Getting started with Maple 10

by Gilberto E. Urroz, July 2005

Maple 10 is the latest version of the mathematical (symbolic) software Maple. Information about Maple can be found at <u>http://www.maplesoft.com</u>.

Launching Maple 10

The location of the Maple 10 icon varies from computer to computer, particularly if using the computer labs on campus. For an individual Maple 10 server, you will find the Maple 10 icon at *Start>All Programs>Maple 10> Maple 10*. This will launch the preferred Maple 10 interface, as shown below.

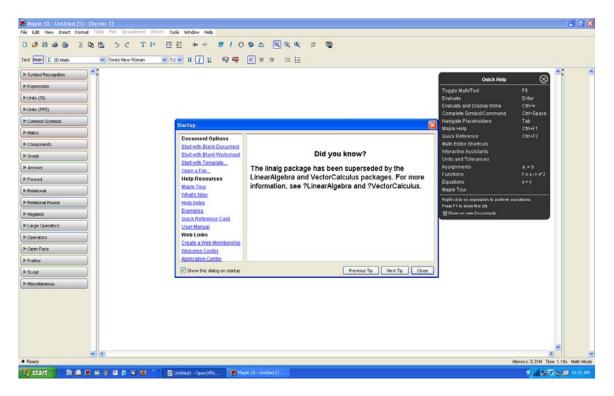


Figure 1. Maple 10 interface when first launched.

The Quick Help window

You will notice an informational window hovering over the interface. This window, labeled *Startup*, provides links for help on Maple, and a random tip on using Maple. Click this screen off, to get to the main Maple interface. In the upper right corner of the main Maple interface you will find a black-background window with a list of help references for using Maple. This *Quick Help* window is reproduced below.

The objective of the *Quick Help* window is to provide a quick reference to the most useful operations and concepts in Maple. If you had clicked off the *Quick Help* window, and would like to recover it, simply press the [F1] key in your keyboard.

Quick Help	\otimes	
Toggle Math/Text	F5	
Evaluate	Enter	
Evaluate and Display Inline	Ctrl+=	
Complete Symbol/Command	Ctrl+Space	
Navigate Placeholders	Tab	
Maple Help	Ctrl+F1	
Quick Reference	Ctrl+F2	
Math Editor Shortcuts		
Interactive Assistants		
Units and Tolerances		
Assignments	a := b	
Functions	f := x -> x^2	
Equations	х = у	
Maple Tour		
Right click on expression to perform operations.		
Press F1 to show this list.		
ᅜ Show on new Documents		

Figure 2. Maple's Quick Help window.

You can click on any of the lines in the *Quick Help* window to obtain a help window with detailed information on that particular operation. For example, for information on functions, click the line *Functions* $f:x \rightarrow x^2$ in the *Quick Help* window. This opens a Maple screen entitled *Maple 10 Help* – *[worksheet, help, QuickHelpDetails]*, which will show some information on how to define functions in Maple. This is illustrated in Figure 3, below. By scrolling the right-hand side window, notice that this *worksheet* contains detailed information on all the topics included in the *Quick Help* window.

Maple 10 Help directory tree

Also, notice that the detailed help worksheet contains a directory tree in the left-hand side with folders and documents. These are Maple help documents, and you can access them from this directory tree by double clicking on a document or folder. Notice that the directory tree shows a document entitled *Quick Help – Detailed Information* highlighted. This is the help document that you are currently reading. You can navigate the directory tree on the left hand side of this window to open other relevant help documents. For example, if you were interested in learning about the *Math Dictionary*, you would double click on that document in the directory tree. Thus, we have shown here how to access the Maple *Help* display through the use of the *Quick Help* window. Remember, to recover the *Quick Help* window, simply press [F1]. Alternatively, you can select *Help* > *Quick Help* in the Maple 10 menu bar.

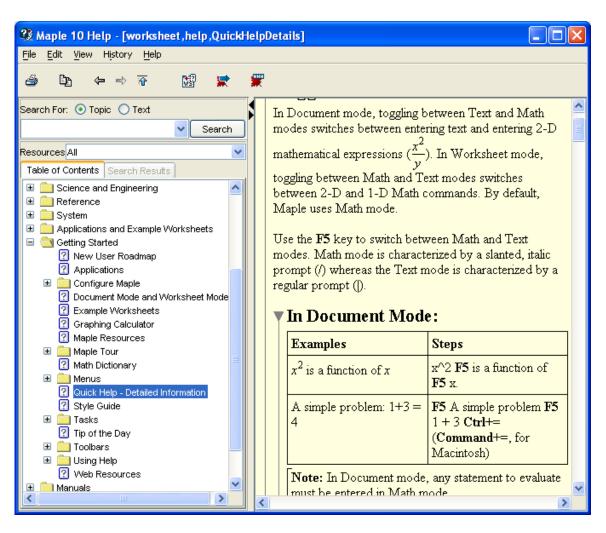


Figure 3 – Maple 10 Help window with *Quick Help* – *Detailed Information* document highlighted.

Using the Math Dictionary

The *Math Dictionary* is an alphabetical listing of quick references on mathematical concepts. The *Math Dictionary*, and other references, are available by selecting *Help> Manuals, Dictionary and more... > Dictionary* in the main Maple 10 interface. As an exercise, find information about the *Laplace Transform* by opening the dictionary and finding the listings under the letter *L*. You should get the information shown in the following figure.

As additional exercises on the use of the *Math Dictionary*, find the following entries: *circle of curvature, heat equation, Napierian logarithm, radian, Ramanujan, factor theorem, Babbage's engine, Bernoulli equation, beta function, Cartesian product, complex number, Laplace equation, normal distribution, quadratic equation, tesselation, translation, gamma function,* and *Klein bottle.*

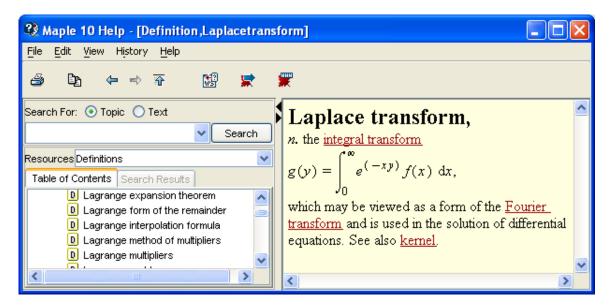


Figure 4 – Maple 10's Math Dictionary's entry on the Laplace Transform

Using Maple 10's Help

The Help item in the Maple 10's menu bar allows access to many other Help documents for Maple 10. The items available are shown in the figure below:

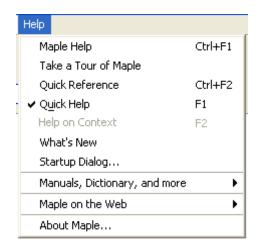


Figure 5 – Items in Maple 10's *Help* menu.

You are welcome to explore all the entries shown. The use of these entries is discussed briefly next:

- Maple Help (Cntl F1):
- Take a Tour of Maple:
- Quick Reference (Cntl F2):
- Quick Help (F1):
- Help on Context:
- What's New:
- Startup Dialog...:
- Manuals, Dictionary, and more:
- Maple on the Web:
- About Maple:

- Opens Maple's Help window
- Detailed tour of Maple a good start for new users
- F2): Worksheet summarizing basic Maple operation
 - Quick Help window (discussed above)
 - Help for specific context in a Maple 10 document
 - Highlights new features in Maple 10 version Launches *Startup* window (discussed above)
 - : Maple and math documents (see below)
 - Links to maplesoft's web sites
- About Maple:
- Version and other basic information

Manuals, Dictionary, and more

The item Manuals, Dictionary, and more shows the following items:

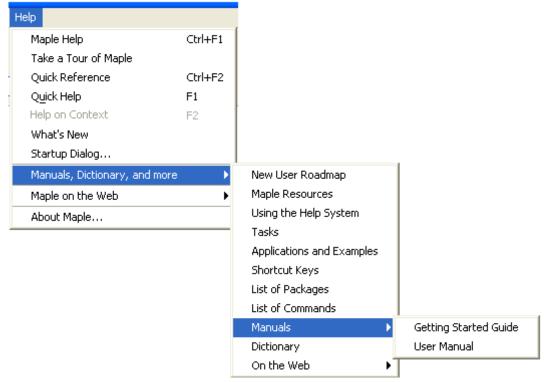
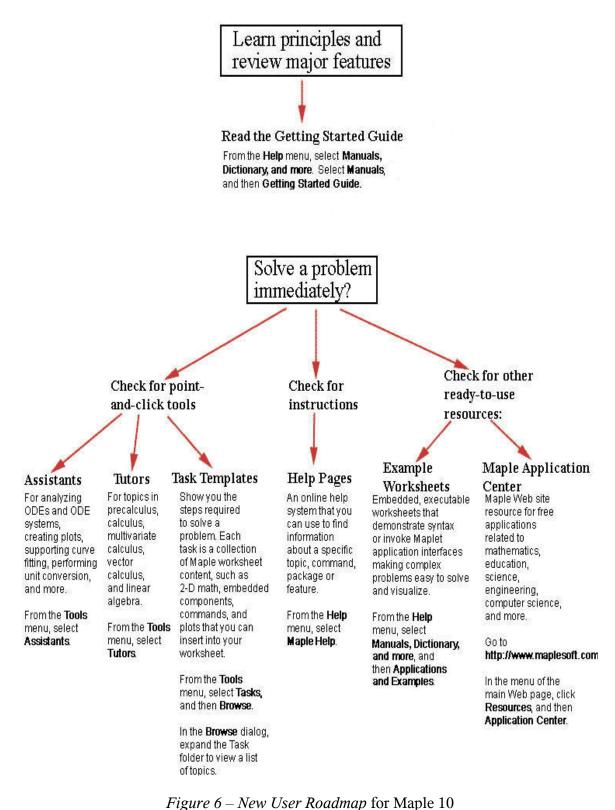


Figure 6 – Items in the Manuals, Dictionary, and more entry for Maple 10's Help menu.

<u>New User Roadmap</u>

Out of the items shown in Figure 6 for the *Manuals, Dictionary, and more* entry, the first one is the *New User Roadmap*. This document is a diagram of suggested resources for using Maple 10 relevant to the user's objective. The *New User Roadmap* is shown next.



Maple Resources

This item in the *Manuals, Dictionary, and more* entry for Maple 10's *Help* menu opens up a worksheet with additional links to Maple references and resources. It even repeats some of the other items listed under *Manuals, Dictionary, and more*. The items listed for this entry are:

- Tour and New User Roadmap
- Tutors, Assistants, and Task Templates, and Maple Calculator
- Online Help and Examples
- Palettes and Context Menus
- Manuals
- Web Resources

Click on the corresponding links in the *Maple Resources* worksheet to open the corresponding references.

Using the Help System

This item in the *Manuals, Dictionary, and more* entry for Maple 10's *Help* menu opens up a worksheet with additional links to specific instructions on using Maple's *Help* facilities. Click the various links to learn more about searching the *Help* facilities, etc. The following are some of the links available in this worksheet:

Finding Information

To learn about different ways of finding help topics, click the following links.

- Context Help
- Display a Known Help Topic
- Display Tool Tips
- Help Navigator
- Perform a Search
- Search Topic Index
- Review Help History
- Table of Contents

Help Menus and Toolbars

For descriptions of the menus, menu items, and toolbar buttons displayed when viewing Maple help pages, click the following links.

