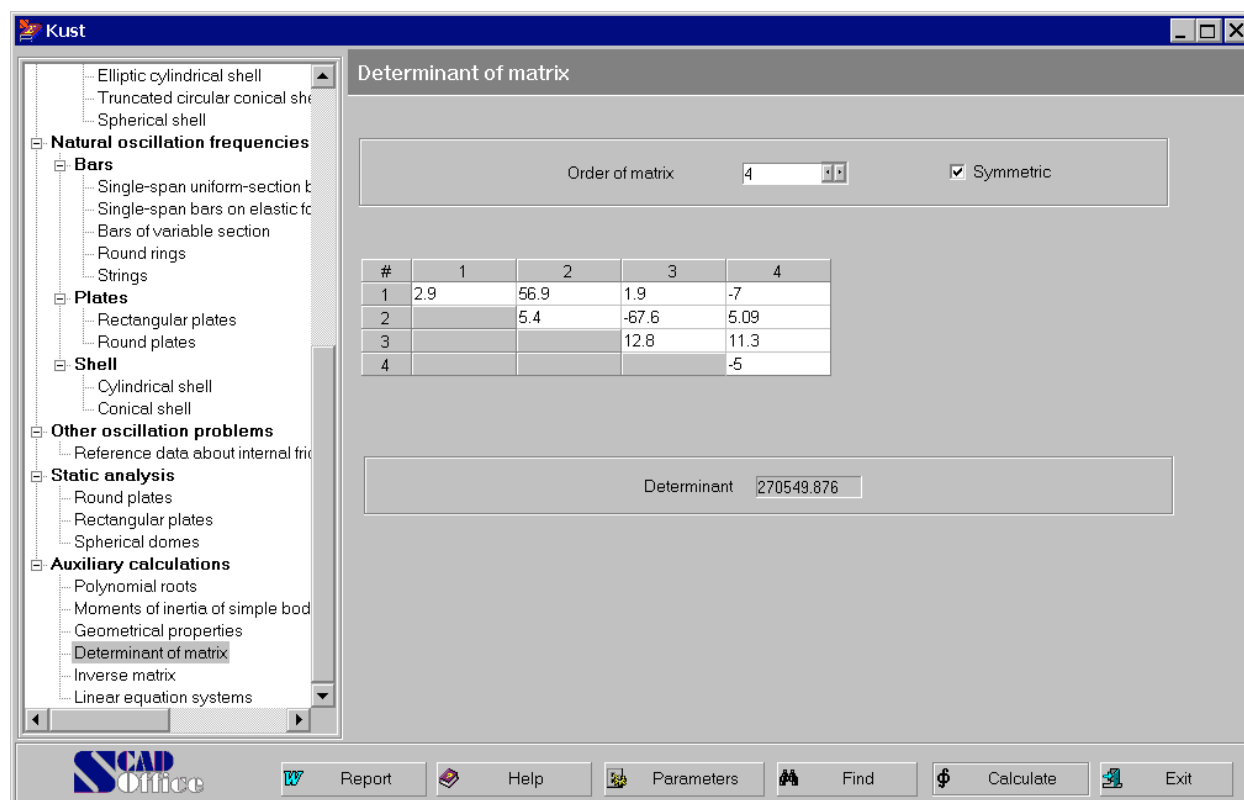


To calculate the properties, choose a desired shape in the corresponding drop-down list, specify required sizes (depending on the shape selection), and click the **Calculate** button. The calculated properties will be displayed in a table at the bottom of the window.

References

- [1] W.C.Young, R.G.Budynas, *Roark's formulas for stress and strains, Seventh Edition*, 2002, ISBN 0-07-072542-X, 2001, 832 pp.
- [2] I.A. Birger, Y.G. Panovko et al., *Strength, stability, oscillation Vol. 1*, Moscow, "Mashinostroyeniye" Publishers, 1988, 831 pp. *In Russian*.

