

Modern Rolling-Element Bearing Analysis Software

USER'S MANUAL (Updated for Version 2.2)

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1.0 Getting Started

1.1 System Requirements

The following minimum system requirements are needed to run ORBIS.

- Windows 7/Vista/Windows XP/Windows 2000/Windows 2003/Windows 2008 Server
- Display monitor with minimum resolution of 1024 by 768 pixels
- 128 MB of free disk space
- 256 MB RAM
- Available USB port
- Java 6.0 or greater (see below for more details)

1.2 End User License Agreement

You must accept the terms and conditions specified in the End User License Agreement before installing and using ORBIS. The agreement is provided during the installation routine and is also located within the ORBIS folder on the CD.

1.3 Installation Instructions

Run the automated installer steps below to complete installation.

- 1. Insert the installation CD and navigate to your CD directory.
- 2. Double click the *Setup.exe*
- 3. Follow installer instructions to complete installation.

1.4 Java Runtime Environment

In order for the software to run properly, the host computer must have Java Runtime Environment (JRE) version 6.0 or greater installed. The JRE is an industry standard and will generally already be installed on most modern computers. If your computer does not have JRE 6.0 or greater already installed you may install the version included from the installation directory or download the latest version from the Sun/Oracle website (www.oracle.com). To install the version included from the ORBIS CD follow these steps.

- 1. Open the Java folder on the CD (\\ORBIS\Java\)
- 2. Double click *jre-6uXX-windows-i586-s.exe* to install on Windows platforms (Windows 7, Vista, Windows XP, Windows 2000, Windows 2003, and Windows 2008 Server). Note: the 'XX' in the filename denotes the particular update to the JRE Version 6.

2.0 User Interface

2.1 Main Graphical Interface

The main graphical interface allows the user to define their bearing system and perform analysis runs. See subsequent sections (2.1.X) for detailed information about each input within the main graphical interface. Once all necessary inputs have been entered the user selects the Analyze button to perform their analysis. A new window will appear containing the analysis results. See section 2.3 for a description on the Results window and section 4.0 for a detailed description on each output parameter.



Figure 1. Main Graphical Interface

2.1.1 System Inputs

The System Inputs area is where external loading and system material definitions are defined. See the following figure for detailed descriptions of each input field.



		Fx (lbf); 1 Fy (lbf); 2 Fz (lbf); 3 Fyy (in-lbf); 4 Fzz (in-lbf); 5 Load Location (in): 6 Shaft Temperature (F): 7 Housing Temperature (F): 8 Allowable Mean Hertzian Stress (psi): 9 Shaft Material: 10 Lubricant: 12		
#	Title	Description		
1	Fx (lbf)	External axial load component (positive is toward the right)		
2	Fy (lbf)	External radial load component (positive is upwards)		
3	Fz (lbf)	External radial load component (positive is out of the page)		
4	Fyy (in-lbf)	External moment about the Y-Axis		
5	Fzz (in-lbf)	External moment about the Z-Axis		
6	Load Location (in)	Location of external load point (along X-Axis)		
7	Shaft Temperature (F)	Bulk temperature of the shaft		
8	Housing Temperature (F)	Bulk temperature of the housing		
9	Allowable Mean Hertzian Stress (psi)	Allows user to specify an allowable contact stress. All elements with contact stress above the specified allowable will be highlighted in the output file.		
10	Shaft Material	Allows user to assign shaft material from the material database		
11	Housing Material	Allows user to assign housing material from the material database		
12	Lubricant	Allows user to assign lubricant to all bearing rows from the lubricant database		

Figure 2. System Inputs

2.1.2 Dynamic Analysis Inputs

ORBIS offers both static and dynamic analysis modes. See the following figure for detailed descriptions of the available options. Dynamic analysis mode provides additional user output parameters (such as torque, fatigue life, film parameters, centrifugal and gyroscopic forces, etcetera).



		1 ✓ Perform Dynamic Analysis [•] Shap a tates [•] Housing Rotates [•] Housing Rotates [•] Load fixed to shaft [•] Load fixed to housing [•] Velocity (rpm): [•] Life Factor: [•] 6
#	Title	Description
1	Dynamic Analysis Checkbox	Selection of this checkbox activates the dynamic analysis inputs. Default is un-checked.
2	Rotational Member	Radio buttons allow user to specify either 'shaft rotates' or 'housing rotates.'
3	Loaded Member	Radio buttons allow user to specify whether load is fixed relative to the shaft or housing.
4	Velocity (rmp)	Defines the rotational velocity, in RPM, of the rotational member
5	Reliability	Defines the reliability for fatigue life. Valid inputs are between 0 and 1, exclusive. Default is 0.9 (L10 equivalent).
6	Life Factor	Allows user to specify an overall combined life adjustment factor. ORBIS will compute reliability and lubricant regime adjustment factors, however other factors such as material and operating environment must included here.

Figure 3. Dynamic Analysis Inputs

2.1.3 System Display

The system display area provides a proportional sketch of the user defined system. See the following figure for a detailed description of the information provided in the system display panel. It is recommended that the user review the system sketch just prior to selecting the analyze button to ensure their setup is correct.