- Overview of Help Menu
- Overview of Help System Menu Bar
- Help Toolbar
- Status Bar

Tasks

This entry describes Maple *tasks*. Typically, these are worksheets that perform a specific set of operations, and to which one can attach a *Help* facility entry.

Applications and Examples

This item opens a worksheet with links to examples of Maple applications.

Shortcut keys

This item produces a list of most commonly used shortcut keys. Here is the listing of the shortcuts for the Windows version of Maple 10:

Shortcut Keys	Function .	
Ctrl Crosse	Complete Commend	
Ctrl + Space	Complete Command	
Home	Cursor to Start of Line	
End	Cursor to End of Line	
Ctrl + Home	Cursor to Top of Worksheet	
Ctrl + End	Cursor to Bottom of Worksheet	
Ctrl + Down Arrow	Move to Bottom of Execution Group	
Ctrl + Up Arrow	Move to Top of Execution Group	
Shift + Enter	Soft New Line	
Alt + Shift + F6	Cycle through Open Maple Windows	
For a list of math editing shortcut keys, see 2-D Math Shortcut Keys and Hints.		

The following is a list of menu accelerators.

Shortcut Keys	Function .
Alt + F	Open File Menu
Alt + E	Open Edit Menu
Alt + V	Open View Menu
Alt + I	Open Insert Menu
Alt + R	Open Format Menu
Alt + T	Open Tools Menu
Alt + W	Open Window Menu
Alt + H	Open Help Menu
Alt + F + D	Send Email with attached worksheet
Alt + F + M	Recent Documents Menu
Ctrl + N	New Document/Worksheet (based on Options setting)
Ctrl + O	Open Worksheet
Ctrl + F4	Close Current Worksheet
Ctrl + S	Save Worksheet
Ctrl + P	Print Worksheet
Ctrl + Shift + P	Page Setup
Alt + F4	Exit Maple
Ctrl + Z	Undo
Ctrl + Y	Redo
Ctrl + X	Cut Selection to Clipboard
Ctrl + C	Copy Selection to Clipboard
Ctrl + V	Paste Selection from Clipboard

Ctrl + Delete	Delete a line	
Ctrl + A	Select All	
Ctrl + F	Find/Replace	
F5	Switch between Text and Math mode	
F3	Split Execution Groups	
F4	Join Execution Group	
(To split/join with the previo	bus execution group, place the cursor at the start of the Maple	
input.)		
- /	execution group, place the cursor at the end of the Maple in	
put.)		
Shift + F3	Split Sections	
Shift + F4	Join Sections	
Enter	Evaluate Expression	
Ctrl + =	Evaluate and Display	
	1 5	
Ctrl + 0	Zoom Factor50%	
Ctrl + 1	Zoom Factor75%	
Ctrl + 2	Zoom Factor100%	
Ctrl + 3	Zoom Factor150%	
Ctrl+4	Zoom Factor200%	
Ctrl + 5	Zoom Factor300%	
Ctrl + 6	Zoom Factor400%	
F9	Show Region Ranges	
Shift + F9	Show Section Ranges	
Ctrl + T	Text Input Mode	
Ctrl + M	Maple Input Mode	
Ctrl + R	2-D Math Mode	
Ctrl + L	Label Mode	
Ctrl + Enter	Insert Page Break	
Ctrl + J	Insert Execution Group After Cursor	
Ctrl + K	Insert Execution Group Before Cursor	
Shift + Ctrl + J	Insert Paragraph After	
Shift + Ctrl + K	Insert Paragraph Before	
Ctrl + B	Bold Style Attribute (text or Maple input)	
Ctrl + I	Italic Style Attribute (text or Maple input)	
Ctrl + U	Underline (text or Maple input)	
Ctrl + .	Enclose Section in Subsection (Indent)	
Ctrl+,	Remove Section Enclosing Selection (Outdent)	
F7	Spellcheck	
Ctrl + Space	Complete Command	
F1	Quick Help Pop-up Menu	
F2	Context-sensitive Help	
Ctrl + F1	Help Table of Contents	
Ctrl + F2	Maple Quick Reference Card	

Ctrl + Shift + 1	Sketch Pencil
Ctrl + Shift + 2	Sketch Highlighter
Ctrl + Shift + 3	Sketch Eraser
Ctrl + Shift + 4	Sketch Selection

List of Packages

This item opens a worksheet with a listing of all Maple 10 function *packages*. A packages is a collection of related functions which can be loaded at once with the command *with*.

List of Commands

This item opens a worksheet with a listing of all Maple 10 top level commands. These are the commands available right away, as soon as Maple is started. Commands in packages need to be called by referring to the package name, or by loading the package first with the command *with*. For example, to produce an implicit plot of an equation in two-dimensions, we can write:

plots[implicitplot]($x^2+y^2-25 = 0$, x = -10 .. 10, y = -10 .. 10);

or, alternatively,

with(plots): implicitplot(x²+y²-25 = 0, x = -10 .. 10, y = -10 .. 10);

Manuals

This item contains two entries:

- Getting Started Guide
- User's Manual

Select one of these items to open the corresponding manual. These are the official Maple 10 manuals in worksheet format. (These manuals are provided in printed form with each copy of Maple 10).

On the Web

These entries require an Internet connection and provide additional Maple 10 resources on line. Check the different entries for details.

Maple Tour

The *Maple Tour* is a good way to get initiated with Maple 10. To activate the tour, use *Help > Take a Tour of Maple*. The resulting worksheet has links to worksheets illustrating the following issues in Maple:

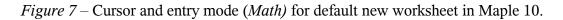
A quick tour of Maple
Basic calculations in Maple
Matrix and linear algebra
Ordinary and partial differential equations
E.g., Bessel, Airy, etc.
Finding maxima and minima with constraints
Probability and statistical applications
Program in Maple, translate to C, Java, etc.
(discussed earlier)
Using units and quantities with tolerances
Use Maple for student assessment
Easy connection to other programs
GUIs for Maple, and online deployment

For basic mathematics and engineering applications I suggest you cover at least items 1 through 4 in this list. Item 5 is applicable to advanced problems in differential equations. Item 6 is useful for optimization applications. Item 7 is needed for a course on probability and statistics. Item 8 will be necessary for writing Maple procedures. Item 9 is an excellent reference for most mathematics and engineering applications. Item 10 can be applied to laboratory physical measurements for error analysis. Items 11 is most useful to instructors to develop online-type of assessment activities. Item 12 is for advanced applications linking Maple to C, FORTRAN, or Java programs. Maplets, in Item 13, are graphic user interfaces (GUI) for Maple applications, while MapleNet is a service provided by *maplesoft* to post Maple applications online.

Creating a new worksheet

To create a new worksheet use File > New > Document mode.. or simply press Cntl+n. This will create an empty worksheet in *document mode*. In this mode, the cursor at the top of the worksheet is an italic forward slash (/) and the entry mode is *Math*. The upper left corner of the Maple worksheet will look like this:

Text Math C 2D Math	Times New Roman	✓ 12 ✓
Symbol Recognition		



Math *entry mode*

In this entry mode one can type a mathematical expression or a Maple command. An example of a Maple command to try would be:

Type it as shown above. However, be aware that in *Math* input, Maple will change the asterisks (*) into dots (·), so that the entry line will actually look as:

$$plot3d((x - y) \cdot (x + y) - 2 \cdot (x + 2 \cdot y), x = -2..2, y = -2..2, axes = boxed)$$

Press [Enter] after typing this command to get a plot of the function used as first argument of function *plot3d*. The arguments x = -2..2 and y = -2..2 represent the ranges of values of *x* and *y*, respectively, to be used in the production of the graph. The last argument, *axes* = *boxed*, indicates that the three-dimensional space where the graphic will be produced will be contained within a coordinate box showing the *x*, *y*, and *z* axes in the edges. The result is the following graph:

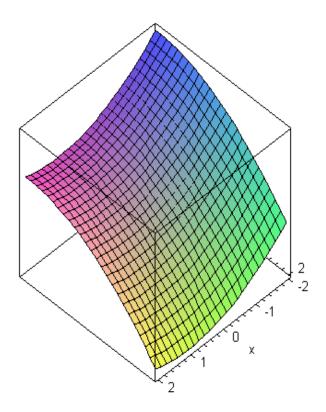


Figure 8 – Graph produced with the *plot3d* command shown above.

Math entry can be used to enter simple arithmetic expressions, for example, click below the graph obtained earlier and type:

$$sq$$
Cntl+Space (click on *sqrt*, the square root symbol)
(2+3/5+2/3
right-arrow key, twice [→][→]
)

The resulting Maple input is the quantity with the square root in the left-hand side of the screen, while the output is the quantity shown in blue in the middle of the screen. To the right-hand side of the screen Maple generates an automatic label, (1), to identify the output. The section of the Maple screen showing the input, output, and label is shown next:

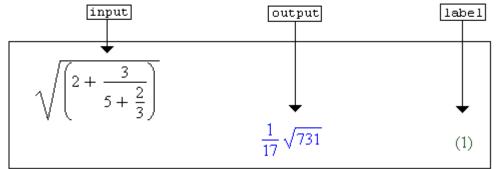


Figure 9 – Example of an arithmetic expression in *Math* entry form, showing input, output, and label.

Before continuing with more exercises in the Maple worksheet, we'll describe the buttons palette located at the top of the Maple interface.

Maple tool bar

The following figure shows the top of the Maple interface including the *menu bar* and the *tool bar*. While in your computer the menu bar and tool bar occupy the top of the interface, they're shown split in two parts in Figure 10 in order to fit the page width. Also, the 36 buttons in the tool bar have been labeled with numbers (1-36) to identify their function in the description below.

Buttons 1 through 8 correspond to typical operations that apply to almost any software, i.e., *1-new file*, *2-open a file*, *3-save file*, *4-print*, *5-print preview*, *6-cut selection*, *7-copy selection to clipboard*, and *8-paste clipboard contents*. As with many software applications, hovering the cursor over each button will provide an information balloon with the button operation.

<u>File E</u> dit <u>V</u> iew	Insert Forma	t T <u>a</u> ble <u>P</u> lot	Spreadsheet	Sketch <u>T</u> ools	\leftarrow menu bar
1 2 3 4	56 Abril 2	789 Da 🕰 ኃ		12 13 14 > F	
	an de			· · · ·	← toolbar
Text Math C 2D) Output	V Time	s New Roman	💙 12 💙	(coomar
					1
Window Help	17 10 10	20 04 2	2 23 24	25 26	← menu bar
15 16 ⇐ ➡	17 18 19	20 21 2		25 26 🔁 😰	
27 28 29	30 31	32 33 34	35 36	- -	\leftarrow toolbar
BIU	📭 📭	≣ ≣ ∃	$\stackrel{1}{\equiv} \stackrel{1}{\stackrel{2}{\equiv}}$		

Figure 10 – Menu bar and tool bar in a Maple 10 interface.

The operation of the remaining buttons in the *tool bar* is listed next by using the identifying numbers shown in Figure 10:

- 9 Undo last operation
- 10 Redo last undone operation
- 11 Insert text
- 12 Insert Maple input
- 13 Enclose selection into a section or
- *subsection* (see the *Insert* menu)
- 14 Remove section or subsection enclosing selection
- *15 Move back to previous worksheet*
- *16 Move forward to next worksheet*
- *17 Execute entire worksheet*
- *18 Execute selection*
- 19 Stop execution of current operation
- *20 Debug current operation* (useful in

programming)

21 – Restart Maple server (clears Maple

memory)

- 22 Zoom to 100%
- 23 Zoom to 150%
- 24 Zoom to 200%
- 25 Toggle entry of tab characters with tab
- 26 Open help system
- 27 Bold characters
- 28 Italics characters
- *29 Underlined characters*
- *30 Change font color in characters*
- 31 Change background color in selection
- *32–Align to the left*
- 33 Center characters
- *34 Align to the right*
- *35 Bulleted list*
- *36 Numbered list*

All of the button operations are available under the different menus, e.g., buttons 9 and 10 (undo, redo) are also available in the *Edit* menu. So, the tool bar facilitate performing a good number of operations by a single click. Become familiar with all the buttons in the tool bar to use Maple more efficiently.