37. Determinant of matrix



This mode lets you calculate the determinant of any given matrix, with its order not to exceed 50. To enter

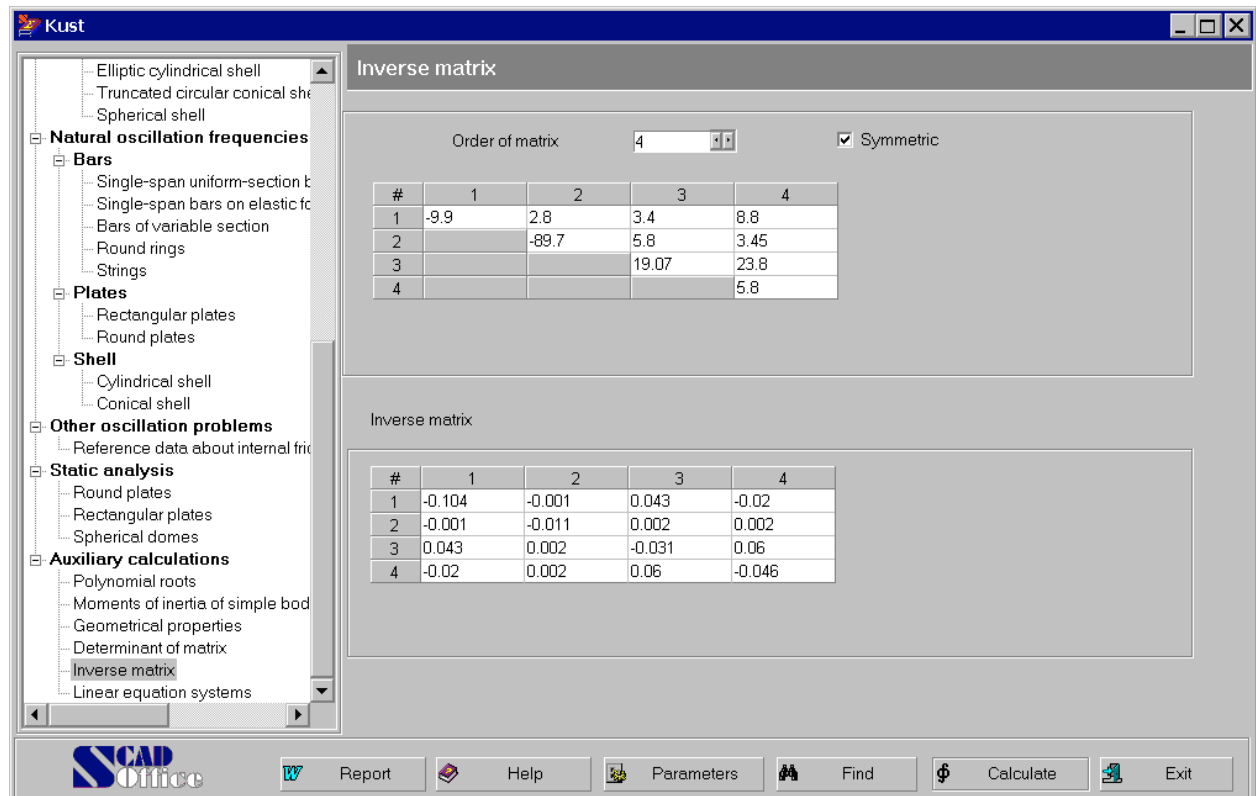
the source data, specify the order of the matrix and then fill in its table of coefficients. If the **Symmetric** checkbox is checked, only coefficients of the symmetric matrix's top triangle should be specified.

The result of the calculation will be the *determinant* of the given matrix.