Figure 4. System Display



2.1.4 Bearing Row Inputs

The Bearing Row Input area is where the user defines necessary inputs for each bearing row in the system. See the following figure for a detailed description of each input type.

		2 Define Total # of Bearing Rows: 1 2 Row 1 Row 2 Row 4 Row 5 3 Contact Angle 5 Preload Condition Convergent Cun-Mounted • CDivergent • Un-Mounted Bearing: 9 • • Preload Type • Mounted Row Location (m): 10 • Rigid * Spring I.R. Fitup (m): 11 • Rigid * Spring I.R. Fitup (m): 12 • Shaft I.D. (m): 13 Housing O.D. (m): 14 • Row Preload (lbf): 15 Coeff of Friction, Ball Contact: 16		
#	Title	Description		
1	# Bearing Rows	Drop-down selection allows up to 5 bearing rows to be specified. Row tabs (see #2) will be activated based on number of bearing rows selected here.		
2	Row Tabs	Row tabs are activated based on the number of bearing rows selected. Selecting an active tab allows the user to define parameters for that row.		
3	Contact Angle	Contact angle definition for active row. A divergent contact angle extends away from, or diverges, from the spin axis as you traverse in the positive direction along the x-axis.		
4	Preload Type	Specification for type of preloading. Options are rigid or spring. Rigid preloading activates input fields for inner and outer ring clamping forces. Spring preloading activates inputs for the spring rate.		
5	Preload Condition	Specifies the condition at which the specified preload is defined. Un-mounted conditions means the rings are radially free at the specified preload. Mounted conditions apply the preload force based on the mounted fit-up conditions, which include changes to internal clearance from interference fitting and ring clamping.		
6	I.R. Clamp Load (lbf)	Input field for the inner ring clamp load. Only active for rigid preload type.		
7	O.R. Clamp Load (lbf)	Input field for the outer ring clamp load. Only active for rigid preload type.		
8	Spring Rate (lbf/in)	Input field for the preload spring stiffness. Only active for spring preload type.		
9	Bearing	Drop-down selection to assign the bearing for the active row. The drop-down menu will contain all bearings defined in the user defined bearing database.		
10	Row Location (in)	Input field for the axial location (along x-axis) of the active bearing row.		
11	I.R. Fitup (in)	Input field for the inner ring fitup to the shaft. Fitup is defined as the difference in the shaft O.D. to the free bearing I.D. A positive value indicates interference fits.		
12	O.R. Fitup (in)	Input field for the outer ring fitup to the housing. Fitup is defined as the difference in the free bearing O.D. and the housing I.D. A positive value indicates interference fits.		
13	Shaft I.D. (in)	Specifies the I.D. of a hollow shaft. For non-constant shaft wall thicknesses use the appropriate shaft I.D. at the bearing row location. For a solid shaft input a zero value.		
14	Housing O.D. (in)	Specifies the O.D. of the housing. For non-constant housing wall thicknesses use the appropriate housing O.D. at the bearing row location.		
15	Row Preload (lbf)	Specifies the preload force applied to the active bearing row. Preload forces are directional and must include the appropriate sign convention. To preload a bearing through its contact angle, standard preloading, specify a positive preload for divergent contact angles and a negative preload for convergent contact angles.		
16	Coeff of Friction, Ball Contact	Specifies the rolling contact friction coefficient for the active bearing row.		

Figure 5. Bearing Row Inputs

2.1.5 Input Field Description

The input field description area provides helpful information to the user for all input fields. When the user places their cursor in one of the input fields (done by clicking the mouse in a field or pressing the tab



button to advance to the next input field) a description about that field appears in the Input Field description area. The following figure illustrates this.

	Cursor placed in fi		
Perform Dynamic Analysis Shaft Rotates Pousing Rotates C Load fixed to si C Load fixed to h Velocity (rpm): Reliability: Life Factor:	Preload Type G Rigid C Spring U.R. Clamp Load (bf) O.R. Clamp Load (bf) Coeff of Friction, Ball Contact:		
Enter row inner ring clamping force (lbf, positive value) Analyze Exit			

Figure 6. Input Field Description

2.1.6 User Menus

User menus are available within the main graphical interface. See the following figure for a detailed description of the available menu options.

	1 File Op Sa Sa Ex	BIS - Bearing Analys ORBIS - Bearing Analysis Software Tools Help ren Ctrl+O ve Ctrl+S ve As 5 it Ctrl+E
#	Title	Description
1	File Menu	The file menu provides standard file options such as Open, Save, Save As and Exit. ORBIS maintains its own file type that allows the user to save their bearing analysis setup. All parameters within the main graphical interface are preserved.
2	Tools Menu	The tools menu provides advanced analysis utilities.
3	Batch Process Load Cases	Selecting this utility allows the user to load a pre-configured comma delimited file with an unlimited number of load cases. Each load case is applied to the current defined bearing system and the results are saved to separate results files.
4	Sensitivity Studies	Selecting this utility launches the Sensitivity Studies window. See section 2.4 for a detailed explanation of the powerful capabilities of this utility.
5	Tolerance Studies	Selecting this utility launches the Tolerance Analysis window. See section 2.5 for a detailed explanation of the powerful capabilities of this utility.
6	System Preferences	Selecting this utility launches the System Preferences window. See section 2.6 for a detailed explanation of the powerful capabilities of this utility.