Maple palettes

Maple offers a number of palettes listed on the left-hand side of the interface as shown in the figure below.

Symbol Recognition
► Expression
►Units (SI)
►Units (FPS)
Common Symbols
Matrix
▶ Components
FGreek
Arrows
Fenced
▶ Relational
▶ Relational Round
►Negated
►Large Operators
▶ Operators
▶ Open Face
▶ Fraktur
▶ Script
Miscellaneous

Figure 11 – Collection of Maple 10's palettes.

Each palette is opened by clicking on the arrow attached to its name. For example, the *Expression* palette shows a collection of mathematical operations including integrals, summations, products, derivatives, partial derivatives, limits, powers, sub-indices, square root, *n*-th root, factorials, absolute value, exponential function, natural logarithm, base-10 logarithm, base-*b* logarithm, trigonometric functions, combinations (binomial coefficient), function references for one or two variables, mapping definition of a function of one or two variables, evaluation of a function at a point, and multiple-valued functions.

Expression
$$\int f \, dx \, \int_{a}^{b} f \, dx \, \sum_{i=k}^{n} f$$

$$\prod_{i=k}^{n} f \, \frac{d}{dx} \, f \, \frac{\partial}{\partial x} \, f$$

$$\lim_{x \to a} f \, a^{b} \, a_{n}$$

$$\sqrt{a} \, \sqrt[n]{a} \, a!$$

$$|a| \, e^{a} \, \ln(a)$$

$$\log_{10}(a) \, \log_{b}(a)$$

$$\sin(a) \, \cos(a) \, \tan(a)$$

$$\binom{a}{b} \, f(a) \, f(a, b)$$

$$f := x \to y$$

$$f := (xl, x2) \to y$$

$$f(x) \Big|_{x=a}$$

$$\binom{-x \, x < 0}{x \, x > 0}$$

Figure 12 – Components of the Expression palette.

Typing mathematical expressions in *Math* entry mode

The *Expression* palette can be used to build mathematical expressions. For example, click under the last expression in your worksheet and use the summation symbol in the *Expression* palette to create the following summation:

$$\sum_{r=1}^{\infty} \frac{1}{r^2}$$

Here are the step-by-step instructions to build this expression:

- Click on the summation symbol in the *Expression* palette (the *i* in the lower side of the symbol will be highlighted)
- Type *r*
- Press the *tab* key in your keyboard (moves cursor from one entry point to the next)
- Type 1
- Press tab
- Click on the infinity symbol (∞) from the *Common Symbols* palette (the *f* will be highlighted now)
- Type 1 / r ^ 2

At this point, the expression is complete. We can do a couple of things with it: (1) highlight it, and use Edit > Copy (or Cntl+C) to copy it to the clipboard and, then, paste it into, say, a *Word* file (in this case we would have used Maple as an equation editor); or, (2) press [Enter] to calculate the expression. Press [Enter] to calculate the expression. The result should be as follows:

$$\sum_{r=1}^{\infty} \frac{1}{r^2}$$

$$\frac{1}{6} \pi^2$$
(2)

Figure 13 - Example of algebraic operation in Math entry mode in Maple 10.

Notice that, as in the case of the arithmetic expression used earlier, we have an input (lefthand side), and output (center), and an automatic label (right-hand side).

Context menus

Context menus are menus that are available to operate on Maple inputs and/or outputs. The items in the context menus are selected automatically by Maple and contain only operations that are relevant to the expression selected. These menus are activated by clicking on the input or output expression (sometimes, the whole expression must be highlighted) and then doing a *right-click* with the computer mouse.

As an example, go back to the input algebraic expression used earlier (the one with the square root), and click somewhere inside it. Then, do a *right-click* with the mouse. The context menu that you get will look like the following figure. Among the operations available, we could try, for example the option *Approximate*. This operation produces a floating-point result for the symbolic operation under the square root. Clicking on the *Approximate* item produces a sub-menu with the options *5*, *10*, *20*, *50*, *100*. These numbers indicate the number of digits in the approximate (floating-point result).

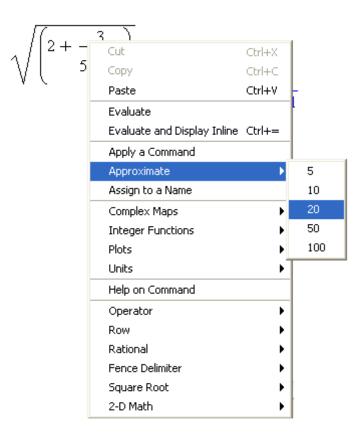


Figure 14 – Context menu for an arithmetic operation.

For the case under consideration, using 10 digits, for example, will produce the result:

$$\sqrt{\left(2 + \frac{3}{5 + \frac{2}{3}}\right)} \to 1.590412451$$

$$\frac{1}{17}\sqrt{731}$$
(1)

Notice that the use of the context menu produced an arrow (indicating an operation was performed) followed by the floating-point result. Thus, context menu items do not document their operation very well in a Maple worksheet. Added comments by the user can help interpret the results for any potential reader of their worksheets if context menus are used. The use of text to document Maple 10's worksheets is shown later. Next, we'll try using the *Approximate* context-menu item but selecting the output of the square-root operation rather than the input.

Going back to your worksheet, click on the output for the square-root operation, namely, on the term

$$\frac{1}{17}\sqrt{731}$$

Then, use the context menu (*right-click*) to calculate an approximation with 20 digits:

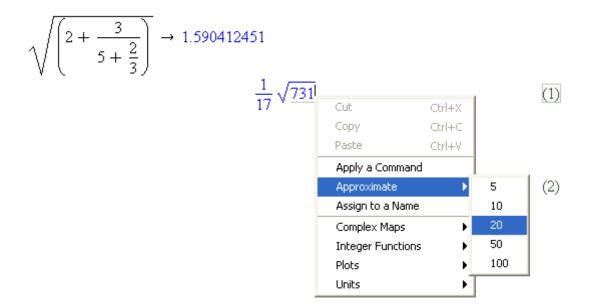


Figure 15 – Using context menu to approximate a symbolic result using the output of a Maple operation.

The results is shown next:

$$\sqrt{\left(2 + \frac{3}{5 + \frac{2}{3}}\right)} \to 1.590412451$$

$$\frac{1}{17}\sqrt{731}$$
(1)
$$\rightarrow 1.5904124511289146572$$

Notice that the arrow indicating the operation is shown now below the output. Obviously, for documentation purposes, we need to add some text to the worksheet.

Adding text to a worksheet

To add text to a worksheet, click in the location where you want to add the text, then, press [F5] to toggle the input format from *Math* to *Text*. Type the desired text in that location. Select another location to insert more text, then repeat the steps indicated

above. For example, by inserting text around the previous calculation we can re-write this piece of the worksheet as follows: (Note: The text input cursor is a vertical line. When a text input is requested, the left part of the toolbar will show the *Text* box highlighted. Also, we used *backspace* to remove the arrows from the worksheet).

The square root
$$\sqrt{\left(2+\frac{3}{5+\frac{2}{3}}\right)}$$
 is approximated by 1.590412451, using 10 digits.
The output of the square root, shown as expression (1), below, is
 $\frac{1}{17}\sqrt{731}$ (1)
and this value is approximated as 1.5904124511289146572, using 20 digits.

*Figure 16 – A*rithmetic calculation edited by inserting text in a Maple worksheet (frame added for emphasis, it cannot be produced in Maple).

Context menus for algebraic expressions

Try some context menu operations with algebraic expressions.

<u>Example 1</u>

Click in a location of your worksheet below the last operation listed there, and type the expression (Note: Use [F5] to toggle to *Math* input if a text cursor shows up):

$$x^2 + 3x^2 + 25$$

Type x ^ 2 [\rightarrow] + 3 x + 25. Then, before pressing [Enter], do a *right-click* to obtain the corresponding context menu. From this context menu, we'll try the following applications:

• Evaluate at a point - This option generates the following dialog box:

🖁 Evaluate at a Point 🛛 🔀
Evaluate the expression at the point:
× 🕶 = 1.5
OK Cancel

Figure 17 – Dialog box for context-menu *Evaluate at a Point* operation.

Replace the value of *x* with 2.5, and press [OK] to get:

$$x^2 + 3x + 25 \rightarrow 38.75$$

• Differentiate

Next, highlight the original expression, namely, $x^2 + 3x + 25$, and, do a copy (*Cntl-C*). Click on a location below the current one, and do a paste (*Cntl-V*), to make an extra copy of the original expression. Then, using a context menu (*right-click*), select the option *differentiate* > *x*, to produce:

$$x^2 + 3x + 25 \rightarrow 2x + 3$$

Control-drag

Highlight the original expression, namely, $x^2 + 3x + 25$, cut it and paste it below the last result in your worksheet. This time, do press [Enter] to produce a Maple output. Next, highlight the output, and, pressing [Cntl], drag the cursor to a new location below to its original location in the worksheet. After a couple of seconds, a copy of the output will appear as Maple input at the location where you released the mouse button.

Integrate

Next, using a context menu (*right-click*), select the option *integrate* > *x*, to produce:

$$x^{2} + 3x + 25 \rightarrow \frac{1}{3}x^{3} + \frac{3}{2}x^{2} + 25x$$

<u>Exercise 1</u>

Using procedures similar to those detailed above for the context-menu operations *Evaluate at a point, differentiate,* and *integrate,* and for the same polynomial shown above, try the following context-menu operations:

- 1. Complete square
- 2. Solve (solve the equation formed by the expression = 0)
- 3. Coefficients > x
- 4. Constructions > Definite Integral > x (Lower Limit = 0, Upper Limit = 1)
- 5. Constructions > Derivative > x
- 6. Constructions > Evaluate at > x (at 1)
- 7. Constructions > Limit > x (at 0)
- 8. Constructions > Product > x (Lower Limit = 1, Upper Limit = 10)
- 9. Constructions > Sum > x (Lower Limit = 1, Upper Limit = 10)
- 10. Conversions > Horner Form > x
- 11.Conversions > To String
- 12.Integral Transforms > Fourier Transforms

Exercise 2 Enter the following rational fraction as Maple input:

$$\frac{x^3 - x^2 - x + 10}{x^2 - 4}$$

Using context menus, try the following operations in Maple 10:

- 1. Evaluate at a point
- 2. Factor
- 3. Normal
- 4. Solve (solve the equation formed by the expression = 0)
- 5. Numerator
- 6. Denominator
- 7. Constructions > Definite Integral > x (Lower Limit = 0, Upper Limit = 1)
- 8. Constructions > Derivative > x
- 9. Constructions > Evaluate at > x (at 1)
- 10.Constructions > Limit > x (at 0)
- 11.Constructions > Product > x (Lower Limit = 1, Upper Limit = 10)
- 12.Constructions > Sum > x (Lower Limit = 1, Upper Limit = 10)
- 13.Conversions > Partial fractions > x
- 14.Conversions > To String
- 15.Integral Transforms > Fourier Transforms

<u>Exercise 3</u>

Enter the following trigonometric polynomial as Maple input:

 $\sin(x) + \cos(2 \cdot x) + \sin^2(x)$

Using context menus, try the following operations in Maple 10:

- 1. Evaluate at a point
- 2. Factor
- 3. Solve numerically (solve the equation formed by the expression = 0)
- 4. Constructions > Definite Integral > x (Lower Limit = 0, Upper Limit = 1)
- 5. Constructions > Derivative > x
- 6. Constructions > Evaluate at > x (at 1)
- 7. Constructions > Limit > x (at 0)
- 8. Constructions > Product > x (Lower Limit = 1, Upper Limit = 10)
- 9. Constructions > Sum > x (Lower Limit = 1, Upper Limit = 10)

Title, sections and sub-sections

When preparing a well-documented worksheet, we may want to give the worksheet a title, and introduce sections and sub-sections into the worksheet. These items would allows us to organize subjects in a reasonable fashion. For example, if we're writing a worksheet about polynomials and fractions, we could type a title *Polynomials and Fractions*, and, then, insert a section called *Polynomials* and one called *Fractions*.