References

1. F.R. Gantmacher, *Theory of matrices*, Moscow, Nauka Publishers, 1967, 576 p.

38. Inverse matrix



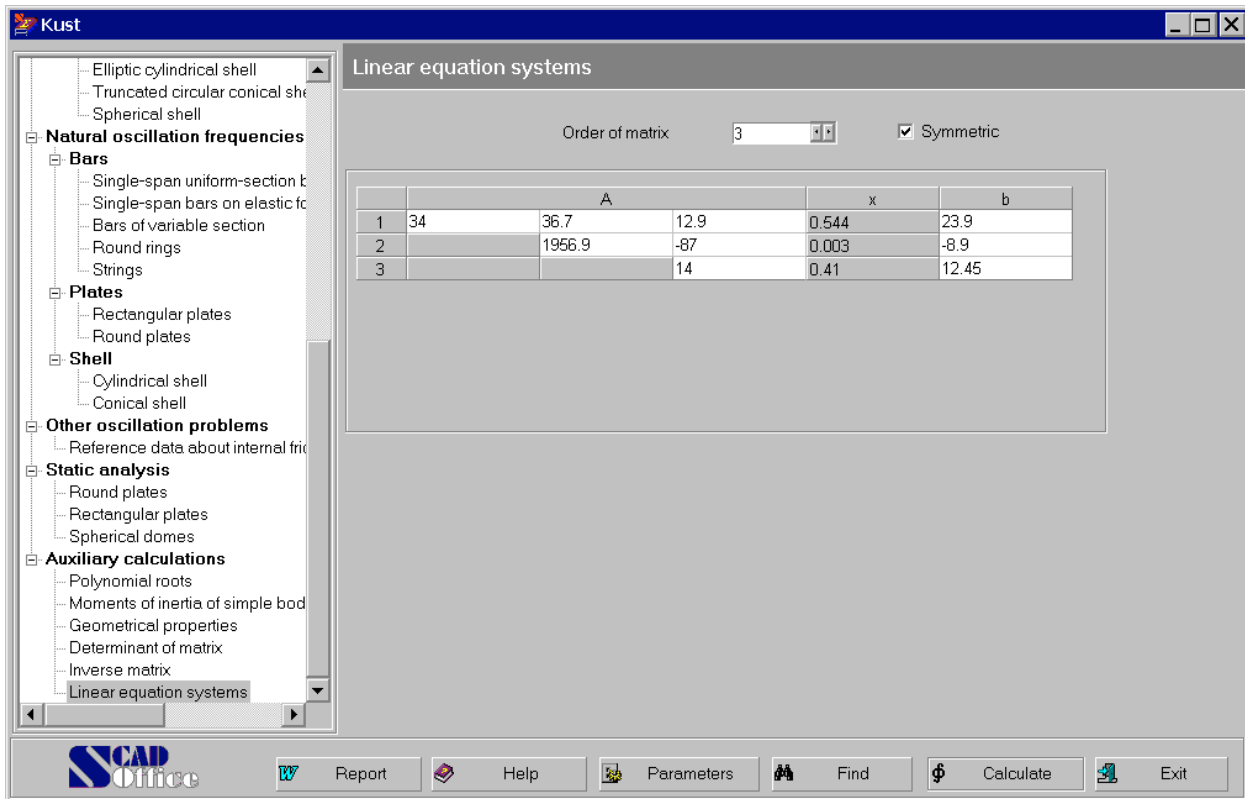
This mode lets you calculate the inverse matrix of any given one, with its order not to exceed 50. To enter the source data, specify the order of the matrix and then fill in its table of coefficients. If the **Symmetric** checkbox is checked, only coefficients of the symmetric matrix's top triangle should be specified.

The result of the calculation will be the *inverse matrix* displayed in a table at the bottom of the editor's window.

References

1. F.R. Gantmacher, *Theory of matrices*, Moscow, Nauka Publishers, 1967.

39. Linear equation systems



This mode enables you to solve a system of linear equations $\mathbf{Ax} = \mathbf{b}$ with any given matrix \mathbf{A} (its order is not to exceed 50) and the right-part vector \mathbf{b} . To enter the data, specify the order of the matrix, and then fill in the table of its coefficients. If the **Symmetric** checkbox is checked, only coefficients of the symmetric matrix's top triangle should be specified. Enter the right-part vector \mathbf{b} in the table under the header \mathbf{b} .

The result of the calculation will be a vector of unknowns \mathbf{x} displayed in a table under the header \mathbf{x} .

References

1. F.R. Gantmacher, *Theory of matrices*, Moscow, Nauka Publishers, 1967.