Figure 7. User Menu's



2.2 Database Editors

Database editors allow the user to view, modify, add and delete bearing, material, and lubricant database entries. The database editors are accessed from the buttons within the System Display area (see section 2.1.3).

Orbis uses bearing, material and lubricant databases to define the majority of input parameters required to perform a bearing analysis. Once the user has defined their database entries they simply assign them to their analysis via drop-down menus.

Bearing Database Editor	Material Database Editor	×	Lubricant Database Editor
Bearing Nuccells Course Ring Bearing Nuccells Sande Bearing Fabring Nuccells Face Registron Pack Demarker (in): 2.400 Fee Contrast Anale (deg): 250 Element Nomers (in): 530 Reverse Contrast: 230 PMS Roughness (Micrond): 53 Land Height (h(d): .200 Dem Height (h(d): .200 Edit Materials .200 Delete E	Miderial Properties Miderial Properties Miderial Name: 440C Starriess Young's Modulas (spi): 2.5%7 Poisson's Rator; 25 Specific Dentry (Ibun)m-3):382 Coefficient of Thermal Expansion (ni)n-F): 5.67e-6 Clear Entries Add To Database #40C Starriess User Entries Delete From Database Close		Lubricant Properties Lubricant Name: Sample Lubricant Atmospheric Viscosity (Ibl-scipin*2): 1.332e-6 Pressure Coefficient of Viscosity (In*2)Ib): 1.82e-4 NOTE: Atmospheric viscosity and the pressure coefficient of viscosity values must pertain to the lubricant temperature Clear Entrites Add To Database Lubricant Sample Lubricant Univers Delete From Database Close
Close	1		

Figure 8. Database Editors

2.2.1 Bearing Database Editor

The Bearing Database Editor allows you to view, edit, add or delete bearing definitions to the bearing database. See the following figure for a detailed description of the editor.



	D esistent	
	Bearing Pr	Database Editor X
	Bearing	Name: Fam 1 ring
	Rolling	Elements Inner Ring Outer Ri
	Fre	ee Contact Angle (deg): 3 I.R. width (m): 9 O.R. Width (m): 15
		Element Diameter (in): 4 Raceway Curvature: 10 Raceway Curvature: 16
		Number of Elements: 5 Land Height (h/d): 11 Land Height (h/d): 17
	RMS	Roughness (Microinch): 6 Dam Height (h/d): 12 Dam Height (h/d): 18
		RMS Roughness (Microinch): 13 RMS Roughness (Mircoinch): 19
	Mate	rial: 140C Stain 7 Y Material: 140C Stainless Y Material: 140C Stainless Y
	Edi	t Materials 20 21 Clear All Entries Add To Database 22
	Bearing D	atabase
	Sample	Bearing 23 View/Edit Properties 24
		Delete Entry (25)
	1	
		Close (26)
#	Title	Description
1	Bearing Name	Specify a name for the bearing.
2	Pitch Diameter (in)	Diameter that describes the rolling element centers (often the average between the bearing I.D. and O.D.)
3	Free Contact Angle (deg)	Contact angle of bearing with no external loading. Must be a positive value.
4	Element Diameter (in)	Diameter of the ball.
5	Number of Elements	Number of balls in a single bearing row.
6	RMS Roughness (Microinch)	Surface roughness, RMS, of the ball.
7	Material	Assign materials from Material Database to the rolling elements, inner ring and outer ring.
8	Inner Diameter (in)	Bearing's inner diameter.
9	I.R. Width (in)	Width along the bearing axis of the inner ring.
10	Raceway Curvature	Inner ring curvature, expressed as the ratio of the raceway radius to the ball diameter.
		Height of the land diameter expressed as the ratio of the radial height to the ball diameter. The land is
11	Land Height (h/d)	specified as the shoulder that contains the loaded contact zone.
10	Dom Height (h/d)	Height of the dam diameter expressed as the ratio fo the radial height to the ball diameter. The dam is
12		specified as the shoulder the is unloaded, or opposite the contact angle.
13	RMS Roughness (Microinch)	Surface roughness, RMS, of the inner raceway.
14	Outer Diameter (in)	Bearing's outer diameter.
15	O.R. Width (in)	Width along the bearing axis of the outer ring.
16	Raceway Curvature	Inner ring curvature, expressed as the ratio of the raceway radius to the ball diameter.
17	Land Height (b/d)	Height of the land diameter expressed as the ratio of the radial height to the ball diameter. The land is
17		specified as the shoulder that contains the loaded contact zone.
18	Dam Height (h/d)	Height of the dam diameter expressed as the ratio fo the radial height to the ball diameter. The dam is
10		specified as the shoulder the is unloaded, or opposite the contact angle.
19	RMS Roughness (Microinch)	Surface roughness, RMS, or the outer raceway.
20		Opens the Material Database Editor.
21	Clear All Entries Button	Clears all current input field entries. This does NOT clear the database entries.
22	Add To Database Button	Commits the specified input entries into the database under the bearing name specified. A warning will
		This window provides all current bearing names within the database.
23	Database Entry	columns of data as eventually become a scrollable window to provide all database entries.
.		Once a database entry is selected within the database window, selecting this button will populate the
24	View/Edit Properties Button	bearing parameters into the input fields.
25	Delete Entry Button	With a database entry selected, this button will permanently delete the entry from the database.
26	Close Button	Closes the Bearing Database Editor.