To do this exercise, create a new worksheet. Then, to enter a title, click at the top of the worksheet. Use [F5] to ensure you're in text mode, and select *P Title* from the input/output descriptor located in the toolbar. Type the title. For this example, the top of the worksheet may look as follows:

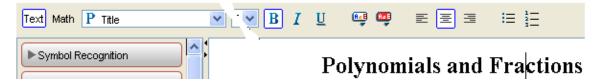


Figure 18 – Typing a title in a worksheet.

To insert sections use *Insert*>Section (or use the *insert section* button – i.e., button number 13 in Figure 10). The cursor will remain at the location of the section's title. Type *Polynomials*. Then, press return, press [F5] to toggle between *Math* and *Text* format, and type a few lines in your worksheet describing the section and introducing a polynomial $(x^3 + 2x^2 - 5x + 3)$ that will be used in the operations illustrated in the section. Then, we'll insert a couple of sub-sections (*Evaluate at a point* and *Integrate*), by using the *insert section* button. Copy the polynomial into them and evaluate the polynomial at x = 2, and integrate with respect to x. Document the operations.

Go back to the upper level of sections in the worksheet and insert a section to be called *Fractions* below the *Polynomials* section. Insert a few lines introducing the section, and define the fraction

$$\frac{x^3 - x^2 - x + 10}{x^2 - 4}$$

to be used in the sub-sections defined next. Within this section insert sub-sections entitled *Normal fractions* and *Numerator & Denominator*. Perform such calculations using context-menus and document the sessions with text.

You can insert as much documentation into your worksheet's sections and subsections as you wish in this exercise. One possible outcome of this exercise is shown in the following page.

Polynomials and Fractions

Polynomials

This is a simple polynomial: $x^3 + 2x^2 - 5x + 3$ upon which we perform the following operations:

🔻 Evaluate at a point

We use a contex menu to evaluate this polynomial at x = 2

$$x^3 + 2x^2 - 5x + 3 \to 9$$

▼Integrate

We use context menu again to calculate the indefinite integral of the polynomial

 $x^{3} + 2x^{2} - 5x + 3 \rightarrow \frac{1}{4}x^{4} + \frac{2}{3}x^{3} - \frac{5}{2}x^{2} + 3x$

Fractions Use the fraction $\frac{x^3 - x^2 - x + 10}{x^2 - 4}$ in the following sub-sections:; Normal fraction Using the Normal operation from the context menu $\frac{x^3 - x^2 - x + 10}{x^2 - 4} \rightarrow \frac{x^2 - 3x + 5}{x - 2}$ Numerator Using functions Numerator in the context menu $\frac{x^3 - x^2 - x + 10}{x^2 - 4} \rightarrow x^3 - x^2 - x + 10$

Figure 19 – Example of a worksheet with a title, sections, and sub-sections.

Note: Click on the arrow defining each section of sub-section to open or close that section or sub-section. Use *View>Expand All Sections* or *View>Collapse All Sections* to manipulate all sections and sub-sections at once.

Using Tables

A table can be inserted in a Maple worksheet to organize data or to organize examples in the worksheet. Let's try an exercise using tables. Open a new worksheet (*Cntl* + *n*), and type the title *Examples of ordinary differential equations*, and press enter. To insert the table, use *Insert* > *Table* to produce the following dialog.

Insert Table 🛛 🛛 🛛	
Rows	3
Columns	2
<u>о</u> к	<u>C</u> ancel

Figure 20 – Dialog box for *Insert* > *Table*

Select the default values, namely, 3 rows, 2 columns, and press OK. As a result, you will get a blank table with 3 rows and 2 columns. In the first row and first column cell type the following text: *Example 1 – First order, linear, homogeneous*. In the first row, second column enter the differential equation:

$$x'(t) + x(t) = 0.$$

Click on the equation and generate a context menu (*right-shift click*), and select the item *Solve DE* > x(t) to obtain a symbolic solution for the equation.

In the second row, first column type the text: *Example 2 – Second order, linear, homogeneous*. In the second row, second column enter the differential equation

$$y''(t) + y'(t) + y(t) = 0$$

[Note: the double prime in this equation, y''(t), is typed as two apostrophes and not as a double-quote]. Click on the equation and use the context menu (*right-shift click*) to solve this second equation.

Finally, in the third row and first column, type the text: *Example 3 – Second order, linear, non-homogeneous*. In the third row, second column type the equation:

$$s''(x) + s(x) = sin(x),$$

which you will solve using the context menu. When done, the spreadsheet should look somewhat like Figure 21.

Examples of ordinary differential equations

Example 1 - First order, linear, homogeneous	$x'(t) + x(t) = 0 \rightarrow x(t) = Cl e^{(-t)}$
Example 2 - Second order, linear, homogeneous	$y''(t) + y'(t) + y(t) = 0 \rightarrow$ $y(t) = _Cl e^{\left(-\frac{1}{2}t\right)} \sin\left(\frac{1}{2}\sqrt{3}t\right)$ $+ _C2 e^{\left(-\frac{1}{2}t\right)} \cos\left(\frac{1}{2}\sqrt{3}t\right)$
Example 3 - Second order, linear, non- homogeneous	$s''(x) + s(x) = sin(x) \rightarrow$ $s(x) = sin(x) _C2$ $+ cos(x) _Cl - \frac{1}{2} cos(x) \underline{x} $

Figure 21 – Example of a table in a Maple worksheet.

Using Common Symbols and Greek letters

Two of the most useful Maple palettes, besides the *Expression* palette, are the *Common Symbols* and *Greek* palettes. The contents of these two palettes are shown below.



Figure 22 – The Common Symbols and Greek Maple 10 palettes.

The Common Symbols palette includes such commonly used symbols such as:

- π The ratio of the length of a circle to its diameter
- e The basis for the natural logarithms
- i, j, I Unit imaginary numbers $(i^2 = j^2 = -1)$
- Infinity

It also includes the common mathematical symbols:

- Σ Summation
- П Product
- ∫ Integral
- \cup Union of sets
- \cap Intersection of sets

You will also find in this palette comparison symbols (e.g., >. <. etc.), symbols used in set theory (e.g., \in , \notin , \subseteq , \setminus , \emptyset), symbols for mathematical logic (\exists , \forall , \neg , \land , \lor , \Rightarrow), symbols for number sets (**C**, **R**, **N**, **Q**, **Z**), real and imaginary functions for complex numbers (\Re , \Im), arithmetic operations (+, -, \times , /), plus/minus signs (±), degrees (°), asterisk for products (*), dot product (•), regular product (·), the *del* or *nabla* operator for vector analysis (∇), factorial (!), aleph (\aleph), Planck's constant for quantum mechanics (\Box), etc.

These symbols can be very useful for editing equations for inclusion in texts or as input for Maple operations. As an example of equation editing using Maple, here are a couple of examples from vector analysis built using the *del* or *nabla* operator and the partial derivative symbol from the *Expression* palette:

$$\nabla f = \frac{\partial f}{\partial x} \quad \mathbf{i} + \frac{\partial f}{\partial y} \quad \mathbf{j} + \frac{\partial f}{\partial z} \quad \mathbf{k}$$

$$\nabla \cdot \boldsymbol{F} = \frac{\partial F_x}{\partial x} + \frac{\partial F_y}{\partial y} + \frac{\partial F_z}{\partial z}$$

Union and intersection of sets can be calculated using Maple as follows:

The *Common Symbols* palette is useful when inserting the base of the natural logarithms (e), which is a different symbol than the letter e. This difference is illustrated by the use of the *Approximate* > 5 operation in the context menus of the following two entries:

$$e^{2} + 5 \rightarrow e^{2} + 5.$$
$$e^{2} + 5 \rightarrow 12.389$$

In the first entry we typed the letter *e*, therefore, the *Approximate*>5 operation does not produce a floating point result (*e* is assumed to be an unassigned variable). In the second entry, the symbol e was inserted from the *Common Symbols* palette, producing the correct result when *Approximate*>5 was used.

The *Greek* palette contains the letters of the Greek alphabet, which are commonly used in mathematical expressions. The Greek alphabet is listed in the following table.

Lower case	Upper case	Letter name	English equivalent	Lower case	Upper case	Letter name	English equivalent
α	A	Alpha	а	V	N	Nu	n
β	В	Beta	b	ξ	Ξ	Xi	x
γ	Г	Gamma	g	0	0	Omicron	0
δ	Δ	Delta	d	π	П	Pi	p
ε	E	Epsilon	е	ρ	Р	Rho	r
ζ	Z	Zeta	Z	σ	$\boldsymbol{\varSigma}$	Sigma	S
η	H	Eta	h	τ	Т	Tau	t
θ	\varTheta	Theta	th	υ	Y	Upsilon	и
t	Ι	lota	i	ϕ	${\Phi}$	Phi	ph
К	K	Kappa	k	χ	X	Chi	ch
λ	Λ	Lambda	1	Ψ	Ψ	Psi	ps
μ	M	Mu	т	ω	${\it \Omega}$	Omega	0

Table 1 – The Greek Alphabet

The *Expression, Common Symbols,* and *Greek* palettes can be used to produce mathematical expressions for equation editing or as Maple entries, such as:

$$\boldsymbol{\varpi} = \sum_{k=1}^{n} \int_{0}^{t} (\xi + k \cdot \alpha \cdot \tau) d\tau$$
$$\boldsymbol{\varpi} = \xi t (n+1) + \frac{1}{4} \alpha t^{2} (n+1)^{2} - \frac{1}{4} (n+1) \alpha t^{2} - \xi t$$
(3)

Using sub-indices

To type sub-indices in mathematical expressions in Maple simply use Shift before typing the sub-index. It is necessary to press the right-arrow key to return to the main entry level in an expression. Sub-indices are used in both the numerator and denominator of the following expression:

$$\Omega = \frac{A_o \sin(\varpi t)}{\sqrt{(\varpi - \varpi_1)^2 + (\varpi - \varpi_2)^2}}$$

$$\Omega = \frac{A_o \sin(\varpi t)}{\sqrt{2 \, \varpi^2 - 2 \, \varpi \, \varpi_1 + \varpi_1^2 - 2 \, \varpi \, \varpi_2 + \varpi_2^2}}$$
(4)

Symbol recognition

The *Symbol Recognition* palette presents a sophisticated symbol recognition device that allows the user to sketch a mathematical symbol or a letter and provides the closest Maple characters that resemble the user's input. The user then can select the intended character to use in Maple. When you click on the *Symbol Recognition* you get the following form.

