# Integrating Logical Functions with ILF

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#### Abstract

This is a description of the system ILF developed at the Humboldt-University at Berlin<sup>1</sup>. ILF is a system that integrates automated theorem provers, proof tactics for interactive deductive systems and models within a graphical user interface. The structure and commands of ILF are presented<sup>2</sup>.

A special part is devoted to the TreeViewer – a part of ILF used for visualising directed acyclic graphs, which can be used as a separate programme.

We describe the possibilities to extend ILF by integrating more interactive and automated deductive systems.

The last part describes the ProofPad – a sample configuration for editing proofs in the field of lattice ordered groups.

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## What is ILF?

Research in the field of theorem proving in many groups in several countries has created a lot of sophisticated tools e.g.

- automated theorem provers for various logical calculi,
- rewrite systems,
- proof tactics,
- model finders and
- domain specific methods.

ILF is a tool that can be configured in many ways to Integrate all these Logical Functions. The common feature of these tools that is used for this integration is that they all can be used to modify a knowledge base.

*ILF* is applied on two different levels. For the knowledge engineer it yields methods of testing the power of tools to support logically correct arguments in a specific field. Several ways to combine these tools in proof tactics can be tested rapidly. When a collection of useful proof tactics has been obtained, it can be encapsulated as a set of "rules of inference" in a new interactive or automated deductive system. It is also possible to extend an existing system in this way. This new, more powerful system can be tailored to meet exactly the needs of an end user, making available just those procedures that his kind of problems demand.

The user of ILF is not restricted to a particular logic. He can use any of the systems that have been integrated at any time. He might start proving a theorem within one calculus. On the way he can decide to prove a specific formula by a specialized system. E.g. he may apply a rewrite system in order to prove an equation and apply this equation to construct a natural deduction proof.

The user can take advantage of the programming language PROLOG to write proof tactics for interactive deductive systems. These tactics can change the state of a proof by applying rules of inference in an automated way. PROLOG is augmented by special constructs – socalled tacticals, loop constructs and global variables – in

order to help the user writing his own control programme for a theorem prover. His proof tactics can ask advanced automated theorem provers running in the background for support. Different alternatives for a proof can be tried automatically using the backtracking capabilities of PROLOG. All the debugging tools of PRO-LOG like tracing and spy points are available to develop and test proof tactics.

Perhaps the most challenging feature of ILF is its modularity. The power of ILF can be easily extended by integrating further systems and developing libraries of domain specific proof tactics. In fact, for an experienced PROLOG programmer, it is a matter of a few days to integrate a new system that has been developed somewhere else independently.

The continuously growing power of ILF requires a simple tool for control. This is provided by a graphical user interface. The functionality of this interface can be changed and modified by the user at run time; allowing also automatic modification by the user's proof tactics.

A common problem is to prevent the user from getting lost in complex hierarchies of objects, e.g. in a proof, a complex term or a hierarchy of theories. Therefore, *ILF* contains a *TreeViewer* that can be used to visualize these hierarchies as marked directed acylic graphs. Though this *TreeViewer* was developed as a part of *ILF*, it is in fact a separate programme with a simple interface to be used in combination with other programmes.

The development of ILF at the Humboldt-University started around 1987 as an interactive theorem prover with a language for proof tactics. In 1989 experiments with the combination of several deductive systems began. In 1991 OTTER from Argonne National Laboratories became the first automated theorem prover to be integrated into ILF. 1990-1992 the development of ILF was supported by the Volkswagen-Stiftung within a joint project "Leistungsfähigkeit von Beweisstrategien" with the group of H. Kleine Büning from Duisburg University. IBM Germany made ILFA available – a toolkit for developing deductive systems in C. Using this system, interactive provers for the modified problem reduction and for the tableau calculus were built for *ILF*. Since 1992 a project "Deduktion und verbandsgeordnete Gruppen" supported by the Deutsche Forschungsgemeinschaft has provided the framework and goals for the development of the system. This project is part of the DFG-Schwerpunkt "Deduktion". Cooperation within the Schwerpunkt made the provers DISCOUNT (University of Kaiserslautern) and SETHEO (Technical University Munich) available to *ILF*. We are greatly indebted to the authors of these systems for their assistance in integrating these provers into *ILF*.

Also the development of the *TreeViewer* has been stimulated very much by discussions at workshops on proof tactics within the Schwerpunkt.

Subsequently, the structure and the commands of ILF, as they were implemented in February 1994, are described.

A sample configuration – the ProofPad – is explained. This "deductive system" is set up to assist a user without special knowledge in automated theorem proving in editing elementary proofs in the field of lattice ordered groups, making the best possible use of the power of automated theorem provers. For the sake of extending the power of ILF, the interfaces needed for integrating other deductive systems are discussed.

We do not presume that the reader has experience with ILF, but some knowledge on PROLOG, on the deductive systems and on the logical calculi used by ILF will be helpful. The corresponding references are either generally available or can be easily obtained. Therefore, we shall only sketch these aspects.

### **Installation and Configuration**

*ILF* is available from the *ILF* group as a compressed tar-file **ilf**.tar.Z. By uncompressing and x-taring **ilf**.tar.Z, the directory ilf and further subdirectories (e.g. the **bin**, man and tmp directories) will be created.

*ILF* is based on *PROLOG-2* from Expert Systems Ltd, so *PROLOG-2* must be available. It is recommended to install also the automated provers *SETHEO* [LSBB92] and *DISCOUNT* [DP92] and use them as described in Section 8.2.2 and 8.2.1.

By convention all executables in *ILF* except for *ilf* have the extension .exe in order to prevent PROLOG-2 from automatically adding the extension .pro.

The following environment variables must be set:

#### environment variables

ILFHOME	the home directory of <i>ILF</i> , usually the directory built by x-taring the ilf.tar file
USERILFHOME	the personal $ILF$ directory owned by the user, in which $ILF$ will store temporary files and configurations and modifications for a particular user
PROLOGHOME	the home directory of PROLOG-2
TVIEWHOME	the home directory of the treeviewer

The executable files are in **\$ILFHOME/bin** and the manpages are in **\$ILFHOME/man**. **\$ILFHOME/bin** and **\$ILFHOME/man** should be included in the user's PATH and MANPATH variable, respectively.

The entries of the manpages normally start with *ilf\_* and are located in the *l*-section of the manpages. The complete list of *ILF*-manpages can be found in the *ilf\_man* manpages.

Since temporary files will be created during an ILF session, a user should have a personal ILF-directory USERILFHOME different from the ILF directory ILFHOME in order to avoid conflicts with filenames. The current version requires a special

structure of the **\$USERILFHOME** directory, which can be created by running **ilf** with the **-ini** option.

ILF is envoked by ilf [option [option ...]], where the currently available options are the following:

#### ILF command line options

-h	show the possible options
-hosts	create a new list of actual hosts
-ilfhome IH	take IH as ILFHOME
-ilfrc IRC	take IRC as .ilfrc file
-ini	create the USERILFHOME directory using the envi- ronment variable \$USERILFHOME and all necessary subdirectories
-prologhome PH	take PH as PROLOGHOME
-t	test the environment, don't start $ILF$
-userilfhome UIH	$take \ \texttt{UIH} \ as \ \texttt{USERILFHOME}$
-x	run $ILF$ in an X-Window system
+x	do not run $ILF$ in an X-Window system
-xilf	take the executable <code>XILF</code> instead of <code>Xilf</code> , the default executable

For the actual list of options see the ilf\_ilf manpages or the README file. Further options (e.g. X-toolkit options) will be passed to Xilf.

*ILF* will first read the file .ilfrc in \$USERILFHOME. If this file does not exist, *ILF* will take the generic .ilfrc in \$ILFHOME.

The entries of the .ilfrc file are divided into groups, each group GROUP is enclosed in the keywords GROUP and END\_GROUP. There are at least the groups ILFSTATE, EXPERT, DEDSYS and SIGNATURE with the following syntax:

```
ILF_STATE
key1 value1
key2 value2
. . .
keyn valuen
END_ILF_STATE
EXPERT
expert1 [file1]
expert2 [file2]
. . .
expertn [filen]
END_EXPERT
```

```
DED_SYS
ded_sys<sub>1</sub> [file<sub>1</sub>]
ded_sys<sub>2</sub> [file<sub>2</sub>]
     .
ded_sys_n [file<sub>n</sub>]
END_DED_SYS
SIGNATURE
op<sub>1</sub> ass<sub>1</sub> prec<sub>1</sub>
op_2 ass_2 prec_2
op_n ass_n prec_n
END_SIGNATURE
TEX_OP
op<sub>1</sub> ass<sub>1</sub> prec<sub>1</sub> texstring<sub>1</sub>
op_2 ass_2 prec_2 texstring_2
op_n ass_n prec_n texstring_n
END_TEX_OP
```

The entries of the groups will be stored as PROLOG predicates:

- the ILF\_STATE entries as ilf\_state(key<sub>i</sub>,value<sub>i</sub>).
- the EXPERT entries as expert\_file(expert<sub>i</sub>,file<sub>i</sub>).
- the DED\_SYS entries as dedsys\_file(dedsys, file\_i).
- the TEX\_OP entries as tex\_op(op<sub>i</sub>, ass<sub>i</sub>, prec<sub>i</sub>, texstring<sub>i</sub>).

If no file is given, **none** is taken as the file. These files are consulted when the corresponding experts and deduction systems, respectively, are called. The entries in the TEX\_OP group define the  $LAT_FX$  representation of these operators.

KILL prog<sub>1</sub> prog<sub>2</sub> . . . prog<sub>n</sub> END\_KILL

forces ILF to kill all processes, where grep finds the pattern  $prog_1, \ldots, prog_n$  in the output lines of ps -auxww after it has finished.

For distributed computation, the list of possibly available hosts is to be held in the file .ilfhosts in the USERILFHOME or in the ILFHOME directory. It is assumed that

the ILFHOME and USERILFHOME directories are mounted at these hosts and that the user can login without password checking (i.e. the hosts should be in the users .rhosts file). *ILF* checks which of these hosts are alive and stores the names of these hosts for further use in the file USERILFHOME/tmp/ilfhosts.pro. As long as this file exists, *ILF* assumes it to be up to date, so further invocation of *ILF* will skip the check. In order to update the list of actually available hosts, the user should simply remove the file USERILFHOME/tmp/ilfhosts.pro or just start *ILF* with the -hosts option. It is not recommended to change any file in USERILFHOME/tmp during an *ILF*-session.

