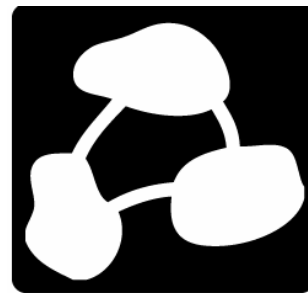


Land Facet Corridor Designer

corridordesign.org



Last updated 20 July 2010

Jeff Jenness

Brian Brost

Paul Beier

Produced with the generous support of

USDA Forest Service Rocky Mountain Research Station

McIntire-Stennis Cooperative Forestry Program

Arizona Board of Forest Research



**Arizona Board of
Forest Research**



**McIntire-Stennis Cooperative
Forestry Research Program**

Compatibility Problems with ArcGIS 10

Some of you may have heard that the next release of ArcGIS has been renamed from ArcGIS 9.4 to ArcGIS 10. One of the reasons ESRI has decided to change this from a minor to a major new release is that they are completely changing the way ArcGIS recognizes custom extensions. Because of this, these Land Facet Corridor tools will likely be completely disabled. The Land Facet Corridor tools are written in Visual Basic 6, and ESRI has changed the way that ArcGIS recognizes custom extensions in such a way that there appears to be no simple way to get ArcGIS too see that the tools are even there.

Jeff Jenness is looking for a way to get the tools to work. So far the method that ESRI is recommending is to rewrite them in VB.NET, and this solution would certainly work. Unfortunately the tools are fairly complex and substantial (over 85,000 lines of code at latest count), and there is no budget for this so it would have to be done in my free time. Therefore it probably won't happen anytime soon. If we can find a way to get ArcGIS 10 to recognize these tools, then we will post the solution on the Corridor Design site.

Installing ArcGIS 9.3.1 Alongside ArcGIS 10:

Some of you may also have heard that ESRI was going to change the installation and registration of ArcGIS in such a way that you could install both ArcGIS 9.3.1 and ArcGIS 9.4 (now ArcGIS 10) on the same system. This was one of the major announcements at last year's ESRI User's Conference, and it might be a reasonable solution to allow you to continue using the Corridor Evaluation tools. Unfortunately ESRI has backed off from this promise, explaining that it turned out to be much more complicated than they had anticipated. At this point, it sounds like they do not mind if you have both versions installed, but you will need to install one of them in a virtual environment such as the Windows XP Virtual Machine available in Windows 7 Professional and Ultimate.

www.corridordesign.org

Produced with the generous support of
USDA Forest Service Rocky Mountain Research Station
and
Arizona Board of Forestry/McIntire-Stennis Cooperative Forestry
Program

Land Facet Corridor Designer

<http://www.corridordesign.org>

OVERVIEW OF LAND FACET CORRIDOR ANALYSIS.....	6
Executive Summary.....	6
Introduction	6
The procedures	7
Major Step 1: Define and map land facets	8
Major Step 2: Develop Maps of Resistance	10
Major Step 3: Least-cost Corridor Modeling	11
Major Step 4: Add a riparian corridor if needed	12
Major Step 5: Join the land facet corridors and corridors for habitat specialist species.....	12
Web-based distribution of the tools.....	16
INSTALLATION OF <i>LAND FACET CORRIDOR DESIGNER</i> TOOLS	17
Uninstalling Land Facet Corridor Designer.....	19
Copying Land Facet Corridor Designer Tools to Other Toolbars	20
If the Land Facet Corridor Designer Crashes	21
SAMPLE WORKFLOW	22
LAND FACET CORRIDOR ANALYSIS TOOLS	24
Export for R Analysis:	24
Land Facet Clusters from R:.....	27
Density Surface Tool:	32
Shannon's Index Tool:.....	34
Identify Termini Polygons Tool:	36
TOPOGRAPHIC POSITION INDEX TOOLS.....	40
Description	40
Scales and Neighborhoods:	41
Classifying by Topographic Position:	42
TPI Types:	44
Neighborhood Types:	45
Using the tools	46
Calculate a TPI Raster:	46
Create a 3-Category Topographic Position Raster:	48