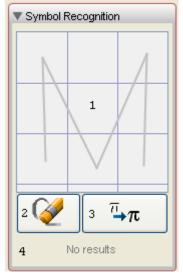


Figure 23 – Maple 10's Symbol Recognition form

The numbers shown in Figure 23 do not appear in the *Symbol Recognition* form and were added to identify the following components:

- 1. Sketch area: this is where the user sketches the intended symbol
- 2. Erase button: clears the sketch area
- 3. Apply button: press this button to allow Maple to recognize the symbol sketched
- 4. Output area: the area where Maple shows the possible symbols based on the sketch

If the symbol intended by the user is shown in the *output area*, the user can just click on the symbol to copy it into the Maple entry area. If the intended symbol is not included in the output area then the user can repeat the recognition attempt by pressing the *erase button* and sketching the symbol in the *sketch area* once more.

For example, the *approximate* symbol can be sketched as follows:

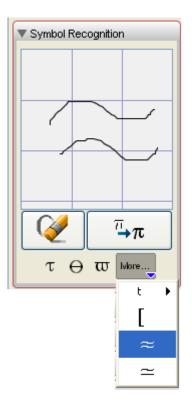


Figure 24 – An exercise in symbol recognition

Notice, however, that Maple suggested the symbols τ , θ , and ω as the first three choices in the symbol recognition operation. To obtain the *approximate* symbol it was necessary to look under the *More*... list as shown above. Clicking in the symbol copies it to the Maple entry location.

Other examples of symbol recognition are shown in the following page. In these examples I was trying to obtain the symbols α (alpha), γ (gamma), and the *del* or *nabla* operator symbol. Maple was successful in recognizing the intended character in each instance.

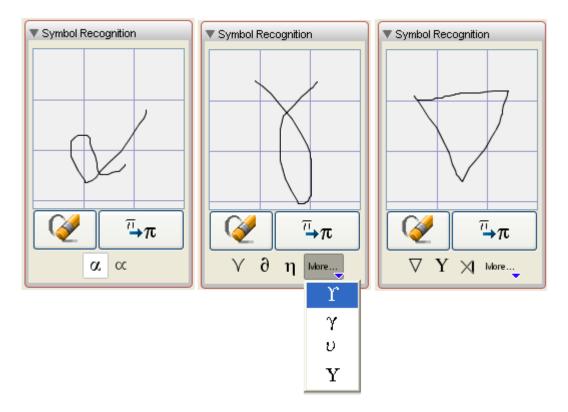


Figure 25 – Additional examples of Maple's character recognition feature.

Two-dimensional plotting with context menus

An expression (in either input or output in Maple) containing a single independent variable can be used to produce a plot in two dimensions through the use of context menus. For example, to plot the function $x = 2.5 e^{-t/10} cos(t/2 + 5)$, in the interval 0 < t < 20, we need only type the expression $2.5 e^{-t/10} cos(t/2 + 5)$ and select the *Plots*>2-*D Plot* item in the corresponding context menu.

By default, the *t* range is [-10,10]. By right-clicking on the plot itself you can generate a context menu for the plot where the *t* range can be changed. The item to use in the context menu is Axes > Range, as shown in Figure 26. This selection produces the dialog box shown in Figure 27. To adjust the *x* range, we select 0 to 20. The vertical range can be adjusted by selecting the range -2.5 to 2.5. The final version of the graph is shown in Figure 28.

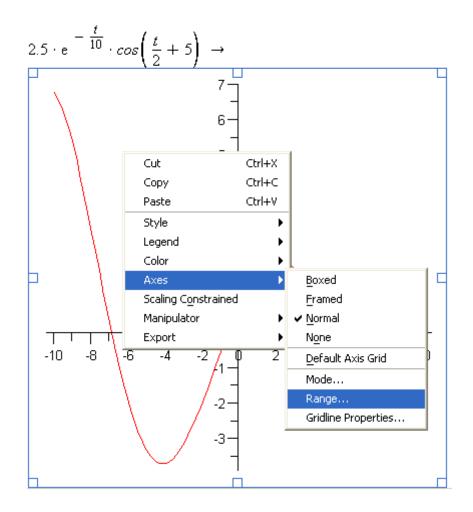


Figure 26 – Context menu for a two dimensional plot.

Axes Ranges						
гX						
0.0						
to						
20.0						
Y						
O Default						
• -2.5						
to						
2.5						
OK Cancel						

Figure 27 – Axes Ranges dialog box to adjust ranges in a two-dimensional plot.

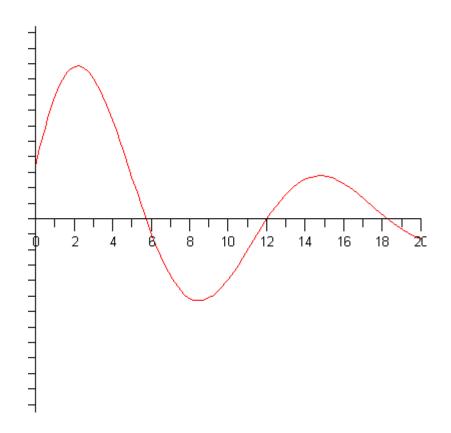


Figure 28 – Final version of the two-dimensional plot after adjusting axes ranges.

Two-dimensional plot manipulation

Having generated a two-dimensional plot through a context menu, we will now show how to manipulate such plot using the corresponding toolbar in the main Maple 10 window. First, one needs to click on the plot. This will produce a new row in the toolbar, as shown next.

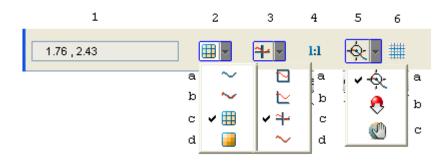


Figure 29 – Graphics toolbar for a two-dimensional plot

In order to describe the different components of the graphics toolbar we assign numbers to the different fields and menus and letters to the items in the drop-down menus. The description of the numbered components is as follows:

- 1. Coordinates of cursor on graph
- 2. Plot style

 (a)Line
 (b)Symbols (points)
 (c)Patch and grid (applies mainly to three-dimensional surfaces)
 (d)Patch but no grid (applies mainly to three-dimensional surfaces)

 3. Axes style
 - (a)Boxed
 - (b)Framed
 - (c)Normal axes
 - (d)No axes
- 4. Constrained scale button (1:1 scale when active)
- 5. Plot manipulator
 - (a)Point probe (determines coordinates of cursor location on graph)
 - (b)Scale (zooms in and out)
 - (c)Pan (moves graph about the plot frame)
- 6. Grid button (shows grid on plot area when active)

Click on the different menus or buttons and select different properties of the graph. For example, by selecting options 2(a), 3(a), and activating the 1:1 scale button, the graph of Figure 28 is now as shown in Figure 30. Figure 31 shows the same graph with a grid.

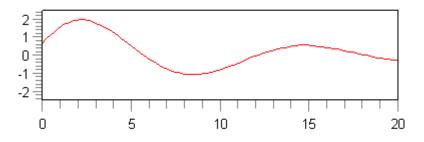
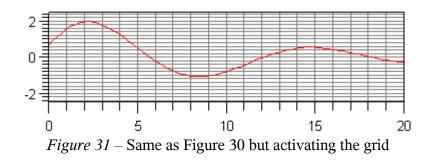


Figure 30 – Same as Figure 28 but using boxed axes and 1:1 scaling.



Getting Started with Maple 10 – Page 35

Two-dimensional animation with context menus

A Maple animation can be produced on a function of the form y = f(x,a) where the graph to be animated is y = f(x) and the animation parameter is *a*. For example, to produce an animation of the equation y = a + sin(ax), we need just type the expression a + sin(ax)and do a right-click on the expression to activate a context menu. Then, we select the item *Plots* > *Plot Builder* from the context menu, and select the *Animation* option in the box entitled *Select Plot Type*. We keep the selection 2-*D plot* in the box entitled *Select Plot* as well as the ranges -10 to 10 for the *x Axis*, and 0 to 10 for *Animation Parameter a* in the box entitled *Select Variable Purpose and Ranges*. Then, we press [Plot]. As a result we obtain a plot that shows no curves on it (this is so because the value a = 0produces no plot). In order to see the animation we need to click on the plot and check out the new animation toolbar.

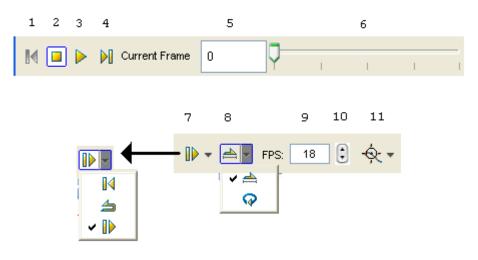


Figure 32 – Maple 10's animation toolbar

Figure 32 shows the Maple 10's animation toolbar, split in two parts to fit in the page. The items numbered in Figure 32 are described next:

- 1. Moves animation backward by one frame
- 2. Stops animation
- 3. Plays animation
- 4. Moves animation forward by one frame
- 5. Shows framed currently being shown in the graph area
- 6. Slider that shows the progress of the animation
- 7. Menu to select animation direction: backward, oscillating, and forward (default)
- 8. Menu to select animation type: single realization or continuous (repeated) animation
- 9. Shows the number of frames per second (FPS)
- 10.Slider to adjust the FPS value
- 11.Plot manipulator menu (same as discussed in Figure 29)

The reader is invited to run the animation using the different buttons and menus shown.

Three-dimensional surface plotting with context menus

A function of the form z = f(x,y) can be plotted as a surface in space. Consider the expression $x^2 sin(x) + y^2 cos(y)$. Type this expression in a Maple worksheet, click on the expression and do a *right-click* to generate a context menu. Select the item *Plots>3-D Plots>x,y* to see the following plot of a surface in three dimensions.

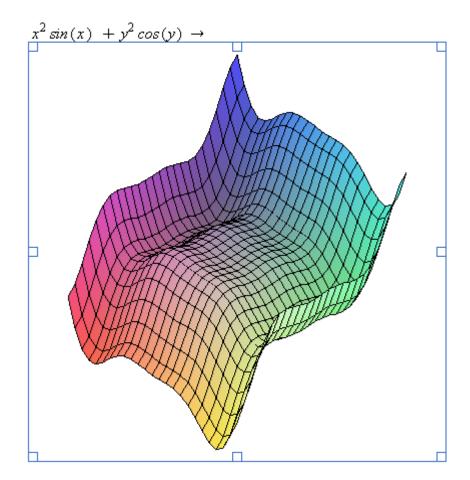


Figure 33 – Three-dimensional surface representing the function $x^2 sin(x) + y^2 cos(y)$.

When one clicks on the graph itself a new graphics toolbar is produced in the Maple interface as shown in the figure below. This toolbar include the following items:

- 1. Angle ϑ on *x*-*y* plane, measured from the positive *x* axis to plane of point of view
- 2. Angle φ measured from z axis on the line connecting the origin to the point of view
- 3. Surface style: (a) patch no grid; (b) patch and grid; (c) patch and contours; (d) contour lines only; (e) grid with hidden surfaces; (f) grid with no hidden surfaces; (g) points
- 4. Axes style: (a) boxed; (b) framed; (c) normal axes; (d) no axes
- 5. Axes scaling: 1:1 scaling if active
- 6. Plot manipulator: same as in two-dimensional plots (see Figure 29).