Figure 9. Bearing Database Inputs



2.2.2 Material Database Editor

The material database editor allows the user to define their own unique materials. See the following figure for a detailed description of the material editor.

		Material Database Editor Material Properties Material Name: 444 1 pless Young's Modulus (ps): 2 Poisson's Ratio: 3 Poisson's Ratio: 3 Specific Density (lbm/in^3): 4 Coefficient of Thermal Expansion (n/in-F): 5 6 6 Clear Entries Add To Database 7 Material Database	
		9 View Parameters Delete From Database 10 Close 11	
#	Title	Description	
1	Material Name	Specify a name for the material.	
2	Young's Modulus (psi)	Specifies Young's Modulus for the material.	
3	Poisson's Ratio	Specifies Poisson's ratio for the material.	
4	Specific Density (lbm/in ³)	Specifies the specific density of the material.	
5	Coefficient of Thermal Expansion (in/in-°F)	Specifies the coefficient of thermal expansion for the material.	
6	Clear Entries Button	Clears all input entries (does NOT clear the database entries).	
7	Add To Database Button	Adds new entire to the Material Database.	
8	Material Database Window	Shows the current entries in the Material Database.	
9	View Parameters Button	Displays the parameters of a selected material database entry.	
10	Delete From Database Button	Deletes the selected database entry from the database.	
11	Close Button	Closes the Bearing Database Editor.	

Figure 10. Material Database Inputs

2.2.3 Lubricant Database Editor

The lubricant database editor allows the user to define their own unique lubricants. See the following figure for a detailed description of the lubricant editor.



		Lubricant Database Editor Lubricant Properties Lubricant Name: Samp 1 Icant Atmospheric Viscosity (Ibf-sec/In^2): 1 2 5 Pressure Coefficient of Viscosity (In^2/Ibf): 1 3 NOTE: Atmospheric viscosity and the pressure coefficient of viscosity values must pertain to the lubricant temperature 4 Clear Entries Add To Database 5 Lubricant Database Sample Lubricant Cose 9	
#	Title	Description	
1	Lubricant Name	Specify a name for the lubricant.	
2	Atmospheric Viscosity (lbf- sec/in ²)	Specifies the viscosity of the lubricant.	
3	Pressure Coefficient of Viscosity (in ² /lbf)	Specifies the pressure coefficient of viscosity of the lubricant.	
4	Clear Entries Button	Clears all input entries (does NOT clear the database entries).	
5	Add To Database Button	Adds new entry to the Lubricant Database.	
6	Lubricant Database Window	Shows the current entries in the Lubricant Database.	
7	View Parameters Button	Displays the parameters of a selected lubricant database entry.	
8	Delete From Database Button	Deletes the selected database entry from the database.	
9	Close Button	Closes the Lubricant Database Editor.	

Figure 11. Lubricant Database Inputs

2.3 Analysis Results Window

Professionally formatted analysis output is provided in a standalone window as shown in the following figure. Refer to section 4.0 for a detailed description of all available output. Results are organized to provide quick access and easy interpretation.

All results windows 'float', which enables the user to perform multiple analyses and compare them sideby-side.