*ILF* will start two processes running PROLOG-2, one in the foreground to react to the user's command and one in the background to control the work of automated systems running as separate processes. Depending on the automated systems used, more processes may be created. All files automatically created by *ILF* at runtime are located in the directory **\$USERILFHOME/tmp**. Files specific for a particular deductive system SYSTEM are kept in **\$USERILFHOME/tmp**. Files systems. Theories and tactics are contained in **\$USERILFHOME/th** and **\$USERILFHOME/th**. Theories and tactics are the and the systems. The systems are the extensions the and tact, respectively.

The behaviour of *ILF* depends very much on the setting of *ilf\_states*, which are explained at appropriate positions in this paper. Any *ilf\_state* used during a session must be initialized in the file .ilfrc described above. Then it can be retrieved by the command ilf\_state(key,Value) and set by the command ilf\_state(key,OldValue,NewValue).

The declaration of operators in the SIGNATURE section of the .ilfrc file follows the conventions of PROLOG-2. Note that changing these settings may change the way *ILF* parses theories and tactics! When states of background systems that have been saved before using the appropriate commands are reloaded, *ILF* checks whether the relevant operator declarations have been changed and displays a warning message if a change has been detected.

### The User Interface

Unlike other deductive systems ILF is normally used with a graphical user interface. The main reason for this is that the integration of many systems confronts the user with a lot of different commands that can be applied. The graphical user interface is an efficient help for the user in order to find out which commands are available in a specific situation. Since these commands – when selected from a menu – are printed in the command line, the graphical user interface can assist in learning the commands necessary to write a proof tactic. Nevertheless, there is also a command line interface available. Both interfaces are described below.

### **3.1** The Command Line Interface

The command line interface of ILF is essentially the top level interpreter of the underlying PROLOG system. Thus any PROLOG-2 command can be run from the command line interface.

The graphical user interface is just a shell on top of the command line interface; any command given to the graphical user interface will be delivered to the command line interface. However, it is also possible to work only with the command line interface. In order to do this, the *ilf\_state*  $\mathbf{x}$  must be set to off – either by including an appropriate statement in the .ilfrc file or by starting *ILF* with the command line option  $+\mathbf{x}$ .

Another *ilf\_state* the user may want to set is exptty. If this *ilf\_state* is set to file, the whole output from the background expert communicator is then sent to file. The default value for exptty is /dev/tty, i. e. the terminal the user is working on. Since the background experts work asynchronously, the default behaviour may be confusing when working with the command line interface. The *Tree Viewer* described in Section 4 is an X11-based application that is not available from the command line interface.

There are very few facilities that are only available at the command line interface due to the way Motif handles the user input. First of all, there is no way to interrupt a running prolog programme from the graphical user interface. From the command line interface this can be done by typing the terminal's INTR character (normally CTRL-C). From the command line interface the EOF character (CTRL-D if not specified otherwise) can be used to signal the end of a file (or a break for that matter). When using the graphical user interface end\_of\_file has to be typed or the corresponding menu item must be chosen. When tracing through a programme, going to the next step on the command line interface is performed by typing RETURN, where the graphical user interface requires SPACE and RETURN.

Subsequently we describe the most important command line interface commands, which are not specific for particular deductive systems. They are given in the full predicate notation predicate/arity.

load/1 loads theories from the th-subdirectory of \$USERILFHOME and tactics from the tac-subdirectory.Whether to load a theory or a tactic is decided by the extension (.th vs. .tac) of the given filename.

load\_th/1 and load\_tac/1 load a theory or a tactic located elsewhere if called with
an absolute path as argument.

load\_th/0 and load\_tac/0 display a list of all theories/tactics available in the user's
th/tac-subdirectories and prompt the user with Choice: to enter a number.

After loading a theory, load\_th/0 and load\_th/1 allow the user to enter additional axioms. A number prompts for the axiom in a form described in Section 5, Name prompts for the name of the axiom. An end. typed to the number prompt stops the input.

forget\_th/0 clears the knowledge base. axioms/0 displays all axioms.

The commands

#### Head to Body by Tactic

#### Name reduces Head to Body by Tactic

are central to *ILF*. Tactic is executed to prove that Body implies Head. The call succeeds if Tactic succeeds and proves an instantiation of  $Body \rightarrow Head$ . In general Head and Body may contain variables for subformulas that are instantiated during the proof if this is supported by the particular deductive system.

**reduces** asserts the proved instantiation under the name **Name** into the knowledge base.

The most simple case of a tactic is to call a deductive system by its name as a 0-ary predicate. This means that the user will interactively construct a proof by means of the specified deductive system.

Sometimes the lack of the occur check in PROLOG can cause problems when unifying formulas or names of axioms. These problems can often be overcome by using the command occur/0, which switches the occur check for some operations on or off. The actual status of this flag is contained in the *ilf\_state* occur.

The halt/0–command leaves the PROLOG system and therefore the command line interface of ILF, too.

### 3.2 The GUI Windows, Menus and Commands

The *ILF* System can be used within a graphical interface that is based on the X11R5 and OSF/Motif 1.2 libraries. Using the graphical user interface, the system consists of the following windows. Some of these windows can be omitted by setting appropriate *ilf\_states* described below. Notably, the graphical user interface can be switched off by setting the *ilf\_state* x to off.

- The **main window** controlling the PROLOG-2 system running in the foreground. It has pulldown menus, an area for the *stdout* stream of PROLOG and a line for editing.
- The ExpertManager window, which displays messages from the PROLOG system running in the background and from the automated systems called by that PROLOG. The window is an ordinary xterm. The ExpertManager and its window can be closed by typing ex\_stop. in the main window. The manager can be restarted (a new PROLOG process will be created) by ex\_start.
- The expert log window, which is used to display some information for debugging. This window is only displayed if the *ilf\_state* debug is set to on in the .ilfrc file. While *ILF* is running, this *ilf\_state* switches the displaying of messages for debugging on or off. If the window is not present, and the state is set on, the debug messages are written into the file exlog.l in the tmp directory.
- The two windows of the TreeViewer that are described in Section 4.

In the graphical user interface, too, all commands can be given to the system by typing them on the command line of the main window, but it is easier to use the menus. There is a standard set of commands given in the menu bar and the pull down menus there. Which menu items are displayed depends on the *ilf\_state* menu\_level. The level 0 will give only the basic menu items, and a higher level will give more menu points. At present 4 is the maximum menu level in use. Menus with a variable number of items contain an item refresh, which can be used to adapt the menu to a new menu level. It is also possible to introduce new menus (see Section 9).

If a command is selected from a pulldown menu, its command line form is shown in the main window. Some commands must be completed by the user by inserting certain parameters. In these cases the displayed format of the commands indicates the types of the parameters required.

After the ILF system has been started, it usually has four menus: the COMMAND menu, the THEORY menu, the DED-SYS menu, and the expert menu. The COMMAND menu has some items that can be used in several systems to edit a proof. These commands are explained in Section 6. Moreover, there are the following general commands.

#### COMMAND menu

occur-check	$n^1$	switches the occur-check for some unifications in the
		foreground PROLOG on or off
load tactic	с	opens a file select box of the user's tactics
halt	n	leaves the $ILF$ system and kills all subprogrammes

The THEORY menu permits access to commands to inspect and manipulate the hierarchy of theories in use. These commands are discussed in Section 5.

The interactive deductive systems, which will be decribed in Section 8.1, can be called from the menu DED-SYS.

<sup>&</sup>lt;sup>1</sup>n: noconfirm, c: confirm, s: submenu

## The TreeViewer

The *TreeViewer* is a graphical and alphanumerical interface for the visualisation of directed acyclic graphs. It is a separate programme that can be integrated into other programmes. The *TreeViewer* can be obtained via ftp from info.mathematik.hu-berlin.de (141.20.54.8, not yet connected to a name service) in the compressed tar-file /ftp/ilf/tview.tar.Z.

It is based on the OSF/Motif library and should therefore work on any X-Windowsystem on SUN SPARCStation and compatibles. In *ILF* the *TreeViewer* is used if the *ilf\_state* treeviewer is set to on in the file .ilfrc.

The graphs to be displayed are given by handles for the nodes, especially a designated root handle, and edges. Each handle for a node can be optionally associated with a shape and an info displayed within the graph and a contents string, which can be displayed in a separate window.

Having been invoked by the user, the *TreeViewer* offers two windows: one for the graphic display of the graph and one for alphanumeric output and editing.

In the graphic window, by default graphs are displayed unfolded as trees showing nodes occurring more than once in several places. Such nodes are marked by a bold line in the drawn rectangle. The user can gather these nodes by commands chosen from the pulldown menus of the graphic window. Of course, they can also be separated again by an appropriate command. According to the shape associated with a handle, the node is displayed as one of 10 bitmaps. These bitmaps are contained in the file tvshapes, which can be edited by the user with a bitmap editor, e.g. bitmap.

It is possible to hide parts of the graph and to redraw hidden parts.

There are several possibilities to display alphanumerical information about the nodes. First of all, there is an info shown on the right-hand side of the nodal rectangle. It is set automatically, but can be modified by the user (see commands). A further way is to click on a node in the graphic window using the left mouse button. This method will show the handle of the node in the bottom line of the graphic window.

In the alphanumeric window, textual information is displayed in the form info-string: spaces handle or contents if set, respectively. The number of spaces depends on the depth of the node in the graph, thus indicating the structure of the graph in the alphanumeric window, too. The information about a node is transferred to the list in this window by clicking on the node in the graphic window with the middle mouse button. Clicking again will remove the information from the list. If information on the node is displayed in the alphanumeric window, the rectangle visualising this node has a shadow.

Another way to get a line into the above mentioned list is to use the tv\_text command (see commands). In this case the string "user" is shown instead of the info-string and the number of spaces is constant. Handle or contents, respectively, can be edited for further use in the bottom line of the alphanumeric window. They are displayed in the bottom line after selection with the left mouse button.