Create a 4-Category Topographic Position Raster:	50
Create a 6-Category Topographic Position Raster:	52
MAHALANOBIS DISTANCE TOOLS	54
Discussion of Mahalanobis Distances:	54
General Concepts:	54
RE-Scaling Mahalanobis Distances using Chi-Square P-values:	58
Applications to Landscape Analysis:	59
Mean Vector and Covariance Matrix Tables:	61
Statistical Matrix Definitions and Formulae:	62
Exact Values vs. Interpolated Values:	63
Additional Reading:	64
Using the Tools:	65
Create Mahalanobis Raster Surface	65
Calculating Mahalanobis Values at Sample Points	69
Generating Statistical Matrices:	73
Chi-Square Raster Transform:	77
R FUNCTIONS FOR DEFINING LAND FACETS	78
An R Primer	78
Using R as a Calculator	78
Assigning Values to Objects	78
Using R Functions	79
Isolating Subsets of Data in a Dataframe:	80
Installing and Loading R Packages	80
Getting Help in R	81
Some Suggestions	81
Overview Of R Functions For Defining Land Facets	82
Kernel Density Estimation: Function LF.kde	83
Identify Outliers: Function LF.outlier	85
Fuzzy c-means Cluster Analysis: Function LF.cluster	86
Exporting Information for Land Facet CorridorDesigner: Function LF.export	88
Downloading The R Functions For Defining Land Facets	89
Workflow For Defining Land Facets	89
ABOUT THE LAND FACET EVALUATION TOOLS AND MANUAL	94
Documents Related to Land Facet Analysis	94

SUGGESTIONS FOR IMPROVEMENTS?..... 95

UPDATES:..... 96

LITERATURE CITED 97

Overview of Land Facet Corridor Analysis

Executive Summary

Land Facet Corridor Designer is a geographic approach to designing wildlife linkages that will be useful in the face of impending climate change. This novel GIS-based procedure identifies the geographic portion of a region that maximizes continuity and diversity of landscape units defined by topographic and soil traits (such as high-elevation north-facing slopes with rocky soils, or low-elevation flats with thick soils) that are expected to facilitate wildlife movement. We refer to these topographic-soil units as *land facets*. The rationale is that future vegetation (and, indirectly, animal assemblages) and human land uses will be determined primarily by the interaction among land facets (soil and topography) and future climate regimes. The conceptual basis for this approach was recently published (Beier, P., and B. Brost. 2010. Use of land facets to plan for climate change: conserving the arenas, not the actors. *Conservation Biology*. DOI: 10.1111/j.1523-1739.2009.01422.x).

Land Facet Corridor Designer is explained in detail, and applied to three landscapes in Arizona, by Brost (2010, MS Thesis, School of Forestry, Northern Arizona University; available online). Publications from this thesis, with Brian Brost as senior author, should appear in the peer-reviewed literature in 2011.

Until now, practitioners designed corridors to promote movement of focal species through today's land cover map. Because land cover maps are likely to change in this century, any corridor linkage based on those maps might fail during climate change. By conserving strands of land facets, linkage designs based on our new procedures should preserve the "arenas" that support current and future biodiversity, without relying on the modeled responses of the temporary occupants of those arenas.

Conservation practitioners now have a flexible tool to design and map corridors of land facets at high resolution (30-m or 10-m, depending on resolution of the DEM) that have a high probability of allowing for animal movement, including shifts of species' geographic ranges, during and after climate change. This can enhance the ability to design wildland networks robust to climate change, reducing the impact of climate change on the biota of natural landscapes. These procedures are transparent and do not depend on global or regional circulation models.

Introduction

In the face of impending climate change, improving connectivity among protected wildlands is the primary conservation strategy (Hannah et al. 2002, Lovejoy & Hannah 2005). Although there are several ways to enhance connectivity, wildlife corridors (e.g., broad, multi-stranded swaths of land connecting National Forests and Grasslands to other nearby protected lands) are appropriate in landscapes increasingly dominated by human uses. However, most existing corridor designs rely on current vegetation maps as the primary driving factor (reviewed by Beier et al. 2008). These corridor designs risk failure because current vegetation and human land uses will change in response to climate change in ways that have proven difficult to predict. Only two efforts (Williams et al. 2005, Phillips et al. 2008) designed corridors to facilitate species' range shifts caused by climate change. Those efforts depended on 50-year projections of a regional circulation model and produced very coarse corridors (chains of 2.9 km² cells). *Land Facet Corridor Designer* is a new approach (finer scale, free of dependence on global and regional climate models) to design corridors robust to climate change.

These GIS procedures produce a linkage design, composed of a multiple swaths that provide high diversity and continuity of land facets (polygons with relatively uniform topographic and soil characteristics, for example high-elevation north-facing slopes on rocky soils, or low-elevation flats with thick soils). The rationale is that future vegetation communities will be determined by the interaction among topographic elements, soil types, future temperature regimes (likely hotter), and future precipitation regimes (wetter or dryer, depending on location). A linkage design with continuous strands of each land facet should provide continuous strands of future vegetation communities, without the need to model climate change and vegetation response directly. Our procedures can also produce a corridor with high interspersions of land facets; such a corridor strand is intended to promote rapid, short movements in response to climate change. The ensemble of about a dozen corridor strands (one for each land facet and one for diversity of facets) constitutes a linkage design for climate change. Because the approach does not in any way depend on global or regional circulation models, emission scenarios, species-specific climate envelope models, or species dispersal models, it avoids massive and compounded uncertainties of approaches that depend on these submodels. Our procedures can be used to make proposed corridors more robust to climate change, or as an alternative useful in areas where no vegetation maps are available (e.g., most of the developing world).