	r	
		Analysis Results
		1 Result Summary
		Row 1 Row 2 Row 3 Row 4 Row 5
		Max Mean Stress (psi) 3.8539E05 3.8539E05
		Nounted Preload (bf) 2.0000E02 -2.0000E02
		Friction Torque (in-ozf) 8.4318E02 8.4318E02
		2 Detailed Results
		Bearing Torque
		Uescription KOW I KOW K KOW K KOW K KOW K KOW S Friction Torque (in-ozf): 8.4318E02 8.4318E02
		Row 1 Output
		Liement Normalisal Normalisal Contact Contact mean Hercz mean Hercz Iruncated Iruncated Number Load I.R. Load O.R. Angle I.R. Angle O.R. Stress, I.R. Stress, O.R. Length, I.R. Length, O.R.
		(#) (bf) (bf) (deq) (deq) (ps) (ps) (%) (%)
		1 6.6948E-16 6.8311E-16 2.2401E01 2.2401E01 3.0640E-01 2.9101E-01 0.0000E00 0.0000E00 2.2401E01 3.0640E-01 2.9101E-01 0.0000E00 0.0000E00
		3 6.6948E-16 6.8311E-16 2.2470E01 2.2470E01 3.0640E-01 2.9101E-0 0.0000E00 0.0000E00
		4 6.6948E-16 6.8312E-16 2.2553E01 2.2553E01 3.0640E-01 2.9101E-01 0.0000E00 0.0000E00 55 6.6948E-16 6.3312E-16 2.2665E01 3.0640E-01 2.9101E-01 0.0000E00 0.0000E00 55 6.6948E-16 2.2665E01 3.2664E-01 2.9101E-01 0.0000E00 0.0000E00 55 6.6948E-16 2.5655E01 3.2645E-16 2.9101E-01 0.0000E00 55 6.6948E-16 3.2565E01 3.2565E01 3.0646E-01 2.9101E-01 0.0000E00 55 55 55 55 55 55 55 55 55 55 55 55 5
		6 6.6948-16 6.8312-16 2.2732601 2.273261 3.0646-01 2.9101-01 0.000000 0.0000000
		7 6.6948E-16 6.8312E-16 2.2939E01 2.2939E01 3.0640E-01 2.9101E-01 0.00000E00 0.00000E00
		9 6.69495-16 6.83122-16 2.3504501 2.3504501 3.06465-01 2.91012-01 0.0000000 0.0000000
		10 1.3991E01 1.3992E01 2.3407E01 2.3405E01 8.4375E04 7.9602E04 0.0000E00 0.0000E00
		11 1.3111602 1.3111602 2.3559401 2.3559401 1.773605 1.676805 0.0000600 0.0000600
		13 5.0504E02 5.0505E02 2.3815E01 2.3815E01 2.7892E05 2.6314E05 0.0000E00 0.0000E00
		14 7.1394E02 7.1394E02 2.3923E01 2.3923E01 3.1303E05 2.9532E05 0.0000E00 0.0000E00 1.0000E00 1.0000E00 1.0000E00 1.0000E00 0.0000E00
		16 1.0855E03 1.0855E03 2.4084E01 2.4084E01 3.5995E05 3.3955E05 0.0000E00 0.0000E00
		17 1.2191E03 1.2191E03 2.4136E01 2.4136E01 8.7415E05 3.2598E05 0.00000E00 0.0000E00 18 1.3034E03 1.3034E03 2.41657E01 2.4165E01 8.2598E05 3.6094E05 0.0000EE00 0.0000EE00
		19 1.3323E03 1.3323E03 2.4177E01 2.4177E01 3.8539E0 3 1.6356E05 0.0000E00 0.0000E00
		20 1.3034E03 1.3034E03 2.4167E01 2.4167E01 8.4259E05 3.6094E05 0.00000E00 0.0000E00 21 1.2191E03 1.2191E03 2.4135E01 2.4135E01 8.7435E05 3.5094E05 0.00000E00
		22 1.0855E03 1.0855E03 2.4084E01 2.4084E01 3.5995E05 3.3958E05 0.00000E00 0.00000E00 ▼
		4 Adjust Fort Size
		-3 -2 -1 0 1 2 3 3 Princ 6 Jave 7 Cuse
#	Title	Description
	Dec III C	Key result parameters are tabulated for each bearing row. This area provides quick access to available key
1	Result Summary	parameters.
-		A scrollable/selectable text window containing the complete analysis output. See section 4.0 for a
2	Detailed Results	comprehensive listing of available output contained in the detailed results section of the results window
		Comprehension and a subject of a second and a second a se
2	Docult Highlighting	Result ingining indices important result parameters impossible to overlook. Each element nertzian
3	Result Highlighting	contact stress exceeding the user specified allowable is highlighted. Additionally, all elements with
		truncation are automatically highlighted.
4	Adjust Font Size	Font slider adjusts font size, in 1pt increments, for all the detailed results text.
5	Print Button	Brings up a standard print dialog. Only the detailed results are printed.
		Save copies the contents of the results window to a delimited text file. The delimited text file provides the
6	Save Button	user with unlimited post processing options and easy importing to various software platforms such as
		Microsoft Excel®.
7	Close Button	Closes the results window.

Figure 12. Results Window

2.4 Sensitivity Studies

ORBIS enables rapid bearing design and quick solutions to common 'what if' scenarios via the Sensitivity Studies utility. This utility allows the user to vary almost any input parameter (independent parameter) and plot them against any output parameter (dependent parameter). The Sensitivity Study dialog is accessed from the 'Tools' menu (see section 2.1.6).





Figure 13. Sensitivity Studies Dialog

2.4.1 Sensitivity Studies - Plot Windows

The plot windows generated from a sensitivity study are interactive. See the following figure for a description of user options within the plot windows.



Phone: (310) 650-8982 Email: info@HalpinEngineeringLLC.com Web: http://www.HalpinEngineeringLLC.com



Figure 14. Plot Windows

2.5 Tolerance Studies

Orbis performs tolerance studies of key bearing parameters with the Tolerance Studies dialog. This utility iteratively solves all permutations of user specified tolerances and provides the combination causing worst case Hertzian contact stress in a results window. Additionally, truncation is checked for all iterations. Reference the following figure for a description of the Tolerance Studies utility.