The communication of the *TreeViewer* with the programme having invoked it is realized by the use of two named pipes, one for the input, one for the output. These pipes can be created by the client programme before invoking the *TreeViewer* or initiated by the *TreeViewer* if it is called with the c option. In this case they are removed automatically when the *TreeViewer* is closed.

The *TreeViewer* is called by

tview [-1] [-c] inputpipename outputpipename ...

The option -1 makes the programme write a logfile into the working directory, which contains all commands received through the inputpipe and errors generated by these commands if occurring.

The option -c causes the programme to generate communication pipes and remove them when being closed. Inputpipename and outputpipename are the names of the pipes for communication with the client programme. At the end of the option list further options as generally known from graphical interfaces like -geometry or -iconic can be added.

The client programme communicates with the *TreeViewer* using the following *commands*. All these commands are given to the *TreeViewer* through the inputpipe.

#### TreeViewer commands for building the graph

root(Root)	creates a new root-node with the handle Root re- moving an existing graph if nesseccary
new_edge(Father,Son)	creates a new edge in an existing graph if Father is known, the edge doesnt yet exist and Son is not already located on the direct way from Father to Root (i. e. the graph must be acyclic)
<pre>del_edge(Father,Son)</pre>	deletes an edge of the graph if it exists and Son is a leaf (i. e. has no sons)
<pre>set_shape(Handle,Shape)</pre>	sets a shape for the node Handle, the number of which must be in the range from 0 to 9
<pre>set_info(Handle,Info)</pre>	sets the info for the node Handle

Handle, Contents and Info are treated as strings, in case they contain a comma (which is used as separator between the arguments of commands) they must be enclosed in double quotes. Quotes are taken as a part of the string if they are preceeded by a backslash.

The *communication* of the *TreeViewer* with the client programme can be performed by the following commands. All messages from the *TreeViewer* are finished with a full-stop.

#### TreeViewer commands for communication

ok(message)	will cause the treeviewer to respond with <b>message</b> . using the outputpipe
quit	closes the $TreeViewer$
get_handle	has the <i>TreeViewer</i> write the next node handle and contents, respectively, selected by the user to the outputpipe. The node has to be selected in the graphic window with the right mouse button. This is signalled to the user by the form of the mouse- cursor appearing as a hand.
get_text	initiates an answer containing facts in the form of a list of PROLOG terms – each item being on a separate line – surrounded by the keywords tv_list. and end The user may select a string in the editable line of the alphanumeric window end has to press the Return key. Then the follow- ing information is passed to the client programme: handle of the node corresponding to the selected line in the text, position of the first character of the selected substring (the first symbol has the po- sition 0), length of the selected substring and the string in the editable line surrounded by quotes and followed by a full-stop. If there is not any part of the string selected, the value of position is set to -1 and the length to 0.
get_info	works as if both get_handle and get_text have been called, but only one answer is allowed. The user decides how to give the answer.
tv_text(message)	generates a line containing "user: message" in the alphanumeric window
update	refreshes the contents of both the graphic and the alphanumeric window after having changed things by commands using the inputpipe

/* */	is a comment to be ignored
call	allows the client programme to call functions usu-
	ally invoked from the menus by using the inputpipe

### TreeViewer menu in the graphics window

Hide	to remove nodes from the drawing, sons possible being displayed as sons of the father node
Above	hides all nodes above the selected one (excepting the root-node)
This	hides the selected node (root-node cannot be hid- den)
Below	hides all nodes below the selected one
Below but Leafs	hides all nodes below the selected one except for the leaves (the nodes without sons)
Draw	displays nodes that have been hidden
Above	displays hidden nodes above the selected one
Below	displays hidden nodes below the selected one
Gather	displays nodes occurring several times in the un- folded graph only once
This	contracts only the selected node
All	contracts the selected node and all nodes having more than one instance below it
Separate	unfolds the graph after having used gather
This	displays the selected node as often as it occurs as a son
All	displays the selected node and all nodes below it as often as they occur as sons
List	transfers textual information to the alphanumeric window
This	transfers information on the selected node (like us- ing the middle mouse button)
All	transfers information on the selected node and all nodes below it

### TreeViewer menu in the alphanumeric window

Discard	Using this menu abandons the list in the alphanu-
	meric window.
Action	erases the list
Abandon	cancels the action and leaves the list intact

Instead of using the menu buttons, the client programme can send the command call(ButtonFunction,Handle)

through the inputpipe. The first argument ButtonFunction is a concatenation of the labels of the buttons that would have to be clicked with the mouse if they were used instead (e.g. the ButtonFunction for Hide-Above is HideAbove). The use of capitals is irrelevant so that e.g. hideAbove may also be used instead of HideAbove. The second argument Handle is the handle string. The argument must exist, if no handle is needed, it is not used. The difference of effects achieved by using the mouse and the buttons and the command call, respectively, is caused by the impossibility of distinguishing between several instances of one node without the mousepointer. That's why the command Hide-This for example can hide one instance of a node only if the mouse is used, in case the command call is used, all instances of the node are hidden. On the other hand, this difference allows to realize the function Draw This for the command call, which would be impossible to use with the mouse.

In order to run the *Tree Viewer* the environment should be set up as follows.

For the graphic display the bitmap-file tvshapes must be available. This file is looked for in the actual directory and then in the directory given by the environmental variable TVIEWHOME.

For trouble-shooting the 1 option should be used. This causes the generation of the file tview.log containing all commands sent through the inputpipe. Commands not accepted are followed by a comment giving the reason of the missing acception. The file can be used as input by sending it through the inputpipe after deleting the last line containing the command quit.

### Theories

This section describes the syntax of theory files for *ILF*. A theory file may contain named axioms, a title, comments and PROLOG commands. It must contain an end line containing end. as the only item.

An axiom is given on two lines. The first of these lines contains a term of the form H:-B., H. or :-B.. H and B are valid PROLOG terms, possibly with variables. The intended meaning of this axioms is the universal closure of  $B \rightarrow H$ , of H and of  $\neg B$ , respectively. Like in PROLOG, conjunction and disjunction ar denoted by a comma and a semicolon, respectively. Variants of conjunction and disjunction, which can take any list of propositions as arguments, are denoted by & and #. Negation is denoted by not. Universal and existential quantifier are written as ex and all. They can bind either a single variable or a list of variables. As in PROLOG variables start either with a capital letter or with an underscore character. It is possible to use operators in prefix, postfix or infix notation if they have been declared in the file .ilfrc.

Of course, it depends on the properties of the concrete deductive systems which axioms can be used in a proof.

Each axiom is followed by a line containing the name of the axiom which can be an arbitrary prolog term. Clever naming conventions can simplify writing tactics in *ILF* considerably, so names should be chosen with care. E. g. all laws of commutativity can be denoted by names of the form comm(Op) where Op is the operator which is commutative. Similarly dis(\*,+,1) and dis(\*,+,2) can be names for the equations saying that \* distributes over + from left or right, respectively.

The (optional) title of a theory is given on a single line as

th\_title : title\_string.

title\_string must be enclosed in double quotes. It is recommended to chose title\_string in such a way that "Theory of title\_string" is meaningful.

Comments are given as in C-programmes. A line containing a PROLOG command starts with ?-. An end line is a line consisting only of end. and must be in any theory file.

After this informal description we give a Backus-Naur-notation for this syntax. Terminal symbols are prolog\_term, which stands for a valid PROLOG term, string, which stands for any string of characters, comment\_string, which stands for any string of characters not including \*/, <lf>, which stands for a line feed and :- ?- : . /\* \*/ " th\_title end, which stand for themselves.

ilf_theory	::=	$\{\text{theory part}\}^*$ end_line
$theory\_part$	::=	empty_part    axiom_part    title_line    comment
empty_part	::=	{ <lf>}*</lf>
axiom_part	::=	axiom. <lf>prolog_term.<lf></lf></lf>
axiom	::=	prolog_term :- prolog_term    prolog_term
		:- prolog_term
title_line	::=	th_title : "string". <lf></lf>
comment	::=	/* comment_string */
end_line	::=	end. <lf></lf>

As mentioned above, theories can contain arbitrary PROLOG commands. The command load("Name.th"). which loads a theory Name from the user's directory of theories is of special significance for theories. This theory is considered as a subtheory of the given theory. In this way, a simple hierarchy of theories is built up. Though a theory can be a subtheory of several other theories it will be loaded only once into memory. If there is a theory named standard.th in the directory \${USERILFHOME}/th, it will be loaded at startup.

Within *ILF*, theory/1 and subtheory/2 can be used to inspect the hierarchy of theories. in\_theory(Formula,Theory) tests whether a formula has been loaded with a particular theory. The following commands, which can be also accessed using the THEORY menu of the graphic user interface, can also manipulate theories.

#### THEORY menu

<pre>make_theory(Theory)</pre>	creates a new theory
<pre>make_subtheory(Th,SubTh)</pre>	determines that SubTh is considered to be con- tained in Th
<pre>make_title(Th,String)</pre>	lets String be the title of Th
<pre>add_ax(Theory,AxList)</pre>	adds the axiom or the list of axioms AxList to the theory Theory
rm_ax(Theory,AxList)	removes the axioms from AxList from Theory but leaves them in the knowledge base
rm_theory(Theory)	removes Theory leaving its axioms still in the knowledge base
add_th	gives the user the possibility to add new axioms from the command line without inserting them into a particular theory
activate(Name)	activates axioms whose name matches Name. De- activated names will not be used by deductive sys- tems. When an axiom is deactivated, its name is changed from Name to \$(Name)
deactivate(Name)	deactivates axioms whose name matches $\verb+Name$

forget_ax(Name)	removes all axioms having a name matching Name from the knowledge base
forget_th	eliminates all axioms and theories from memory
<pre>save_th(Theory)</pre>	is used to save a theory to the user's directory of theories
<pre>save_th_as(Th,NewTh)</pre>	is used to save a theory to the user's directory of theories under the name ${\tt NewTh}$
save_changed_ths	asks the user for each theory that has been changed whether it should be saved or not
axioms	displays all axioms in memory on the terminal or in the command window

The  $ilf\_state$  save\_th can contain a list of theories that are to be saved automatically when ILF is left. From the graphic user interface additional tools for the presentation of theories are available.