The procedures

A land facet Linkage Design looks a lot like a focal species Linkage Design (Figure 1). Like linkages designed for multiple focal species, linkages designed for a diversity of land facets contain multiple strands connecting two wildland blocks (the natural landscapes to be connected by the linkage, such as a National Forest and a National Park). Specifically the Linkage Design for land facets includes:

- Several (typically 5-15) corridors, each of which is designed to maximize continuity of one of major land facets that occurs in the planning area. Each such strand or corridor is intended to support occupancy and between-block movement by species associated with that land facet in periods of climate quasi-equilibrium. Like each focal species corridor, each land facet corridor is produced by least-cost modeling.
- One corridor with high local interspersions of facets to support range shift, species turnover, and other ecological processes relying on interaction between species and environments. The high diversity corridor is also produced by least-cost modeling.
- A riverine strand to support aquatic species, nutrient and sediment flows, and upland-wetland interactions. Although such a corridor could be produced by an automated GIS procedure, we believe that hand-drawing the major riverine connection is typically easier, and just as accurate.

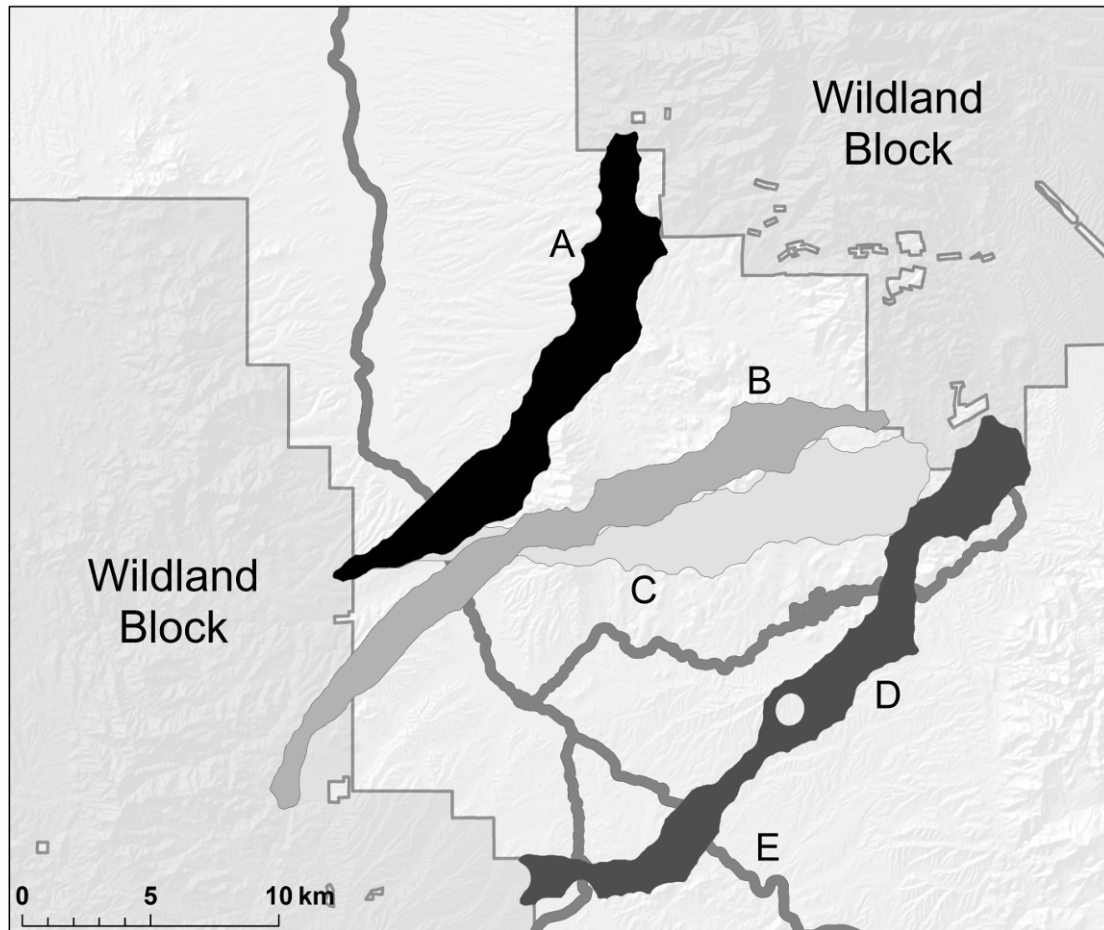


Figure 1. Illustration of a multistranded linkage of land facets designed to allow species to shift their range in response to climate change and to support movement between Wildland Blocks during periods of quasi-equilibrium. Area A optimizes continuity for high local diversity of land facets. Other areas provide the best continuity of high-insolation, steep slopes (area B), low-elevation, gentle canyons (area C), and low-elevation, gentle ridges (area D). Area E encompasses the region's main river and its only perennial tributaries from each wildland block. In practice, a design would include about 10-15 strands, but for clarity fewer are illustrated here.