		Tolerance Analysis	
		Tolerances Min Max Free Contact Angle (deg): 19 125 Inner Raceway Curvature: .52 2 .52 3 .54 Outer Raceway Curvature: .52 3 .54 Preload (lbf): 280 4 Options 5 V Mary sign convention on load components 6 Apply tolerances to all bearing rows Select Bearing Row: 1 7 Notes 1. This utility evaluates all permutations of min/max tolerances and reports the routine will stop iterating and report the truncation is found the routine will stop iterating and report the truncated results. 2. WARNING: Due to the large number of possible permutations, this routine may take several minutes to complete (i.e. A two bearing row system with varied sign convention on load components and tolerances applied to all rows has 4,096 possible permutations). 8 Analyze Close 9	
#	Title	Description	
1	Free Contact Angle (deg)	Specify min and max free contact angles in degrees.	
2	Inner Raceway Curvature	Specify min and max inner raceway curvatures (ratio of raceway radius to ball diameter).	
3	Outer Raceway Curvature	Specify min and max outer raceway curvatures (ratio of raceway radius to ball diameter).	
4	Preload	Specify min and max preload (always as a positive value). Orbis will correct sign based on contact angle orientation and the assumption that the preload should load through the contact angle.	
5	Vary Sign Convention	Checkbox to specify if sign convention should be varied on all load components. Selecting this checkbox will run all permutations of positive and negative load components.	
6	Apply Tolerances to all rows	Checkbox to specify how tolerances are applied to the system. Selecting this checkbox causes all bearing rows to have specified tolerances analyzed. Un-selecting this checkbox activates item 7 below and tolerances are only applied to selected bearing row.	
7	Row Selection Drop-down	When active the drop-down menu is used to specify which bearing row to apply the specified tolerances to.	
8	Analyze Button	Button to begin analysis of tolerances.	
9	Close Button	Closes the Tolerance Analysis dialog window.	

Figure 15. Tolerance Studies Dialog

2.6 System Preferences

The system preferences dialog is available from the tools menu (reference section 2.1.6). Options available are shown in the figure below.



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Under Other Sector Description 1 Tabled Pane Selection Each system preference category is accessed by selecting the appropriate tab. 2 Database Location This are contrains the folder selection is only control to the default database. The select which the each are maintenance and the selection is on a database import or simply very contrast database. The selection is on a database import or simply very contents of a database (the each area and each				
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Image: Sected many bases the constraints of the sected and sected	Spec	ase cucation ify default location for databases:	2	System Luduing Parameters System Force Balance Error, lbf [0 < Value < 1]
Image: Notice intervention Description Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice intervention Image: Notice interventintervention Image: Notice interven	C:\D	Documents and Settings\Jake\My Documents\Orbis	Browse	Specifies the maximum allowable system force balance error. Convergence criteria will be determined by multiplying this value by the root sum squares (RSS) of the applied external loadies. If DSS of determal loads is for them can acteacted with a true different.
# Title Description 1 Tabbed Pane Selection Each system preference category is accessed by selecting the appropriate tab. 2 Database Location Each system preference category is accessed by selecting the appropriate tab. 3 Select Database Trype Each system preference category is accessed by selecting the appropriate tab. 4 Load Remote Database Top preform a database import, on simply vew contents of a database, the user subtrave selection is any appropriate tab. 5 Remote Database Select on the selection is achieved database. The database there is the selection selection is achieved by two scrollages (see 6 & 47) populate with the default database into a database. The database is preferred database. The database is database is preferred database. The datab	Datab	ase Importing		9 100 Max No. of System Solver Iterations [1 < Integer]
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Image: And weight of the second se	4856	6	ng	Specifies the maximum number of preload solver iterations before aborting.
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Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: Image: <thimage:< th=""> <thimage:< th=""> <thimage:<< th=""><th>812</th><th>mort mat Test58-22</th><th>Load Remote Database</th><th>13 Reset Defaults</th></thimage:<<></thimage:<></thimage:<>	812	mort mat Test58-22	Load Remote Database	13 Reset Defaults
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13 Reset Defaults Select this button to restore all solver options to their default values. 14 Close Button Closes the system preference dialog window.	12	Max Internal Clearance Error	Specifies the maximum allowab greater than zero [0 <value]. d<br="">bearing row's change in interna</value].>	le internal clearance error for convergence, in inches. Acceptable values are puring mounting and preloading routines the solver will converge on each I clearance within this value.
14 Close Button Closes the system preference dialog window.	13	Reset Defaults	Select this button to restore all	solver options to their default values.
	14	Close Button	Closes the system preference d	ialog window.

Figure 16. System Preferences

3.0 Technical Background

ORBIS uses numerical techniques to solve the user defined system of one or more bearing rows simultaneously. A solution to the system is achieved when the sum of all bearing row reaction forces is sufficiently close to the external applied forces (system equilibrium). ORBIS does not use pre-generated

lookup tables within the computations and all solutions are, unless otherwise specified, based on the mathematical theories developed and published by A.B. Jones (1964).

Some outputs provide results based on mounted contact angle. When a bearing is defined within the database editor the user specifies the free contact angle. ORBIS uses the free contact angle as the starting point for all subsequent computations. The first set of computations determines the mounted contact angle. Inputs such as I.R. and O.R. Fitup, Housing and Shaft Temperatures changes from ambient (68°F), and preloads influence the mounted contact angle.

3.1 Convergence Criteria

ORBIS uses the IEEE 754 technical standards for all floating point arithmetic. All calculations use at least 64-bit precision. Key calculations pertaining to matrix inversion and the overall system Jacobian are extended to 128-bit precision to improve accuracy of the solver. The default criteria for convergence are show below. Refer to section 2.6 for instructions on how to change these settings.