#### more of the THEORY menu

view_th	displays the hierarchy of theories in the windows of the <i>TreeViewer</i> . If a particular theory is selected with the right mouse button, it is displayed by the $IAT_EX$ system. Selecting the top node quits this operation
view_theory(Theory)	displays a particular theory by the $I\!AT_E\!X$ system

### **Proof Tactics**

Proof tactics are a way to automate parts of the work to be done to build a proof in a deductive system. They can perform a fixed sequence of steps like a macro or a refined control strategy like an automated theorem prover. In general, tactics are developed to test different procedures to control the search for a proof. Approved tactics are frequently incorporated as new rules of inference into a deductive system. Tactics are kept in files in the directory USERILFHOME/tac having the extension .tac. If there is a file named standard.tac, it is reconsulted at the start of *ILF* into the module tactics. These files can also include other commands to be performed, notably commands like ?- load("Filename.tac"). to reconsult more tactic files.

In principle, a tactic is developed and tested like any other programme in PROLOG-2 (see the PROLOG-2 manual for details). Basic tactics are provided by the integrated deductive systems as rules of inference or as commands for moving a focus to a certain position in the proof. From these, more complex tactics can be build using all the facilities of PROLOG 2 and some special tools described below. As long as tactics manipulate proofs only through the use of rules of inference, the correctness of the resulting proofs is guaranteed.

The specific set of commands that are available for building proof tactics depends on the deductive system in use. However, the following commands have been implemented for many systems in order to unify their use.

#### common tactics commands

pos(X)	unifies $X$ with the current position in the proof
<pre>set_pos(Pos)</pre>	moves the focus to the position $Pos$
<pre>successors(S)</pre>	unifies S with the list of successors of the current position. This assumes that the proof is represented as a directed graph.
predecessors(S)	unifies S with the list of predecessors of the current position. This assumes that the proof is represented as a directed graph.

<pre>subgoals(S)</pre>	unifies S with the list of open subgoals that have to be solved in order to solve the goal at the cur- rent position. The exact meaning of the concept of an open subgoal depends on the specific deductive system in use
fd(N)	moves the focus to the $\ensuremath{\mathbb{N}}\xspace$ the successor of the current position
bd(N)	moves the focus to the $\ensuremath{\mathbb{N}}\xspace$ the the the the transformation of transformation of the transformation of transformation o
up	is the same as $fd(1)$ . Backtracking does not undo the effects of the positioning commands. There- fore, in order to continue editing a proof at a cer- tain position after performing a tactic, this posi- tion has to be stored before the tactic and restored after the tactic has finished by a construction like $pos(X),Tactic,set_pos(X)$
d	is the same as bd(1)
problem(Pos,Con,Stat)	matches the formula at the position Pos in the proof with Con and the status of the position (e.g. proved or unproved) with Stat. The exact mean- ing of contents and status is system dependent. problem/3 is often used to analyze the current goal in order to chose an appropriate tactic

In many systems the application of a rule of inference is triggered by specifying a certain axiom. In ILF a name Name of an axiom can be used to call a procedure ax(Name) that acts in a system specific way. On backtracking, the effect of this procedure is undone.

The following *tacticals* can combine tactics. They are similar to the corresponding tacticals of the *Oyster* system ([BH90]).

#### common tactics commands

repeat_tac(Tac)	applies the tactic Tac at the current position and recursively to all open subgoals generated by Tac. This is done in a depth-first/left-to-right way. Backtracking into Tactic is possible
Tac1 then_tac Tac2	applies the tactic Tac1 at the current position and Tac2 at all open subgoals created by Tac1. Back-tracking into Tac2 is possible; if this has failed on all subgoals, backtracking into Tac1 is performed
Tac then_l [T1,,Tn]	succeeds if the tactic Tac generates exactly n open subgoals to which T1,,Tn are applied success- fully. Backtracking into Tn,,T1,Tac is possible

Global variables and loops are available for a procedural style of programming.

#### global variables commands

assign(R(A1,,An),V)	stores V in R in association with the parameters $A1, \ldots, An$ (n can be 0). For all settings of the parameters $A1, \ldots, An$ at most one value V is stored in R. It can be retrieved by $R(A1, \ldots, An, V)$
R(A1,,An) := V	evaluates V to a number and stores the result- ing value in R in association with the parameters $A1, \ldots, An$ . The value of V can be retrieved by $R(A1, \ldots, An, Value)$
(Procedure until Test)	applies Procedure until Test succeeds. Test is called after each run of Procedure. No backtrack- ing into Procedure is performed
(Procedure while Test)	applies Procedure as long as Test succeeds. Test is called before each run of Procedure. No back- tracking into Procedure is performed

Example:

```
my_status_tac(T,S) :- pos(P),(T until problem(P,_,S)).
```

 $my_status_tac(T,S)$  applies the tactic T until the initial position P has a status that matches S.

A complex tactic may generate large new subproofs. It may not be possible for a tactic to determine the size of these proofs in advance. In such a situation it can be useful to forget those positions that have been created by the tactic except for those which contain new open subgoals that still have to be proved. This can be achieved by running the tactics hard. In order to do this, call Tactic h\_d. Since a part of the result of the tactic has been eliminated, backtracking into Tactic is disabled. It appears as if a single new rule of inference that generated the new subgoals has been called.

### **Background Experts**

Background experts are systems controlled by the PROLOG running as a background process. Each of these experts can occur in several instances working on completely separated data. In order to use an expert, it must be mentioned in the .ilfrc file read at startup.

An expert named expert is started by  $ex\_start(expert,Nr)$ . If this call succeeds, Nr is instantiated with the number assigned to this expert by the internal ExpertManager. Commands can be sent to this expert by using the syntax Nr : Command\_1, ..., Command\_n. If Nr is 0, the commands are sent to the background ExpertManager.

If the expert has been successfully started, it must be usually configured by reconsulting an appropriate file from its directory \${USERILFHOME}/dedsys/expert. This can be done automatically if a file has been mentioned in the .ilfrc file or from the command line or by a tactic using the command Nr : open\_sit(File). The internal situation of an expert can be saved by Nr : save\_sit(File).

In order to use a background expert it is important to synchronize the work of the foreground deductive system and the background expert. Communication is synchronised by the command ex\_sync/0. All axioms having a name matching Name are sent to expert Nr by Nr : send\_ax(Name). Axioms can also be activated and deactivated for selected experts as for the foreground system. The easiest way to synchronize the knowledge bases of the foreground and a background expert is by using the commands ax\_sync/1, th\_sync/1 and kb\_sync/1. ax\_sync(Nr) assures that the foreground and the background expert Nr have the same axioms with the same names; th\_sync/1 synchronizes the hierarchies of theories and kb\_sync/1 performs both.

Before a background expert can be asked, an expert goal must be built. This can be done interactively by Nr : get\_expert\_goal/0 or automatically by a tactic. For the latter method, make\_exp\_goal(Goal,expert,unproved,Name,Nr) should be called. If this call succeeds, the background has accepted to try to prove Goal. Name can be an arbitrary PROLOG term that will be passed to the background system and back. It can be used to identify the results of the proof or to pass further control information to the background system.

When the background system has started its work on the goal, there will be a

fact expert\_goal(Goal, expert, started(Job), Name, Module) asserted in the foreground. Here, Job is the number of the job in the background and Module is the current input/output module when the problem was set up. By reference to the module the ExpertManager can continue to handle a job even if the deductive system which started the job has been suspended for some time or if different deductive systems start jobs with the same name. When the job gets done, started(Job) is changed to finished(Job). If the goal has been proved, a fact expert\_goal(Goal, expert, proved, Name, Module) will be present. Expert goals can be removed by rm\_exp\_goal/5. No deductive system is allowed to remove expert goals initiated by other systems.

In order to obtain the results of the background systems, the foreground system must call ex\_answer/0 from time to time.

In general it is impossible for a background expert to decide whether it should keep on trying to find a proof or better try another problem. In order to make this decision in an automated way the method of *flexible killing* can be used to interrupt the work of automated experts running as separate processes. A maximum and minimum number of seconds a system is allowed to run can be set up by Nr : set\_max\_sec(Seconds) and Nr : set\_flexy\_sec(Seconds). Default values can be determined in the *ilf\_states* default\_max\_sec and default\_flexy\_sec, respectively. Note that the time given in default\_max\_sec is CPU time, but the time in default\_flexy\_sec is real time. If a command kill\_flexy/0 is send to the expert Nr, its processes will be killed if its minimum number of seconds has expired. If the time given in default\_max\_sec is reached, the processes belonging to the expert will be killed by the cpu limit mechanism of the C shell.

# **Deductive Systems**

We distinguish interactive and automated deductive systems. Usually, interactive systems are controlled by the PROLOG working in the foreground, while automated deductive systems work in the background, sometimes as separate processes.

### 8.1 Interactive Deductive Systems

### 8.1.1 FLEX – SLD Resolution

FLEX is an interactive proof editor for SLD-resolution proofs for universal Horn theories. A (partial) proof is given as a tree of literals with a unique root input which stands for contradiction. The semantics of such a proof tree is given as follows: The universal closure of a node is proved if the universal closure of all of its sons is proved.

ax/1 is the only inference rule of *FLEX*. It applies the axiom whose name is given as its argument to the actual position, i.e. if the actual position is a leaf and the literal at this position matches the head of the axiom, then the most general unifier is applied to the tree and the literals of the body of the axiom are added as sons of the current position.

If the axiom is a fact, the current node is treated as being closed. A tree having only closed leaves is a proof. The name given as argument to ax/1 can be any valid PROLOG term including \_. On backtracking all axioms with matching names will be applied to the actual position. For the user's convenience for every axiom named Name a clause Name :- ax(Name) is asserted, so axioms can be called by simply typing their names.

For positioning in the proof tree the commands d/1, d/0, up/1, up/0,  $up_down/2$  described in Section 6 can be used.

last/0 positions on the most recently generated leaf.

tree/O shows the actual proof tree.

tree(N) shows the actual proof tree starting N nodes above the actual position.

problem/0 shows the literal at the current position together with its state (proved or unproved, leaf or node).

h/0 shows the actual possibilities to proceed, that is, the open leaves that can be selected or the axioms appliable to the selected leaf.

back/0 does explicit backtracking.