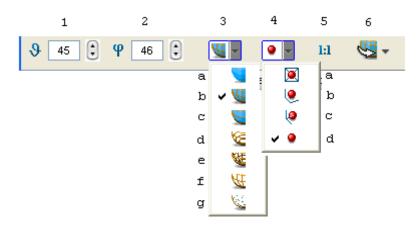


Figure 34 – Three-dimensional graph toolbar

By default, the plot manipulator is set to rotate (as shown above). To rotate the plot simply click on it, press the left mouse button, and drag in any direction. You will see the plot rotating in space. You will also notice that the values of the angles ϑ and φ change as the graph rotates since, for all practical purposes, we're changing the location of the point of view (i.e., that point in space from which the surface plot is being observed.

Many of the options available through the toolbar are also available through the context menu for the graph. Figure 35 shows some of the options available, in particularly the lightning scheme. Some of the options shown in Figure 35 are described next:

- Style: same as item 3 in Figure 34
- Color: changes the color(s) of the surface see Figure 36 for a list of options
- Lighting: changes illumination patterns on surface see Figure 35 for a list
- Axes: same as item 4 in Figure 34
- Scaling ..: same as button 5 in Figure 34
- Projection: scale plot manipulator -- same as option 5(b) in Figure 29
- Transparency: slider to select surface transparency (0 -- opaque to 1- transparent)
- Manipulator: same as item 6 in Figure 34 or item 5 in Figure 29
- Export: options for saving a Maple plot as a variety of graphics format files

The reader is invited to manipulate the different options available for three-dimensional surface plots in the context menu or in the toolbar.

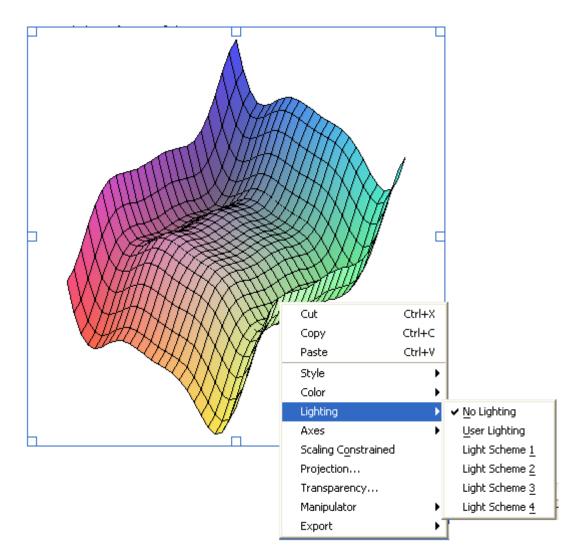


Figure 35 – Context menu for a three-dimensional surface plot, *Lighting* sub-menu highlighted.

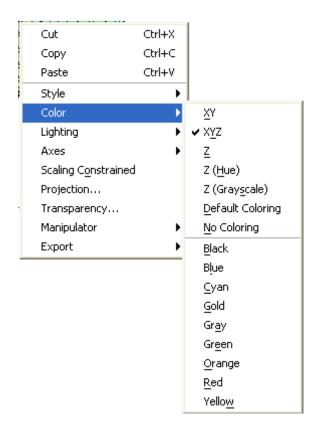


Figure 36 - Context menu for a three-dimensional surface plot, *Color* sub-menu highlighted.

Two-dimensional implicit plots with context menus

A function of the form f(x,y) = 0 or of the form g(x,y) = c can be used to generate an implicit plot in the *x*-*y* plane through context menus. Consider, the equation

$$\frac{x^2}{9} + \frac{y^2}{16} = 1$$

Type this equation in a Maple worksheet in *Math* entry mode. Click on the equation and generate a context menu for the same (*right-click*), then select the item Plots > 2-D *Implicit Plot*.

The result is a plot that looks like a circle. In order to see the true shape of the implicit plot we need to use a 1:1 scaling, which we can get by simply clicking on the plot area and using the [1:1] button in the toolbar. The resulting graph is an ellipse with semi-axes 3 in x and 4 in y, as shown next.

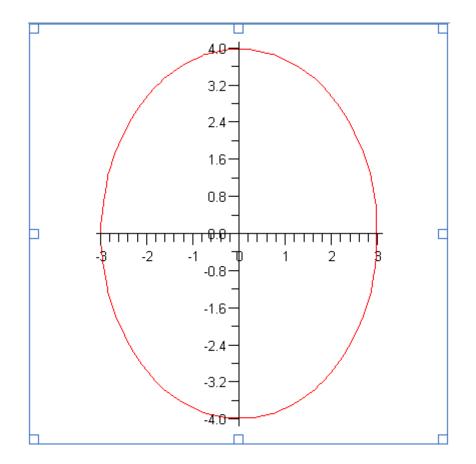


Figure 37 – An ellipse generated as a two-dimensional implicit plot.

Implicit plots can also be generated out of an expression of the form f(x,y). In such case, Maple will assume that the corresponding equation to be plotted is f(x,y) = 0. For example, using the expression $x^2 sin(x) + y^2 cos(y)$, which generated the surface plot of Figure 33, try to generate a two-dimensional implicit plot using a context menu. Select the option *Plots*>2-*D Implicit plot* > *x*,*y*.

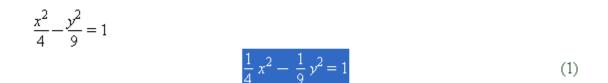
Drag-and-drop plotting

Once you have produced a plot (e.g., the ellipse of Figure 37), you can drag an expression or equation from a Maple output and drop it on top of the plot. Maple will automatically generate a new plot atop the existing one corresponding to the expression or equation dropped on the existing plot. For example, repeat the exercise leading to Figure 37. Then, type the equation

$$\frac{x^2}{4} - \frac{y^2}{9} = 1$$

and press [Enter].

The corresponding Maple worksheet, with the output highlighted, will look as follows:



Next, click on the highlighted output and drag it on top of the plot area for the ellipse of Figure 37 in your Maple worksheet. As a result Maple will add the implicit plot for the equation you just dropped on the plot area.

Legends in graphics

As an additional exercise, click on the plot and do a *right-click* to generate the corresponding context menu. Then, select the option *Legend* > *Edit Legend* to generate a dialog box corresponding to the legends (description) of each of the plots shown in the plot area. For "Legend for Curve 1" type "Ellipse" in the *Label* field of the dialog box (see Figure 39, below), then press [Done]. As a result, legends will be shown at the bottom of the plot in your Maple worksheet with the legend for the first curve being labeled "Ellipse" while that for the second curve the legend shows the label "Curve 2".

Legend Labels	Legend Labels
Curve Legend for Curve 1 🗸 Label Ellipse Done Cancel	Curve Legend for Curve 2 🗸 Label Hyperbola

Figure 38 – Dialog boxes for editing curve legends in a plot.

To edit the legend for the second curve, once more open the context menu for the plot and select the option *Legend* > *Edit Legend*. Select "Legend for Curve 2" in the "Curve" field, and type "Hyperbola" for the "Label" field in the dialog box. Then press [Done]. The result from these operations will be the plot as shown in Figure 39.

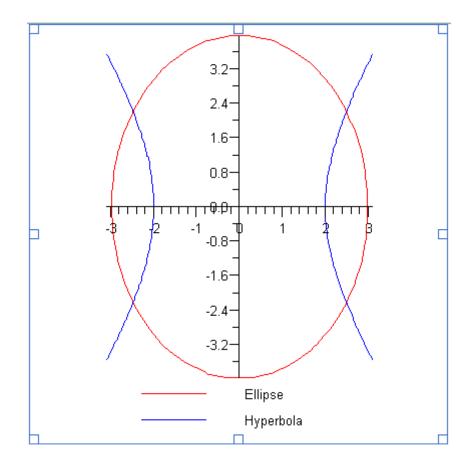


Figure 39 – Ellipse of Figure 37 with hyperbola added by a drag-and-drop operation. Plot includes legend edited through context menus.

<u>Exercise</u> Using the expression

2.5 e
$$-0.01 t \sin(t)$$

to generate a 2-D plot in the range -10 < t < 10 (similar procedure to that leading to Figure 28, except that default range for *x* is not modified in the present exercise). Use drag-and-drop to add the graphics corresponding to the expressions

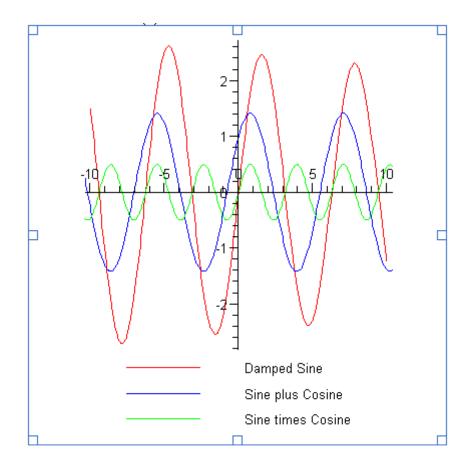
sin(t) + cos(t)

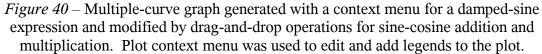
sin(t) cos(t).

Use the plot's context menu to edit the legends so that the legends for the three expressions read "Damped Sine", "Sine plus Cosine", and "Sine times Cosine", respectively. The resulting graph should look like that in Figure 40.

Getting Started with Maple 10 – Page 43

and





Plots with logarithmic scales using context menus

Consider the expression

$$e^{2x} + e^{x}$$

Using context menu we can generate a 2-D plot showing the variation of the function, $y = e^{2x} + e^x$. The vertical scale in the default range -10 < x < 10 reaches from 1 to about 5×10^8 . Using a logarithmic scale for *y* would be use to better understand the variation of the function with *x*. In order to replace the natural scale for a logarithmic one in a graph, we first generate the graph following a procedure similar to that leading to the plot of Figure 28, namely,

- Type the expression $e^{2x} + e^x$ in *Math* input format
- Click on the expression and generate a context menu (*right-click*)
- Select option *Plots*>2-D plot

The resulting plot will be shown in you Maple worksheet. In order to replace the *y* scale with a logarithmic one proceed as follows:

- Click on the plot to select it
- Generate the context menu by doing a *right-click*
- Select the option *Axes* > *Mode*

This will produce a dialog box. Modify it so it looks as in Figure 41, below, then press [Apply][OK], or simply [OK], to produce a logarithmic scale in y. The resulting graph is shown in Figure 42, below.

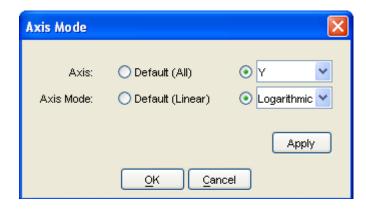


Figure 40 – Dialog box for axes modes generated using a 2-D plot context menu, and selecting Axes > Mode.

Using the *Axes*>*Mode* option in a 2-D plot context menu thus allows us to select logarithmic scales for the *x* axis only (semilogarithmic plot in *x*), for the *y* axis only (semilogarithmic plot in *y*), or for both axes (*double-logarithmic* or *log-log* plot).