Parameter	Default Error (±)	Comments
System Equilibrium Error	0.001%	The allowable system equilibrium error is defined as a percentage of the applied external loading (Euclidean norm of force components). Error is defined as the difference between the norm of all bearing row reaction forces and the norm of the external applied forces. In the case where there is zero external loading the error defaults to 1.0E-5 lbf.
Preload Force Error	1.0E-5 lbf.	Preload force error is defined as the difference between the bearing reaction forces and the applied preload force.
Ring Expansion Error	1.0E-7 in.	The ring expansion error is defined as the difference between ΔP_D input into the Jones model (a 'fixed ring' model) and the resulting ΔP_D due to ring deflections. Ring deflections are determined by using the resulting ball normal forces and associated contact angle to determine an equivalent radial pressure on the bearing ring.

Table 1. Solver Convergence Criteria



4.0 **Output Descriptions**

The following sections describe the analysis output generated by ORBIS.

4.1 Input Parameters

This section provides a list of the user inputs used to generate the analysis results. These are provided to the user as reference.

4.2 External Applied Loads

This section displays the user defined system load components and the application point at which they are applied (location is along the x-axis).

4.3 Ball Crossing Angles

Ball Crossing Angles are displayed for each row and are defined as the angular rotation required by a given ring, inner or outer, to cause a ball to travel to an adjacent ball station. These results are based on the mounted bearing contact angle.

4.4 Internal Clearances

This section provides bearing diametral (or radial) and axial free-play. Results are given for both initial (free) and mounted conditions. Diametral play is defined as the total linear radial distance the inner ring can move relative to the outer ring with negligible applied force. Axial play is defined as the total axial displacement the inner ring can move relative to the outer ring.

4.5 Bearing Ring Properties

This section provides the equivalent raceway diameters used for the mounting/preloading algorithm. These diameters are defined as function of the bearing geometry as shown in the following figure. The bearing inner and outer diameter expansion from fitup and preloading, at both unmounted and mounted condition, is also included.

$$\mathcal{D}_{IR} = d_{IR_{race}} + 0.68(h_l + h_d) - \frac{2h_l}{d_{IR_{race}}}(h_l - h_d)$$
$$\mathcal{D}_{OR} = d_{OR_{race}} - 0.68(h_l + h_d) + \frac{2h_l}{d_{OR_{race}}}(h_l - h_d)$$





Figure 17. Bearing Nomenclature

4.6 Preload Data

This section provides the applied preload, resulting mounted preload and corresponding axial deflections for each bearing row. The axial deflection shown is purely due to the mounted preload condition.

4.7 Reaction Forces on Shaft

This section provides the resulting bearing reaction force components on the shaft at each bearing row. These forces include all mounting, preloading and external loading conditions and apply at the center of their respective bearing row locations.

4.8 Inner Ring Displacements

This section provides the components of the displaced inner rings due to mounting, preloading and external loading. All non-axial results are based on fixed outer ring theory developed by Jones (1964).

4.9 Stiffness Output

Orbis provides three different types of stiffness calculations: axial stiffness with ring compliance considerations, system Jacobian diagonal terms, and complete 5x5 stiffness derivatives for each bearing row. Refer to subsequent sections for a description of each type of stiffness result.

4.9.1 Axial Stiffness

This result provides the system axial stiffness, at mounted and preloaded state, with compliant ring considerations. Effects from external loading are not included in this result.



4.9.2 System Jacobian

This result provides the system Jacobian diagonal terms. These result apply in the fully loaded condition. Additionally, the system Jacobian assumes a rigid system during external load application. The system Jacobian results apply at the center point of the user's system (e.g. if the user system contained two rows placed at -0.5" and +0.5" along the x-axis the system Jacobian would be computed at x=0.0").

4.9.3 Row Stiffness Matrix

This section provides complete 5x5 stiffness derivatives for each bearing row. Stiffness results correspond to the quasi-static equilibrium state of the system in its final loaded state.

4.10 Fatigue Life

This section provides individual ring and total system fatigue cycles for various conditions. Note: Fatigue results are only generated for dynamic analysis runs. Outputs include L10 life, adjusted L10 life, and adjusted life with consideration for film thickness. L10 Fatigue life calculations are based on the Lundberg – Palmgren theories as shown in Jones (1964). The adjusted life output is based on the life factor theory adopted in AFBMA (1990) standards. This result includes the user defined life factor input along with a computed factor based on the user reliability input.

The life factor input allows the user to enter a combined factor to account for items such as materials, cleanliness, and misalignments. Bamberger (1971) provides a useful reference for computing various life factors. The adjusted life with film includes an additional lubricant factor, which is also provided for reference. The film parameter is from Bamberger (1971) and follows the AFMBA recommended average curve and uses the minimum film parameter as discussed below. All fatigue calculations use the individual rolling element results and do not require determination of an equivalent radial load on the bearing row.