A sequence of positioning commands and inference rule applications in *FLEX* can be recorded as a tactic by record\_tac/0. The tactic recorder is stopped by end\_tac. The user will be prompted for a name under which the tactic will be saved. A saved tactic can be stored in a file using store\_tac/0.

FLEX can be started by flex/O or flex/1. If no tactic is given as an argument, the tactic break is used and FLEX will work interactively. If it is not started by the command Head to Body by flex(Tactic) but simply by the command flex, FLEX prompts the user for a goal to prove which must be a conjunction of literals. The proof tree is initialized by adding the literals of the goal as sons of the root.

If no tactic is called *FLEX* works in PROLOG-2's break modus, which can be left by typing end\_of\_file or selecting leave FLEX from the flex menu (in fact, this is currently the only point to select from this menu).

Successors of a node in the proof tree are its sons and the only predecessor is its father. Subgoals of a node are the leaves below it that are not closed. These concepts are relevant for the use of tacticals (see Section 6).

### 8.1.2 ME – Model Elimination

ME is an interactive proof editor for the model elimination procedure as suggested by Stickel in [St84]. Stickel considered the model elimination as an extension of PROLOG-style logic programming from Horn clauses to arbitrary clauses. Therefore ME was implemented as an extension of FLEX, so most of the functionality of FLEX is also available under ME. The code both systems are sharing is located in kern.prm while the system-specific code is in me.prm.

A (partial) proof is a tree of literals with the root false, which stands for contradiction. The semantics of this tree are given similiar to *FLEX*: if the universal closure of all sons of a given node is proved, then the universal closure of this node is proved, too. A tree whose leaves are proved is therefore a proof of a contradiction, i. e. a refutation for the given set of clauses. Completeness for first order Hornlogic is achieved by using all contrapositives of all clauses including the goal and an additional inference rule, the (ME-)reduction rule (the inference rule of PROLOG or *FLEX* is in this context called extension rule).

*ME* can be started by **me/O** or **me/1**. If no tactic is given as argument, the tactic **break** is used, i. e. *ME* works interactively. If necessary, it prompts the user for a goal to prove which must be a conjunction of literals. The proof tree is initialized by adding these literals as sons of the root.

Because of the need of all contrapositives ME uses its own theory data base formed during startup. If you add axioms to ILF's theory while using ME, use\_cp/0 must

be called to make the contrapositions available for *ME*. The name of a contrapositive is derived from the name of the corresponding axiom by adding the number of the literal considered to be the head as last argument (e. .g. from **ass(+)** you will get **ass(+,1)**, **ass(+,2)**, ... corresponding to the choice of the first, second, ... literal as the head). The names of the contrapositives of the negated goal are goal(1), goal(2), ....

All contrapositives can be listed by cps/0.

**ax/1** is the command for the extension rule and works as in *FLEX*. For the user's convenience for every contrapositive/axiom named name a clause name :- **ax(name)** is asserted as in *FLEX*.

The reduction rule can be applied via the red/1 command. red(N) reduces the actual leaf with its N-th ancestor, i. e. if the current goal matches the complement of its N-th ancestor goal, then the most general unifier will be applied to the tree and the current goal will be treated as solved. If N is not instantiated, red/1 finds all possibilities for ME-reduction by backtracking. red/0 is a shorthand for  $red(_)$ .

The tree positioning commands and the concepts of successors, predecessors and subgoals are the same as in FLEX (see Section 8.1.1).

### 8.1.3 MPRT

MPRT is an interactive proof editor for the modified problem reduction format as defined by Plaisted in [Pl88].

Proofs are represented as trees similiar to FLEX and ME. A discussion of the tree representation of modified problem reduction can be found in [Me90].

MPRT uses three inference rules: axiom application, assumption application and splitting (see below). Note that MPRT is much simpler than the TMPR-prover developed by Mellouli<sup>1</sup>.

The system consists of two parts: the executable mprt connected with *ILF* as described in Section 9 and the Prolog module mprt.prm which provides some additional functionality. The executable was developed in the programming language C using the *ILFA*-libraries (see [DFKBLL]).

**ax/1** is the command for the axiom application rule. It applies the axiom whose name is given as an argument at the actual position, i. e. if the actual position is a leaf and the literal at this position matches the head of the axiom, then the most general unifier is applied to the tree and the literals of the body of the axiom are added as sons of the current position. If the axiom is a fact, then the current node is treated as proved. The name given as argument to **ax/1** can be any valid Prolog term including \_. On backtracking all possible axioms will be tried at the actual position. For every axiom named name a clause name :- **ax(name)**. is asserted for the user's convenience.

ass/1 applies an assumption at the actual position, i. e. if the actual position is an unproved leaf and the assumption identified by the argument matches the literal

 $<sup>^{1}</sup>MPRT$  is comparable to the WMPR (weak MPR) described in [Me90].

of the leaf, the matching substitution is applied to the tree and the current node is marked as proved by assumption.

case/1 splits the current node over the literal provided as argument. This rule is applicable to each node of the tree, not only to leaves. The positioning commands described in Section 6 are available.

problem/0 shows the literal at the current position together with its state (proved or unproved, leaf or node). By problem/3 you can use this information in a tactic.

h/O shows the axioms and assumptions applieable at the current node. Under the graphic user interface a menu Rules containing these possibilities is constructed. h is accessible via the help point from this menu.

back/0 does explicit backtracking.

MPRT is started by mprt/0 or mprt/1. If no tactic is given as the argument, the tactic break is used, i. e. MPRT works interactively.

The core of MPRT is a C programme. Under the graphic user interface a window for error messages from this programme will be created presenting the process id of the executable in the title. MPRT has to be initialized by mprt\_start/0.

The proof tree is initialized by applying the goal to the root and positioning to the first son of root.

Interactive work in *MPRT* can be left by typing end\_of\_file or selecting leave from the mprt menu.

### 8.1.4 pNAT – PROLOG Based Natural Reasoning

The pNAT is an Interactive Theorem Prover on the calculus of Natural Reasoning, as it is usually described in the literature. A detailed description can be found in [Wo92].

### Commands of pNAT

sequents.	lists out all sequents of the actual situation of the system
nat_start.	initializes or reinitializes the system, all previous information will be lost
load_theory.	converts all $ax\_name$ facts from the current situa- tion module into the internal syntax of pNAT
load_goal.	converts the <i>ilf_goal</i> into the internal syntax of pNAT

use(Rule,Info,Pos_list).	performs a deduction step in the calculus, pre- dicate is backtrackable, Rule can be one of the following: $in(not)$ , $out(not)$ , $in(and)$ , $out(and_1)$ , $out(and_2)$ , $in(or_1)$ , $in(or_2)$ , $out(or)$ , $in(imp)$ , $out(imp)$ , $in(aeq)$ , $out(aeq_1)$ , $out(aeq_2)$ , $in(all)$ , out(all), $in(ex)$ , $out(ex)$ , $ns1$ or $ns2$ , Info is in most of the cases a pattern of the right side to be built and may often be a variable, and Pos_list is the List of parent sequents, often all parameters can be variables
use(Offs,Rl,Info,Posl).	as use/3, the Value of Offs will be added to the numbers in the Posl, can be used to access to rel- atively adressed sequents, Offs and Posl may not be Variables, else the predicate fails
<pre>control(Left,Right).</pre>	is true if there is a sequent of the given form
result(Pos).	asserts the sequent with the highest position (number) as proved to an $\mathit{ilf}\_goal$
offset(Nr).	Nr will be the number of the sequent created last, it is usable e.g. with $use/4$
set_pos(Pos).	sets the actual position of the system to be $Pos$ , backtrackable
pos(Pos).	gives back as ${\tt Pos}$ the actual position, backtrack-able
predecessor(Pred).	gives back as <b>Pred</b> a parent of the actual position, backtrackable
predecessors(Predl).	gives back as <b>Predl</b> the list of all parents of the actual position
<pre>predecessors(Pos,Predl).</pre>	gives back as $\tt Predl$ the list of all parents of $\tt Pos$
successor(Succ).	gives back as Succ a child of the actual position, backtrackable
successors(Succl).	gives back as Succl the list of all children of the actual position
<pre>successors(Pos,Succl).</pre>	gives back as Succl the list of all parents of $\tt Pos$
up(N).	sets the actual position to be the N-th predecessor of the current actual position
down(N).	sets the actual position to be the $N-$ th successor of the current actual position
contents(Seq).	gives back as $\operatorname{Seq}$ the contents of the actual position
contents(Pos,Seq).	gives back as ${\tt Seq}$ the contents of the position ${\tt Pos}$
status(Stat).	shows the status of the actual position, Stat can be <i>initial</i> (the root node), <i>axiom</i> , <i>leaf</i> or <i>node</i>

<pre>status(Pos,Stat).</pre>	gives back as $\texttt{Stat}$ the status of the position $\texttt{Pos}$
back.	retracts the sequent created last
back(N).	retracts the sequent with the number $\mathbb{N}$ , it naturally must be a leaf

The subgoal. command is not implemented, because it makes no sense in the context of the pNAT system.

### 8.1.5 pTAB – PROLOG Based Tableau Calculus

The pTAB is an interactive theorem prover based on the tableaux calculus, as it is usually described in the literature (see [Sm68]). For details of this implementation see [Wo92].