Exercise

Using the context menu for the plot of Figure 41, try the following:

- 1. Change the horizontal scale from 1 to 10000
- 2. Produce a semilogarithmic plot in *x* (*x* scale logarithmic, *y* scale natural)
- 3. Produce a semilogarithmic plot in *y* (*x* scale natural, *y* scale logarithmic)
- 4. Produce a double logarithmic plot (both scales logarithmic)
- 5. Add the plots for the functions xe^{2x} and e^x to the existing plot by a drag-and-drop procedure
- 6. Edit the legends of the resulting plot to read "Exp Sum", "X time Exp", and "Exp"
- 7. Produce the plots indicated in steps 2 and 3, above

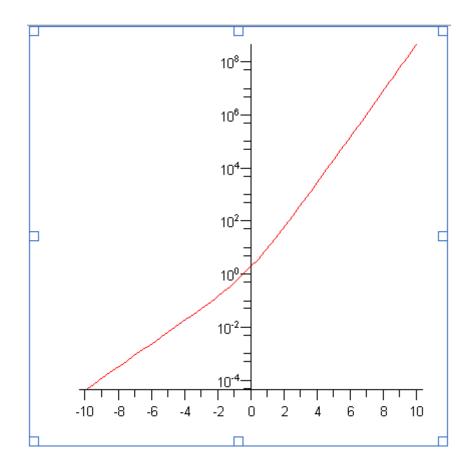


Figure 41 – Two-dimensional plot with *y* logarithmic scale (semilogarithmic plot in *y*).

Contour plots and density plots using context menus

An expression of the form f(x,y) can be plotted in a two-dimensional format as a contour plot or as a density plot. In a contour plot curves corresponding to constant values of f, i.e., f(x,y)=c, are shown in the *x*-*y* plane. In a density plot, instead of showing curves of constant values of f(x,y), different colors or grayscale are shown to indicate the variation in the function f(x,y). Contour plots and density plots (as well as a number of other plots) can be obtained by using the option *Plots* > *Plot Builder* in a context menu associated with the expression f(x,y).

As an example, consider the expression,

$$x \sin(x) + y\cos(y)$$

Type this expression in a *Math* input format, select the expression by clicking on it, and do a *right-click* to produce the corresponding context menu. Then, select the option *Plots>Plot Builder*. As a result you will get the dialog box shown below.

🖁 Interactive Plot Builder: Select Plot Type 🛛 🔀
Select Plot Type
Plot
Select Plot
3-D plot
2-D contour plot
2-D density plot
3-D contour plot
2-D gradient vector-field plot
2-D implicit plot
Select Variable Purpose and Ranges Parameter 1 x Y -5 to 5
Parameter 2 y 💙 -5 to 5
Cancel Options Plot

Figure 42 – Dialog box for the *Plots* > *Plot Builder* option on the context menu for an expression of the form f(x,y).

This dialog box allows us to select from a variety of plots, as shown in Figure 42. I have selected the option 2-D contour plot in the Select Plot box. This selection shows two parameters at play, x and y. The dialog box also indicates the default ranges of those parameters, -5 to 5, for both of them. Keeping those default ranges, press [Plot] to produce the contour plot. The resulting contour plot is shown in Figure 43.

Click on the plot and open the corresponding context menu to see the options available. The contour plot being a two-dimensional plot will show a context menu like that of the 2-D plot of Figure 26.

Exercise

To produce a density plot, click on the expression of interest, and open the corresponding context menu (*right-click*), then select *Plots>Plot Builder*, but this time select *2-D density plot* in the *Select Plot* box. Modify the scales for the two parameters if you so desire, and press [Plot] to produce the density plot equivalent to the contour plot of Figure 43.

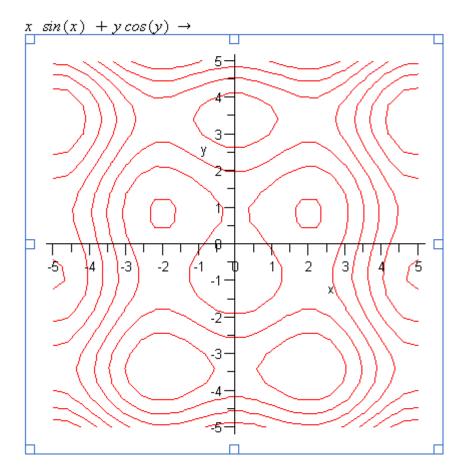


Figure 43 – Contour plot for the expression $x \sin(x) + y \cos(y)$ produced using a context menu and the option *Plots* > *Plot Builder*

Animation of a surface using context menus

Consider the expression

 $sin(a \cdot x) + cos(a \cdot y)$.

Enter this expression in as a *Math* input in a Maple worksheet. Click on the expression, and generate the corresponding context menu (*right-click*). Then, select the options *Plots* > *Plot Builder*. In the resulting dialog box, select *Animation* in the *Select Plot Type* box. Keep all the default selections as shown in the dialog box, except for the range of the animation parameter *a* which should be changed to the range 0 to 2. Then press [Plot].

Click on the resulting plot to open the animation toolbar (see Figure 32), and press the *Play* button in the toolbar (item 3 in Figure 32) to see the animation of the surface produced.

Animation of a contour plot using context menus

Consider once more the expression

 $sin(a \cdot x) + cos(a \cdot y)$.

Enter this expression in as a *Math* input in a Maple worksheet. Click on the expression, and generate the corresponding context menu (*right-click*). Then, select the options *Plots* > *Plot Builder*. In the resulting dialog box, select *Animation* in the *Select Plot Type* box, and select 2-D Contour plot in the Select Plot box. Make sure that *x*, *y*, and *a* are selected as the *First*, *Second*, and *Animation* parameters in the dialog box, with ranges of -5 to 5 for both *x* and *y*, and of 0 to 2 for *a*. Press [Plot].

Click on the resulting plot to open the animation toolbar (see Figure 32), and press the *Play* button in the toolbar (item 3 in Figure 32) to see the animation of the contour plot produced.

Animation of a density plot using context menus

Repeat the exercise from the previous section, but selecting 2-D Density Plot in the Select Plot box in the Plot Builder dialog box. Make sure that the parameters and ranges are the same as in the contour curve animation exercise, and press [Plot]. Run the animation from the animation toolbar after clicking on the plot.

Example of a well-documented worksheet

Maple includes some examples of well-documented worksheets that address specific problems in electrical engineering. Let's look to one of them (the *Harmonic Oscillator* worksheet) as an example of the type of worksheets you want to develop for the solution of your own assignments.

To access the *Harmonic Oscillator* worksheet, select the option *Help* > *Take a Tour of Maple*. This will open the tour worksheet. On the right-hand side of this worksheet there is a column labeled *Sample Documents*. The *Harmonic Oscillator* worksheet can be opened by clicking on the first link in the *Sample Documents* column. Open the worksheet and explore it using the scroll bar on the right-hand side of the document. (Alternatively, use *Help*>*Manuals, Dictionary, and more...*>*Applications and Examples*. This will open the *Applications and Examples* worksheet. The *Harmonic Oscillator* worksheet can be accessed by clicking in the proper link under the section *Applications*).

The *Harmonic Oscillator* worksheet contains a title, a figure (which was produced in a sketching software and pasted into the worksheet), two sections (*Initialization, System Analysis*), and tables with text, equations, and graphics.

Use the options *View>Collapse All Sections* to "close down" the sections in the worksheet. Then, use *View>Expand All Sections* to "open them up." If you have collapsed all sections at once (*View>Collapse All Sections*), you can open one at a time by clicking on the arrow attached to the section title. You can also selectively close one section at a time by clicking on the vertically-downward arrow next to the title of an open

section or sub-section. Try these options with this worksheet. Before continuing, make sure that the two sections are open (i.e., use *View>Expand All Sections*), and scroll the worksheet to the top.

To activate the worksheet select *Edit* > *Execute* > *Worksheet*. This will run all the executable commands in the worksheet. You will see the worksheet scrolling down as the commands are executed. Scroll the worksheet up and down and stop at one of the graphs. Notice that the graphs have sliders attached to them, which are associated with parameters used in the equations. By clicking on the slider and moving the slider indicator you can change the values of the parameters and modify the plot. Try some changes in the parameters by using the sliders. Click the *Harmonic Oscillator* worksheet when done.

Maplets

The ability of adding sliders and other components facilitate sensitivity analysis in a graphical format. Such interactive displays are referred to as *Maplets*. Note: A self-standing application with a GUI (Graphics User Interface) programmed in *Java* is referred to as an *applet*, from *app* – an abbreviation for *application* – and *let* indicating something small or brief. The word *Maplet* is a play on *Maple* and *applets*.

Maplets can be built by adding GUI components to an area of a Maple worksheet. To see the available components click on the *Components* palette in the Maple 10's palette collection (see Figure 11).

The building of Maplets is an advanced application in Maple, therefore, it will not be covered in this document. However, information on Maplets is available in the *Help* facility. For example, try *Help>Manuals*, *Dictionary*, *and more...>Manuals>User Manual* to open the *User Manual* worksheet. Click on item *9 Maplets* to learn the basics of Maplets.

Typically, you'll need some programming to activate a Maplet. Maple programming has not yet covered, another reason to postpone working with Maplets for the time being.

Worksheet mode

By default (e.g., when using *Cntl+n*), Maple worksheets follow a *Document* mode. Thus, so far we have used *File>New>Document mode* to generate new Maple worksheets. In this exercise we'll open a new Maple worksheet in *Worksheet* mode by using *File>New>Worksheet* mode. This will generate a new worksheet showing what is called a *execution group* prompt at the upper left corner of the worksheet. Such a prompt is shown in the following figure.



Figure 44 – Execution group prompt available in Worksheet mode.

When you type in front of the execution group prompt, the input shows up, by default, in *Math* input format. For example, at the prompt, type:

$$int(x^2, x = 0..2)$$

and press return. This command calculates the definite *int*egral of x^2 within the limits 0 and 2. The result, given in symbolic format, is 8/3. This result is shown within the execution group where the command was entered. Also, after executing this command, Maple automatically generated a new execution group immediately below, and moved the cursor at the prompt of that new execution group.

We could use the *Expression* palette to enter the same integration in formal mathematical mode by clicking on the definite integral button in the palette. We need to keep the cursor in front of the new execution group prompt. The resulting operations are shown below:

> $int(x^2, x = 02)$ > $\int_{-2}^{2} x^2 dx$	<u>8</u> 3	(1)
$\sum_{0}^{\infty} x^2 dx$	<u>8</u> 3	(2)

Maple Input format

A new execution group prompt will now be available. Keeping the cursor in front of the prompt of this new execution group, we are going to change the input mode by pressing [F5]. In *Document mode* (i.e., in all the examples in the previous sections of this document), pressing [F5] changed the input mode from *Math* to *text*. In Worksheet mode, however, pressing [F5] changes the input mode from *Math* to *Text/Maple Input*. This is the preferred input mode in earlier versions of Maple (e.g., before version 8), and it's still available in Maple 10 for those of us (like me) who learned Maple way before version 10 became available.

$$\begin{bmatrix} > int (x^{2}, x=0..2); \\ \frac{8}{3} \end{bmatrix}$$
(3)

As an exercise, we'll enter now $int(x^2,x=0..2)$; and press [Enter]. The resulting execution group is shown below.

Note: in *Maple Input* mode you need to end Maple commands with a semi-colon (;) or a colon (:). When you end a command with a colon, the command is executed, but no output is shown, e.g.,

$[> int(x^2,x=0..2):$

In Maple 10, if you are using *Maple Input* to enter commands, and you forget to end it with a semi-colon (or colon), Maple will complete the command anyway, but issue a warning that an incomplete command was entered. Here's an example:

```
> int(x^2, x=0..2)
Warning, inserted missing semicolon at end of
statement
\frac{8}{3}(4)
```

To correct this oversight one needs only click back on the offending command, type the semi-colon (or colon), and press [Enter] again. Maple will recalculate the command and remove the warning message.