4.11 Bearing Torque

Bearing torque results are only generated for dynamic analysis runs. The bearing torque output represents the torque associated with rolling and spinning within the contact area. Precisely, this is the torque due to interfacial slip (aka Heathcoate Slip) at the contact ellipse. It is important to note that there are numerous other factors, such as lubricant shear/churning or cage drag, which can have a profound effect on bearing torque. ORBIS uses the 'Race Control' theory from Jones (1964) and therefore only allows spin to occur on one raceway. The computed torque output can be scaled with the coefficient of friction input parameter. Reference Jones (1964) for the torque calculations used by ORBIS.

4.12 Row Outputs (Element-Wise results)

Detailed outputs for each element of each row are provided in tabular form. Output tables are repeated for each bearing row in the user's system. These tables differ depending on whether the analysis is static or dynamic. All outputs correspond to the system equilibrium state after application of all external loading.

4.12.1 Element Number

The Element Number is simply an indexing scheme to identify each of the rolling-elements uniquely.



4.12.2 Normal Ball Load

The Normal Ball Load is the load applied by each ball into each raceway contact. This load is directly normal to the contact ellipse.

4.12.3 Contact Angle

The Contact Angle output describes the angle of the normal ball load vector.

4.12.4 Mean Hertz Stress

The Mean Hertz Stress output represents the average Hertzian contact stress over the elliptical contact area. Peak stress for an elliptical contact can be computed by multiplying the mean stress by 3/2. ORBIS will automatically highlight, in red, all values that exceed the user defined allowable mean Hertzian stress from the main user interface. All stress results assume the contact ellipse if fully contained within the raceway.

4.12.5 Truncated Length

The Truncated Length represents the percent of the total length of the contact ellipse, along the major axis, that is truncated due to shoulder or dam override. ORBIS will automatically highlight all elements that have any truncation.

4.12.6 Ellipse Semi Major

The Ellipse Semi Major output represents one half of the major dimension of the contact ellipse.

4.12.7 Ellipse Semi Minor

The Ellipse Semi Minor output represents one half of the minor dimension of the contact ellipse.

4.12.8 Max Sub-Surf Shear

The Max Sub-Surface Shear is the peak shear stress developed below the raceway surface due to contact stress.

4.12.9 Max Shear Depth

The Max Shear Depth is the location along the normal to the contact area, below the raceway surface, at which maximum shear stress is developed.

4.12.10 Upper Edge Location

The Upper Edge Location represents the edge of the contact ellipse that is closest to the land diameter. This value is represented as a ratio of its height from the center of the raceway to the ball diameter.

4.12.11 Lower Edge Location

The Lower Edge Location represents the edge of the contact ellipse that is closest to the dam diameter. This value is represented as a ratio of its height from the center of the raceway to the ball diameter.



4.12.12 Contact Normal Approach

Contact Normal Approach represents the total combined deflection of the contacting bodies (rollingelement and raceway). This deflection is along the normal direction to the contact area.

4.12.13 Contact Normal Stiffness

Contact Normal Stiffness represents the stiffness of the rolling-element to raceway contact area stiffness in the normal direction.

4.12.14 Spinning Velocity

Spinning Velocity is the angular velocity of rolling-element spin relative to the un-controlling raceway. Per Jones' (1964) race control theory, spin can only occur on one raceway while pure rolling occurs on the other. Based on the spinning velocity output one can deduce race control (i.e. if there is zero spinning velocity on a given raceway than that raceway is 'in control').

4.12.15 Rolling Velocity

Rolling Velocity is the absolute angular velocity of the rolling element relative to the raceways.

4.12.16 Spinning Torque

Spinning Torque is the component of torque generated by interfacial slip within the contact area due to rolling-element spin.

4.12.17 Rolling Torque

Rolling Torque is the component of torque generated by interfacial slip within the contact area due to pure rolling.

4.12.18 Element Roll Velocity

The Element Roll Velocity represents the rotational velocity of the rolling elements as seen relative to the pitch orbit velocity.

4.12.19 Pitch Orbit Velocity

The Pitch Orbit Velocity is the rotational velocity of the bearing pitch diameter about its spin axis. This is essentially the angular velocity of rolling-element cage or retainer.

4.12.20 Minimum Film Height

The Minimum Film Height represents the thinnest point of the lubricant within the contact ellipse. This calculation is based on the 'Hard-EHL' theory by Hamrock and Dowson (1981) for fully flooded conditions.

4.12.21 Minimum Lambda Value

Lambda is a dimensionless parameter that is often used to describe the lubricant regime of the bearing. Its value is determined by taking the ratio of the minimum film height to the root sum squares (RSS) of the contacting surface roughness. Mathematically, lambda is defined as follows.

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$$\lambda = \frac{h_{min}}{\sqrt{R_{raceway}}^2 + R_{ball}^2}$$

4.12.22 Centrifugal Force

The Centrifugal Force output represents the radial body force of the rolling element due to its orbital velocity and mass. This force tends to create differing contact angles between the inner and outer race contacts and is treated in the analysis per Jones (1964).

4.12.23 Gyroscopic Moment

The Gyroscopic Moment output represents the spinning body moment of the rolling element due to its angular velocity and inertia. The influences of this force are treated in the analysis per Jones (1964).

5.0 References

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