#### Commands of pTAB

nodes.	lists out all nodes of the tableau tree
structures.	lists out all variable structures of the current tree (see implementation)
<pre>show_branch(Leaf).</pre>	shows all nodes on the path from <code>leaf</code> to the root node of the tableau tree
show_tree.	shows all branches
proof.	tests if the current tree is a proof, too
tab_start.	(re-) initializes the prover
load_theory.	integrates the current knowledge base in the ta- bleau tree, new axioms will be built in as root node
load_goal.	integrates the current $ilf_{-}goal$ into the tree
<pre>set_pos(Name,Leaf).</pre>	sets the actual position to be on the node Name and on the path above Leaf
<pre>set_pos([Name,Leaf]).</pre>	as set_pos(Name,Leaf).
<pre>successor(X).</pre>	gives back a successor of the actual position, back-trackable
<pre>predecessor(X).</pre>	gives back a predecessor of the actual position, backtrackable
top.	sets the actual position on the root node and an arbitrarily selected leaf
up.	sets the actual position on the predecessor
up(N).	N times $up$ .
d.	sets the actual position on the first sucessor
d(N).	sets the actual position on the N-th successor, corrects the actual leaf $% \mathcal{A}_{\mathrm{rec}}$

left.	sets the actual position on the left brother of the old position
<pre>left(N).</pre>	sets the actual position on the N-th left brother of the old position $\$
leaf(Leaf).	gives back as Leaf a leaf of the tableau tree
leaves(X).	gives back the list of all leaves
open_branch(Leaf).	gives back as ${\tt Leaf}$ an open leaf of the tableau tree
open_branches(X).	gives back the list of all open leaves
<pre>subgoal(X).</pre>	gives back an open leaf below the actual position, backtrackable
<pre>contents(Node,Formula).</pre>	gives back as ${\tt Formula}$ the formula of the node ${\tt Node}$
<pre>status(Name,Leaf,Sta).</pre>	gives back as <b>Sta</b> the status informations of the node <b>Node</b> with respect to the leaf <b>Leaf</b>
<pre>split(Name,Leaf).</pre>	splits the formula of the node Name, and expands the tree by appending the resulting formulas of the split below the leaf Leaf (if all that is possible), the predicate is backtrackable, the arguments may be variables
<pre>close_branch(Leaf,N).</pre>	tries to close up the branch above $\texttt{Leaf}$ , if $\mathbb{N}$ is an integer, one of the two nodes used for a closure must have a node number greater than $\mathbb{N}$
close_branch(Leaf).	the same as close_branch(Leaf,_).
close_branch.	prompts for a leaf and (re-) tries to close up the branch belonging to that leaf
back.	prompts for a node and takes back all splits done after the creation of this node

### 8.1.6 iTAB – Tableau Calculus based on the ILFA Library

The iTAB is an interactive theorem prover based on the tableaux calculus, as it is usually described in the literature (see [Sm68]), implemented in C using the libraries of the *ILFA* system (see [DFKBLL]).

#### Commands of itab

back.	takes back the last tree expanding command
load_theory.	transmits the current knowledge base to $itab$
goal.	transmits the current <i>ilf_goal</i> to <i>itab</i>

<pre>local_pos([Node,Leaf]).</pre>	reads the list of local positions, i.e. the actual node and the actual leaf from <i>itab</i> and assigns that information to be the argument of the predicate <i>local_positions</i> (as a list)
<pre>set_local_pos([Nd,Lf]).</pre>	sets the the actual node and the actual leaf to be $\tt Nd$ and $\tt Lf$
pos(Node).	reads the actual position from $itab$ and assigns that information as the argument of the predicate $ac$ -tual_position
<pre>set_pos(Node).</pre>	sets the the actual node to be Node
<pre>contents(Cont,Var).</pre>	reads the formula contained in the node of the actual position from $itab$ as Cont with the variable name structure Var
contents(Cont).	the same as contents(Cont,_).
<pre>contents(Pos,Cont,Var).</pre>	as contents(Cont,Var)., but not of the actual position but of the node Pos
status(Stat).	gives back as <b>status</b> the status information of the actual node in relation to the actual leaf, i.e. if the branch is closed or open
status(Pos,Stat).	as status(Stat)., but not of the actual position but of the node Pos
subgoals(Sub).	gives back as ${\tt Sub}$ the list of all open leaves below the actual node
subgoals(Pos,Sub).	as <pre>subgoals(Sub).</pre> , but not of the actual position but of the node Pos
successors(Succ).	gives back as $\tt Succ$ the list of all nodes directly below the actual node
<pre>successors(Pos,Succ).</pre>	as $\verb+successors(Succ)., but not of the actual position but of the node \verb+Pos+$
predecessors(Pred).	gives back as <b>Pred</b> the list with the node directly above the actual node
predecessors(Pos,Pred).	as predecessors(Pred)., but not of the actual position but of the node Pos
fd(N).	sets the actual node to be the Nth successor of the current actual node, warns if the leaf is not set correctly
bd(1).	sets the actual node to be the predecessor of the current actual node
<pre>set_leaf(Leaf).</pre>	sets the actual leaf to be Leaf
ax(Name).	splits the axiom $\tt Name$ below the actual leaf, if possible
branch.	shows the contents and status of all nodes above the actual leaf with respect to that leaf

s(Node,Leaf).	tries to split the node Node and to expand the tree
	below the leaf Leaf
c(Leaf).	tries to close up the branch above the leaf ${\tt Leaf}$

## 8.2 Automated Deductive Systems

## 8.2.1 DISCOUNT

This system integrates the *DISCOUNT* system for distributed knowledge based equational reasoning and completion from the University Kaiserslautern [DP92]. The flags and parameters follow the user manual of *DISCOUNT*. The system automatically works in the silent and team mode and will perform *PCL* with the same input files if the task can be proved to get the dependencies. It is possible to configure experts, referees and selectors (in the sense of *DISCOUNT*) and to combine them to teams. Unlike the original *DISCOUNT*, experts, referees and selectors have to be referred to by names that can be arbitrary PROLOG terms.

#### **DISCOUNT** menu

ask	n	gives the current <i>expert_goal</i> to the background and expert starts working, performs <b>ex_ask</b> .
end	n	terminates this expert, performs <b>ex_end</b> .
refresh	n	rebuilds the menu with the current menu level, performs refresh_menu.
send_axioms	с	transmits the matching axioms of the current knowledge base to the expert, performs send_axioms(Name).
goal	с	prompts the user to type a formula to use it as an <i>expert_goal</i> , performs get_expert_goal.
use result	С	prompts the user for a name to integrate a proved <i>expert_goal</i> with the given name into the current knowledge base, performs use_expert_goal.
kill_flexy	n	kills the actual task of the expert if the minimum time ( <i>default_flexy_sec(Sec)</i> , set in the .ilfrc file) for the task is over, performs kill_flexy.
file	S	submenu relating to file operations
open_sit	С	performs <code>open_sit(File).</code> , prompts the user for the name of the file with the data module to be used by the expert
<pre>save_sit</pre>	с	performs save_sit(File)., prompts the user for the name of the file to save the data module as this file

In higher menu levels there are many other menu points to configure the team of DISCOUNT experts, here are listed only the points that are additions to the user manual.

#### more from the **DISCOUNT** menu

set_flexy_sec	с	prompts the user to type in the minimum (real) time <i>DISCOUNT</i> can work without getting killed, performs set_flexy_sec(Sec).
max_seconds	С	prompts the user to type in the maximum (cpu) time <i>DISCOUNT</i> can work without getting killed, performs set_max_sec(Sec).
define experts -	→ bui	ild $\rightarrow$ statistics
	S	nested submenu to create and name an expert, here a $statistic$ expert, other types see the menus and the user manual of $DISCOUNT$
add_weight	С	the user shall fill in the pattern $bld(exp, Name, add_weight(FWeight, VWeight, RedInst, Order))$ with the wanted parameters to define the $add_weight$ expert Name
define spec $\rightarrow$ 1	build	
	$\mathbf{S}$	nested submenu to create and name a specialist
reduce_cp	С	the user shall fill in the pattern <i>bld(spec, Name, re-duce_cp(StrtCp, RdCp, SsCp, DblCp))</i> with the wanted parameters to define the <i>reduce_cp</i> specialist <i>Name</i>
define referee	→ bui	ild
	$\mathbf{S}$	nested submenu to create and name a referee
statistic	с	the user shall fill in the pattern <i>bld(ref, Name, statistic(SR, SE, SCP, RedCnt, MsFg))</i> with the wanted parameters to define the <i>statistic</i> referee <i>Name</i>
define select -	→ bui]	Ld
	$\mathbf{S}$	nested submenu to create and name a selector
statistic	С	the user shall fill in the pattern <i>bld(sel, Name, statis-</i> <i>tic(NrRls, NrEqs, MinV, RCnt, RRt, RLt, REq, RGl,</i> <i>RSsum, CpCnt))</i> with the wanted parameters to define the <i>statistic</i> selector <i>Name</i>
$\texttt{team} \ \rightarrow \ \texttt{static}$		
	S	nested submenu to create and name a <i>static</i> triple of expert, referee and selector
add	С	the user shall fill in the pattern <i>add_er(static, Exp, Ref, Sel)</i> with the names of the predefined expert, referee and selector, the system will treat them as a triple for the configuration of <i>DISCOUNT</i>

## 8.2.2 SETHEO

The *SETHEO* system uses the *SETHEO* resolution based automated theorem prover from the Technical University Munich [LSBB92]. The system will verify the dependencies of the goal from the input formulas and write them back to the user.

#### SETHEO menu

ask	n	gives the current <i>expert_goal</i> to the background and expert starts working, performs <b>ex_ask</b> .
end	n	terminates this expert, performs <b>ex_end</b> .
refresh	n	rebuilds the menu with the current menu level, performs refresh_menu.
send_axioms	С	transmits the matching axioms of the current knowledge base to the expert, performs <code>send_axioms(Name)</code> .
goal	с	prompts the user to type a formula to use it as an <i>expert_goal</i> , performs get_expert_goal.
use result	С	prompts the user for a name to integrate a proved <i>expert_goal</i> with the given name into the current knowledge base, performs <b>use_expert_goal</b> .
kill_flexy	n	kills the actual task of the expert if the minimum time ( <i>default_flexy_sec(Sec)</i> , set in the .ilfrc file) for the task is over, performs kill_flexy.
<pre>set_flexy_sec</pre>	С	prompts the user to type in the minimum (real) time <i>DISCOUNT</i> can work without getting killed, performs set_flexy_sec(Sec).
max_seconds	n	prompts the user to type in the maximum (cpu) time <i>DISCOUNT</i> can work without getting killed, performs set_max_sec(Sec).
file	s	submenu relating to file operations
open_sit	С	performs open_sit(File)., prompts the user for the name of the file with the data module to be used by the expert
save_sit	с	performs <b>save_sit(File)</b> ., prompts the user for the name of the file to save the data module as this file

#### 8.2.3 **OTTER**

OTTER is an automated theorem prover from Argonne National Laboratory ([MC90]) for first order theories with special support for reasoning about equality. The syntax of the commands is as described in *Otter*'s manual, except that theories and goals are taken from *ILF*. Therefore, we describe only the commands to control the work of the expert.