Inserting execution groups

An execution group can be inserted below the current location of the cursor by using Cntl+j, or above the current location of the cursor by using Cntl+k. Alternatively, you just can use the options *Insert>Execution Group>Before Cursor* or *Insert>Execution Group>After Cursor*. Another possibility is to click the *Inset Maple Input* button (item 12 in Figure 10) available in the toolbar.

As an exercise, click on any of the execution groups currently available in your worksheet and insert execution groups before and after.

Deleting execution groups

To delete an execution group, click in front of the prompt, and use *Cntl+Delete*. You can also use *Cntl+Delete* to delete individual objects such as Maple input and output, and graphs. All you need to do, is highlight the object you want to delete before using *Cntl+Delete*. Try some execution group deleting in your worksheet.

Inserting a text prompt in an execution group

Text could be used to document the operation(s) in an execution group. Use Cntl+Shift+j to insert a text prompt before the current cursor location, or Cntl+Shift+k to insert a text prompt after the current cursor location. Alternatively, you just can use the options Insert>Paragraph>Before Cursor or Insert>Paragraph>After Cursor. Another possibility is to click the Insert Text button (item 11 in Figure 10) available in the toolbar. This latter option will actually insert a new text block separate from any execution group. Try the different commands listed in this paragraph to insert text in your execution groups, or to insert a separate text block.

Inserting and removing sections

Use *Insert>Section* to insert a section (or *Insert>Subsection*) immediately below the current cursor location. If you want to insert a section (or sub-section) encompassing a number of execution groups, first highlight the collection of execution groups you want to collect into a section, and then press the *Insert Section* button (button 13 in Figure 10) in the toolbar. This will indent the selected execution groups into a section or sub-section. To remove them from a section or subsection, use the *Remove Section* button (button 14 in Figure 10).

Multiple-lines in a single execution group

To enter more than one command into a single execution group, type *Shift-Return* after each line. For example, type:

[F5] (x+y)^2; *Shift-Return* (x-y)^2; *Shift-Return* %+%% *Return*

to produce the following results:

$$\begin{cases} > (x+y)^{2}; \\ (x-y)^{2}; \\ \frac{3}{2} + \frac{3}{2}; \\ (x+y)^{2} \\ (x-y)^{2} \\ (x-y)^{2} + (x+y)^{2} \end{cases}$$
(6)

Using palette commands in Maple Input format

If we have selected the *Maple Input* format in an execution group, inserting expressions from the *Expression* palette will produce the original Maple command corresponding to the desired expression. Table 2, in the following page, shows a listing of some of the calculus commands from the *Expression* palette and their equivalent *Maple Input* commands. Table 3, on the other hand, shows a similar listing for a number of algebraic operations. The operation a^b is straightforward, i.e., a^b . So it's the case with the trigonometric functions, i.e., sin(a), cos(a), tan(a). Table 4 shows operations related to the definition of functions. These operations are also available at the *Expression* palette.

Table 4 shows palette expressions from the *Expression* palette and their equivalent *Maple Input* commands for function evaluation and definitions. The six items shown are the following:

- 1. Evaluation of univariate functions
- 2. Evaluation of bivariate functions
- 3. Definition of univariate functions using the standard "mapping" notation
- 4. Definition of bivariate functions using the standard "mapping" notation
- 5. Definition of multi-value or piecewise functions

Palette expression	Corresponding Maple command
$\int f \mathrm{d}x$	$\left[> \operatorname{int}(\mathbf{f}, \mathbf{x}) \right]$
$\int_{a}^{b} f \mathrm{d}x$	<pre>[> int(f,x=ab);</pre>
$\sum_{i=k}^{n} f$	<pre>[> sum(f,i=kn);</pre>
$\prod_{i=k}^{n} f$	<pre>[> product(f,i=kn);</pre>
$\frac{\mathrm{d}}{\mathrm{d}x}f\text{or}\frac{\partial}{\partialx}f$	[> diff(f,x);
$\lim_{x \to a} f$	<pre>[> limit(f,x=a);</pre>

Table 2 – Palette expressions and Maple Input commands for calculus operations

Table 3 - Palette expressions and Maple Input commands for algebraic operations

Palette expression	Maple Input command
a _n	[> a[n];
\sqrt{a}	<pre>[> sqrt(a);</pre>
, ⁿ /a	<pre>[> (a)^(1/n);</pre>
a!	[> (a)!;
<i>a</i>	<pre>[> abs(a);</pre>
e ^a	<pre>[> exp(a);</pre>
$\ln(a)$	<pre>[> ln(a);</pre>
$\log_{10}(a)$	<pre>[> log[10](a);</pre>
$\log_b(a)$	<pre>[> log[b](a);</pre>
$\begin{pmatrix} a \\ b \end{pmatrix}$	<pre>[> binomial(a,b);</pre>

Palette expression	Maple Input command
f(a)	<pre>[> f(a);</pre>
f(a, b)	<pre>[> f(a,b);</pre>
$f \coloneqq x \to y$	$\begin{bmatrix} \mathbf{y} & \mathbf{f} & \mathbf{f} \end{bmatrix} = \mathbf{x} \rightarrow \mathbf{y};$
$f \coloneqq (x1, x2) \to y$	$[> f := (x1, x2) \rightarrow y;$
$\left \begin{array}{c} f(x) \\ x = a \end{array} \right $	[> eval(f(x), x=a);
$\begin{cases} -x \ x < 0 \\ x \ x > 0 \end{cases}$	[> piecewise(x<0,-x,x>0,x);
$\begin{bmatrix} x & x > 0 \end{bmatrix}$	

 Table 4 - Palette expressions and Maple Input commands for function definition and evaluation

Table 5 shows some examples of Greek characters from the *Greek* palette in Maple 10, an the equivalent reference in *Maple Input* form.

Greek character from palette	Maple Input reference
Г	[> GAMMA
Θ	> Theta
Φ	> Phi
Ŷ	[> gamma
θ	<pre>[> theta</pre>
φ	[> phi

Table 5 – Greek letters and their references in Maple Input form

Notice that the letter Γ (upper-case gamma) is referred to as GAMMA in Maple Input format. The name GAMMA actually refers to the gamma function from mathematics (see the mathematical dictionary, *Help>Manuals, Dictionary, and more>Dictionary*). Upper-case Greek letters have names that start with upper-case letters in *Maple Input* format. Lower-case Greek letters' names start with lower-case letters in *Maple Input* format. See Table 1 for the list of names of the letters in the Greek alphabet.

As an example of application of the *Maple Input* commands and characters of Tables 2 through 4, consider the following Maple command and its result:

> int((alpha+beta)^2*xi+tau,xi=0..alpha/2);

$$\frac{1}{8} (\alpha + \beta)^2 \alpha^2 + \frac{1}{2} \tau \alpha$$

One disadvantage of using *Maple Input* format is that the mathematical expression thus typed is not shown in full mathematical format before it is calculated. One possible solution, if using this type of input, is to enclose the expression in quotes, and add a % symbol (referred to as the *ditto* operator) to the command line, e.g.,

> 'int((alpha+beta)^2*xi+tau, xi=0..alpha/2)';%;

$$\int_{0}^{\frac{1}{2}\alpha} (\alpha + \beta)^{2} \xi + \tau d\xi$$

$$\frac{1}{8} (\alpha + \beta)^{2} \alpha^{2} + \frac{1}{2} \tau \alpha$$

The ditto (%) operator

The *ditto* operator, represented by the percentage symbol, is a reference to the most recent result in Maple. Two ditto operators represent the second-to-most-recent result, and so on. As shown above, the ditto operator is very useful when using *Maple Input* notation, but has not much use in the *Document* mode of Maple 10's worksheets. The ditto and double-ditto operators were used in an earlier example (see equation (6) in page 53).

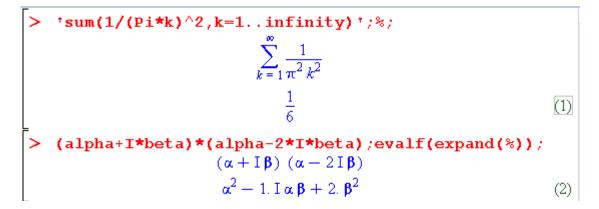
Additional characters in Maple Input representation

The *Common Symbols* palette includes some characters of interest for which we present its *Maple Input* representation in Table 6.

Palette characters	Maple Input reference
π	[> Pi
e	[> exp(1)
<i>i</i> , <i>j</i> , or I	[> I
00	<pre>[> infinity</pre>

Table 6 - Additional characters and their references in Maple Input form

Examples using these characters in *Maple Input* format are shown below.



Summary

In summary, we can create worksheets in *Document* mode or in *Worksheet* mode. *Document mode*, which is the new preferred mode for Maple 10, allows for free location of entry points and allows to enter commands in *Math* input format. The [F5] key in *Document* mode toggles input from *Math* input form to *Text*.

On the other hand, in *Worksheet* mode, we use *execution groups* which can take commands in *Math* input form or in *Maple Input* form. Use [F5] to toggle between these two input forms in an execution group. Maple Input form is the old-fashioned (but still useful, particularly for programming) way to enter Maple commands.

So, which mode is better? The *Document* mode is definitely the best and it is today's preferred mode for Maple worksheets. There is, however, an enormous quantity of old-fashioned Maple worksheets that have been developed in the last 10+ years, for that we can use the *Maple 10 Classical Worksheet application* to operate upon those worksheets. This approach is presented in the next section.

The Maple 10 Classical Worksheet application

This application can be used to read old-fashioned worksheets created in earlier versions of Maple. For an individual Maple 10 server, you will find the Classic Worksheet Maple 10 icon at *Start>All Programs>Maple 10> Classic Worksheet Maple 10*. Use it to open old-fashioned Maple worksheets created with previous versions of the software. You can find many of those worksheets in my web site:

http://www.engineering.usu.edu/cee/faculty/gurro/

Find the *Software* and then the *Maple* links.

The following is a picture of a classic worksheet opened and operated upon in *Classic Worksheet Maple 10*.

🚟 Maple 10 - [FluidsV.mws - [Server 1]]
🐯 File Edit View Insert Format Spreadsheet Window Help 🗕 🗗 🗙
P Normal Trebuchet MS III BIU EE III
$w := U - \frac{m}{2}$
$ z^2$
The velocity components are:
> u:=evalc(-Re(subs(z=x+I*y,w)));
.2.2
$u := -U + \frac{m(x^ y^-)}{2}$
$u := -U + \frac{m(x^2 - y^2)}{(x^2 - y^2)^2 + 4x^2y^2}$
> v:=evalc(Im(subs(z=x+I*y,w)));
$y = \frac{2mxy}{n}$
$v := \frac{2mxy}{(x^2 - y^2)^2 + 4x^2y^2}$
The denominator in the fractions included in <i>u</i> and <i>v</i> can be simplified by using:
[> factor(expand((x^2-y^2)^2+4*x^2*y^2));
2
$(x^2 + y^2)^2$
Available: 565M

Figure 45 – Classic worksheet interface in Maple 10

The preferred Maple 10 interface (shown in the previous 50+ pages) does not support many elements that were used in the classic worksheets. Thus, care must be exercised if opening an old-fashioned worksheet in Maple 10. If in doubt, use the *Classic Worksheet Maple 10* application, and try to copy and paste components from the old-fashioned worksheets into new versions using the new Maple 10 interface.