#### **OTTER** menu

ask	n	gives the current <i>expert_goal</i> to the background and expert starts working, performs <b>ex_ask</b> .
end	n	terminates this expert, performs <b>ex_end</b> .
refresh	n	rebuilds the menu with the current menu level, performs refresh_menu.
send_axioms	С	transmits the matching axioms of the current knowledge base to the expert, performs <b>send_axioms(Name)</b> .
goal	С	prompts the user to type a formula to use it as an <i>expert_goal</i> , performs get_expert_goal.
use result	С	prompts the user for a name to integrate a proved <i>expert_goal</i> with the given name into the current knowledge base, performs use_expert_goal.
kill_flexy	n	kills the actual task of the expert if the minimum time ( <i>default_flexy_sec(Sec)</i> , set in the .ilfrc file) for the task is over, performs kill_flexy.
file	$\mathbf{S}$	submenu relating to file operations
open_sit	с	performs <b>open_sit(File)</b> ., prompts the user for the name of the file with the data module to be used by the expert
save_sit	С	performs <b>save_sit(File)</b> ., prompts the user for the name of the file to save the data module as this file
otter_input	С	prompts the user for the name of the file to use as $OT$ - $TER$ input file, performs otter_input(File).

## 8.2.4 An AC Rewrite System for Lattices and Groups

The BgPest system tries to prove a given formula by rewriting due to a method of Peterson and Stickel [PSt81]. It decides automatically whether the theory of groups or of lattices is to be used, depending on the leading operator of the left side of the equation. If there is no operator, then one will be searched on the right side.

The result will be the (lexicographically smallest) normal forms of both sides of the equation, but only if these sides are not variables. The usage follows the standard of the ExpertManager, but it is not necessary and not possible to send theories to the background.

#### BgPest menu

ask	n	gives the current <i>expert_goal</i> to the background and ex-
		pert starts working, performs <b>ex_ask</b> .
end	n	terminates this expert, performs $ex\_end$ .

goal	с	prompts the user to type a formula to use it as an <i>ex</i> -
		<pre>pert_goal, performs get_expert_goal.</pre>
use result	с	prompts the user for a name to integrate a proved $ex$ -
		<i>pert_goal</i> with the given name into the current knowledge
		base, performs use_expert_goal.

### 8.2.5 Algebra

*algebra* is an automated deductive system specialized to utilize simple algebraic properties. Unlike other automated systems it works in the foreground because it performs relatively simple actions.

When *algebra* is started for the first time it checks the actual knowledge base for axioms saying that some of the operators are associative, commutative, or distributive. Currently, *algebra* has the following rules.

#### algebra menu

iso_rule(P).	reduces a goal G with subterm T at position P to (T=U,G'), where U is a new variable and G' is obtained from G by replacing T at position P by U
<pre>demod_rule(Name,PosList)</pre>	applies an equation name Name at the positions in the list PosList of the goal. If the equation has preconditions, they are collected in the body of the goal to be proved
dis_rule(P).	reduces a goal G by applying a distributive law at position P of G. If the same law can be applied at the newly generated subterms, this is performed
ac_move_rule(Src,Dest).	reduces a goal G by moving the subterm at position Src to the subterm at position Dest, provided this is justified by associative and commutative laws

### 8.2.6 TwoLat – the Two Element Lattice

The *TwoLat* system is not a deductive system in the usual sense, it tests formulas in the lattice with two elements. The fact that a universal Horn formula is true in that model, can be treated as a proof of this formula from the theory of distributive lattices (see [Da93]). Moreover, the system can be used as a model tester to prevent proofs of formulas not valid in that model (so-called junk theorems). The usage follows the standards of the *ExpertManager*, but it is not nessecary and not possible to send theories to the background. The user must recall, that "proved by *TwoLat*" means only valid in the model of *TwoLat*. TwoLat menu

ask	n	gives the current <i>expert_goal</i> to the background and expert starts working, performs <b>ex_ask</b> .
end	n	terminates this expert, performs ex_end.
goal	С	prompts the user to type a formula to use it as an <i>ex-</i> <i>pert_goal</i> , performs <b>get_expert_goal</b> .
use result	С	prompts the user for a name to integrate a proved <i>expert_goal</i> with the given name into the current knowledge base, performs <b>use_expert_goal</b> .

### 8.2.7 ThreeLat – a Three Element Lattice Model

ThreeLat is a system that checks the validity of a quantifier free formula G from the language of lattice ordered groups in the integers. G may contain additional constants, and facts about these constants may be given as additional axioms. More precisely, it is checked whether G holds in this model for all instances of the constants with the values -1, 0, 1 satisfying the additional axioms. If this is true and G is a Horn formula which does not contain the symbol for the group operation, *ThreeLat* returns **proved** since G is a logical consequence of the theory of lattice ordered groups and the additional axioms (see [Da93]). If G holds but is not a Horn formula or contains the group operation symbol, *ThreeLat* returns **passed**, otherwise it returns **refused**. The usage follows the standard of the ExpertManager, but it is not necessary and not possible to send theories to the background.

#### ThreeLat menu

ask	n	gives the current <i>expert_goal</i> to the background and expert starts working, performs <b>ex_ask</b> .
end	n	terminates this expert, performs $ex\_end$ .
goal	С	prompts the user to type a formula to use it as an <i>ex-</i> <i>pert_goal</i> , performs get_expert_goal.
use result	С	prompts the user for a name to integrate a proved <i>expert_goal</i> with the given name into the current knowledge base, performs <b>use_expert_goal</b> .

## Chapter 9

## Extending ILF

Extending the power of ILF requires more information on the internal structure of ILF, which will be given in this section. We shall describe how to integrate new interactive and automated systems.

## 9.1 Integration of Interactive Systems

The knowledge base of ILF is kept in the PROLOG module axioms.prm in the predicate ax\_name/4. The first argument of this predicate is the name of the axiom, the second and third argument are head and body of the sequent constituting the axiom. The last argument is a variable name structure as described in the manual of PROLOG 2. If the structure of a sequent is not relevant, the complete formula can be contained in the second argument while the third argument is true.

When a new deductive system is called, the corresponding module is loaded and a separate module for the data of the system is created. If the system contains predicates defined elsewhere, the new definitions override the existing ones. This makes it possible to realize the same commands in different systems by different procedures. When a system finishes its work, the original definitions are restored.

Deductive systems are accessed via the deduction system manager, which is called by ded\_sys\_man/2. The first argument is the deductive system to activate, the second a tactic to execute.

By convention every deductive system DedSys provides the predicates DedSys/0 and DedSys/1 defined as

```
DedSys :- ded_sys_man(DedSys,break).
DedSys(Tactic) :- ded_sys_man(DedSys,Tactic).
```

If the deduction system manager gets messed up (for instance by leaving the Tactic or the break by abort) use reset/0 to set it in its initial state.

When a deductive system starts, the deduction system manager has created a data module containing only a fact ilf\_goal(Head,Body,unproved,Name) and being

the current input/output module. Body  $\longrightarrow$  Head is the formula to be proved. The last argument Name is a name for this formula if the system was called by the command reduces and none otherwise.

When the system is left, the third argument must be changed from unproved to proved if the goal has been proved. It is also possible to instantiate variables in the formula if only an special case of the goal could be proved.

The designer of a deductive system must be aware that ILF may backtrack into the system in order to look for another proof of the same goal.

A deductive system is integrated by defining a new fact:

```
ded_sys_props(System,Modules,CallProcedure,ExitProcedure)
```

Here

- System is the name of the system,
- Module is a list of PROLOG modules to be loaded,
- CallProcedure is a PROLOG predicate that is performed before any tactic,
- ExitProcedure is a PROLOG predicate that is performed before the deductive system is left, if the tactic succeeded.

A new interactive deductive system should – if possible – define the predicates successors, predecessors, subgoals, problem described in Section 6 in order to make tacticals available.

New deductive systems developed in C must also be connected with ILF through a PROLOG module.

Strictly speaking, the C programme required is a collection of procedures. Some of these procedures are necessary. E.g. load\_theory to load a knowledge base and return handles for the axioms read, goal to read a goal to be proved etc. A complete list with a description of the interface is contained in the file ceditor.dok. The main() function and the functions necessary to communicate with *ILF* are defined in editor.c. The C-programmer has to include ceditor.h and editcmds.h and link his object files with editor.o and editcmds.o. All these files are located in the \$ILFHOME/src/c/ceditor directory.

The PROLOG side of the interface can make use of the modules ilfa.prm and editor.prm, which implement the standard commands and the predicates for the communication. If the call procedure of the new deductive system calls ilfasys\_init(Path,Title), where Path is the complete path to the executable programme, Title in connection with a process ID is used as the title of an X-term showing the stderr of the C programme.

## 9.2 Integration of Automated Theorem Provers

Automated theorem provers are usually integrated as background experts. They should have a PROLOG module SYSTEM.prm that has all its predicates private except for SYSTEM\_top/0, which is called starting the system named SYSTEM and a

special predicate port\_SYSTEM/1, which must be defined by port\_SYSTEM(X) :- X. Moreover, there must be the predicate listen\_problem/1. If this predicate is called with an argument of the form expert\_goal(Goal,SYSTEM,Job,Name,Nr), the automated theorem prover should try to prove Goal from the theory it finds in its ax\_name/4 predicate in its data module exp\_Nr, where Nr is the the number of the expert, obtained from the ExpertManager. Since all predicates in the data module of the system are private, different copies of the same system may be active at the same time. In order to access the data in the data module, port/1 is used. If predicates from the data module are called by external predicates like bagof, they must be included in port/1. When the prover has finished its work successfully, it should call output\_write(Job,expert\_goal(Goal,SYSTEM,proved(Job),Name,N)). Finally it must call output\_write(Job,ready).

If an external system is not implemented within the PROLOG-2 in the background is called, listen\_problem/1 must produce an input file for the external system and start it as a background process using PROLOG's call/1 command. Then listen\_problem/1 should succeed without the call of output\_write(Job,ready). For such systems there must be a predicate search\_results/3 defined for the system. The call search\_results(SYSTEM,Nr,Job). informs the system SYSTEM with data module exp\_Nr that the results of the Job Job can be analyzed. Usually, the raw output of the external system will be analyzed roughly by a filter programme which sends the call search\_results(SYSTEM,Nr,Job). to the pipe \$USERILFHOME/tmp/coma.p. The ExpertManager in the background prolog will forward this call to SYSTEM. search\_results should finish calling output\_write(Job,ready).

It is recommended to start external processes with limited CPU time. After the call of the external system in the listen\_problem predicate, a programme that finds out the PID's of the processes belonging to the external system should be called. These PID's should be sent to the pipe \$USERILFHOME/tmp/coma.p as pid(List), where List has the form [Nr|PID\_list] and PID\_list looks like [PID1,...,PIDn] or [[Host1,PID1],...,[Hostn,PIDn]]. Since the determination of the exact PID's is often not possible (e.g. using *DISCOUNT*), the flexy\_kill mechanism will send signal 9 to the processes PID, PID+1 and PID+2.

Generic background experts can be found in the files  $\{ILFHOME\}/doc/name.pro$  and  $\{ILFHOME\}/doc/name1.pro$ .

## 9.3 Adding Menus

If the graphical user interface is active, a new menu named MENU can be brought up by the command create\_menu(MENU). The items of this menu are descibed by the predicate menu\_info\_MENU/2 in the module exmenus.prm. The first argument of this predicate is a number N indicating that this item will be displayed at menu levels greater or equal to N.

If the item is a submenu, the second argument is the string to be shown as the title of the submenu.

By an *itemlist* we mean a list having three members. The first is one of the atoms confirm and noconfirm, indicating whether the action triggered by the menu item needs confirmation from the user or not. The second member is a string or an atom to be displayed in the menu and the last member is a string to be passed to PROLOG when the menu item has been selected.

It is also possible to create a separator within a menu by filling in [separator] as *itemlist*.

For menu items of the top level menu, the second argument of  $menu_info_MENU/2$  is an itemlist describing the item. For items of submenus the second argument is a difference between a sequence of x and an itemlist. The length of the x-sequence coincides with the depth of the item in the menu hierarchy.

Here we give an example of some possible lines:

```
menu_info_expert(0,[confirm,load_tac,"0:load_tac(Tac)"]).
menu_info_expert(0,[noconfirm,answer,ex_answer]).
menu_info_expert(0,[confirm,menu_level,"new_level(N)"]).
menu_info_expert(0,[separator]).
menu_info_expert(1,synchronize).
menu_info_expert(1,x-[noconfirm,communication,ex_sync]).
menu_info_expert(1,x-[confirm,axioms,"ax_sync(ExpertNr)"]).
```

## Chapter 10

# A Sample Configuration: The ProofPad

We describe a configuration of ILF that has been designed to make the power of recent deductive systems available to users not specially trained. The version currently implemented is configured to support proofs from the first order theory of lattice ordered groups. However, the description below will not refer to these special aspects. We shall explain the integration of the different parts of ILF within one application.

The *ProofPad* is a deductive system of very limited abilities that are considerably extended by the use of other deductive systems. It presents to the user as a sequence of proof lines to be edited. Each line has a status and the aim of the user is that each line has the status proved. However, the user cannot change the status directly. The system checks automatically, whether a specific line is a logical consequence of the preceding lines. It takes a fixed number of preceding lines into account. This number can be set with the *ilf\_state* pad\_recall; its default value is 3. Each time the user inserts a new line, the modified problems are passed automatically to a process running in the background. This background process tries to solve the problems within a limited amount of time. It can employ also other deductive systems, notably the automated theorem provers SETHEO and DISCOUNT. The work of these systems is controlled in a flexible way using the predicate **flexy\_kill** described in section 7. If the background prover can prove a line, its status is changed in the foreground to proved, otherwise to unproved. Since the background can also test the validity of formulas in domain specific finite structures, it may also find out that a formula is unprovable and change the status accordingly to unprovable. This may happen because the user has made a semantic mistake or because the preceding lines do not yet contain enough information.

Like any other deductive system, it is called by [Name reduces] Head to Body by pad(Modus) (cf. 3.1). Modus can be direct or indirect depending on the type of proof to be edited. Currently only direct proofs are supported. It is also possible to call simply pad. Then the *ProofPad* will ask the user for the necessary information.

When the *ProofPad* has been started, the background is configured in an appropriate way. This can be seen by the menus of the background experts that become available

now. The actual status of the proof can be inspected in three ways, which are all available either from the command line or from *ProofPads* pulldown menu.

#### viewer commands of ProofPad

show_pad	is the fastest way to see the proof in the command window
pad_graph	shows the structure of the proof in the graphics window of the <i>TreeViewer</i> . The single lines can be seen in the text window of the <i>TreeViewer</i> . The form of the presentation depends on the <i>ilf_state</i> pad_mode. If it is set to line, the proof is pre- sented as a sequence of lines as by the show_pad command. However, if it is set to tree, the logical structure of the proof is shown as a directed graph. Edges of this graph indicate logical dependencies among the lines.
pad_view	this command produces a file proof.tex in the directory \${USERILFHOME}/tmp. This is treated by IAT <sub>E</sub> X and presented by the xdvi command. Details on the IAT <sub>E</sub> X output are explained below.

In each of these presentations the goal will be named **Theorem** if the proof is complete. Otherwise it is displayed as **Conjecture**. The user may move through the lines using the commands **set\_pos**, **up**, **d** described in Section 6. The command **last** takes him to the first line that has not been proved yet. The main tool of the user is the insertion of lines containing new formulas by the command **ins(Formula)** at the current position. These formulas get the status **untried**. Then they are automatically passed to the background system to be proved from a theory that can be set in the *ilf\_state* **pad\_default\_theory**. If the background started working on the line, its status is changed to **tried** and can be changed later on by the background to **proved**, **unproved** or **unprovable**. **del** deletes the current line. The status of all lines that have been proved using the deleted line directly is changed to **untried**.

If the background is not able to prove the formula, the user can

- insert further lines or
- modify the theory to be used by the command use(Theory) or
- extend the theory by the command use\_also(Theory)

Here Theory can be either the name of a theory or an axiom or a list of such names. Moreover, Theory can contain numbers of lines to be used, provided they occur before the current line. pad\_use\_always(Theory) specifies a theory that will always be added to the theories given to prove the lines on the *ProofPad*. Usually,

this is applied to ensure that frequently needed axioms like the basic axioms of equality or of an ordering are not omitted.

The deductive system algebra (cf. Section 8.2.5) provides tools to construct new proof lines automatically. From the *ProofPad* they are used by the commands ac\_move and distribute. These commands require parameters for the position of the subterms of the actual formula to be used. If they are called without parameters (e.g. from the pulldown menu of the *ProofPad*), the structure of the formula in the current line is displayed as a tree by the *TreeViewer* and the user can select the desired position with the right mouse button or he can display a subformula in the *TreeViewers* text window as a string and select a certain substring with the mouse. In the latter case, the position of the smallest subterm containing this substring is selected.

If an axiom is a Horn clause with a head matching the formula in the current line, the literals in the body can be automatically inserted as new lines in front of the current line by using the name of the axiom as a command. This mechanism is also used internally to connect the algebra system with the *ProofPad*. E.g. moving a subterm from Pos1 to Pos2 by ac\_move calls the procedure:

```
pos(P),problem(P,F,_),
```

/\* Getting the actual position and the contents of the current line (cf. section 6)\*/ alge(dist) reduces F to F1 by algebra(ac\_move\_rule(Pos1,Pos2)),

/\* Calling the algebra system (cf. section 3.1) with the rule of inference ac\_move\_rule. Note that F1 is a variable that will be instantiated by this call!\*/ alge(dist),

```
/* Applying the axiom alge(dist) just created */
```

```
forget_ax(alge(dist))
```

```
/* Forgetting this axiom */
```

Lines of a proof can be reordered by the command move\_line(Line1,Line2), which will move Line1 towards Line2 as far as possible without violating the correctness of the proof. move\_lines\_fd (move\_lines\_bd) moves all lines to the bottom (to the top, respectively) as far as possible. This can provide a better readability of the proof, especially when transformed to  $I\!AT_F\!X$  output.

The  $I\!AT_EX$  output uses the article style of  $I\!AT_EX$ . Author and title can be set by the *ilf\_states* pad\_author and pad\_title, respectively. All files making up the  $I\!AT_EX$  input reside in  $\{USERILFHOME\}/tmp$ . The files proof.tex contain the proof. The title is contained in the file title.inp.

For the IAT<sub>E</sub>X output, lines of equations or inequalities may be combined into a chain of equations or inequalities. These formulas are connected by the words "clearly", "hence", "therefore" and "by". "clearly" indicates that no other line in the proof has been used, "hence" means that just the formula immediately preceding the current formula has been used and "therefore" shows that just the number of immediately preceding formulas set in the *ilf\_state* pad\_recall have been used. All the other references are given explicitly. All axioms not belonging to one of the theories specified in the *ilf\_states* pad\_default\_theory and pad\_use\_always are explicitly mentioned at the places where they have been used. All formulas that are

added to the knowledge base at run time for further use with the *ProofPad* should be inserted in a theory specified in the *ilf\_state* pad\_reference. The default theory for this purpose is lemmata.

The *ProofPad* can be left by typing end. If a proof has been completed, the user has the possibility to write it into a  $IAT_EX$  input file that can be used in a larger manuscript. In order to do this, the formula that has been proved must have a name NAME, which must be a PROLOG atom. Then the files NAME.inp - a  $IAT_EX$  input file - and NAME.dep containing the relevant dependencies are created.

If the proof on the *ProofPad* is the last of a series of proofs of lemmata, a manuscript can be created. This is done in two steps. First, the command **outline** erases the *ProofPad* after saving the actual proof and builds a new proof by analyzing the dependencies in the files **\*.dep**. Each line of this new proof consists of one of the lemmata proved before. The lines can be arranged for the manuscript using the commands described above. Then the final manuscript containing all the proofs of the lemmata can be created by the command **make\_manuscript**.. It generates a file **manuscript.tex**.

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