The conceptual approach to using land facets in conservation planning is described by Beier and Brost (2010); we recommend this paper as an accessible introduction to the topic. We describe our procedures in the following narrative in terms of five Major Steps. The details of the first three Major Steps are illustrated in two flow charts (Figures 2 and 3).

MAJOR STEP 1: DEFINE AND MAP LAND FACETS

Ideally soil attributes should be used along with topographic attributes to define land facets. Unfortunately, soil maps have many limitations (Sanchez et al. 2009). For instance, polygons may lack values for a certain attribute or contain several states of that attribute, indicating the presence of unmapped heterogeneity. In most nonagricultural parts of the western United States, soil maps consist of large, heterogeneous polygons from which inferences about relevant traits, such as moisture, texture, depth, or soil nutrients, cannot be made (Beier and Brost 2010). Therefore, in this description of the approach, land facets are based only on topographic

variables. Because the approach can use both categorical and continuous variables, it can readily be adapted to accommodate categorical soil variables (such as soil type) and continuous soil variables (such as soil depth or moisture). We strongly encourage use of relevant soil data if they are available throughout a planning area.

Moore et al. (1991) and Franklin (1995) discuss approximately 20 topographic variables that can be derived from a digital elevation model (DEM). Our procedures allow the user to select up to 5 soil or topographic variables. To maintain easily interpretable and biologically meaningful land facets, Beier and Brost (2010) recommend using four variables to define land facets from 30-m DEM:

1. Topographic position: Each pixel is assigned to one of three classes, namely canyon, ridges, and slopes¹ (including flat slopes), by comparing the elevation of the pixel to the average elevation within a 200-m radius (Jenness 2006).
2. Annual solar insolation: Sum of instantaneous radiation at half-hour intervals for one day per month over a calendar year using the 'Solar Radiation' tool in ArcGIS 9.3 (ESRI, Redlands, California). The tool calculates half-hour radiation as a function of latitude, aspect, slope, and topographic shading, but ignores thickness of atmosphere and cloud cover.
3. Steepness, expressed as slope angle (see previous footnote).
4. Elevation.

To ensure that the classification represents the land facets of the Wildland Blocks, we use only pixels inside the blocks to define the land facets. Later, pixels in the rest of the analysis area will be assigned to appropriate land facets. Using only the pixels inside the Wildland Blocks, the procedures start with these two steps:

1. Assign each pixel into broad classes of the categorical variable topographic position. This classifies each pixel as a ridge, canyon, or slope pixel. The procedure allows you to choose another categorical variable, such as soil type, or a combination of a categorical soil variable and a topographic position.
2. Characterize each slope pixel based on all three continuous variables (steepness, elevation insolation). Characterize each ridge or canyon pixel based only on steepness and elevation².

Within each topographic position, the procedures involve the following sequential steps:

¹ We use the term *slopes* to refer to the topographic position (a categorical variable) that includes every pixel that is not classified as a canyon bottom or a ridgetop. We use the term *steepness* (or *slope angle*) to refer to the continuous variable that can describe any of the 3 topographic positions. This can result in awkward phrases like “steepness of a slope” – sorry about that. If we ever slip up and refer to “slope of a slope” we are *very* sorry.

² Insolation is not used to identify subclasses of ridges or canyons, because ridges and canyons are usually symmetrical features, that is, a high-insolation ridge is almost always close to a low-insolation ridge. A classification that used insolation to define land facets within ridges would identify different land facets for their opposing sides, such as north-facing and south-facing ridgelines, despite their otherwise similarity. This unnecessarily complicates corridor design because the opposing sides of canyons and ridges are generally close in proximity and can be treated as a unit for conservation purposes. Splitting ridges and canyons on insolation would produce redundant corridors, such as a “cold, high elevation, steep ridge” corridor that is completely intertwined with a “hot, high elevation, steep ridge” corridor.

1. Identify outliers³, i.e., cells with combinations of values of the continuous variables that rarely occur in the Wildland Blocks, and remove them from the analysis. These cells often occur in isolated patches and are limited to a small portion of the landscape. Outliers produce clusters that span a large fraction attribute space, with a diffuse or diluted ecological interpretation. Extreme cells also shift the position of the cluster centroid to a sparse region of multivariate space.
2. Use fuzzy c-means clustering to classify the pixels into c natural clusters or groups, for each value of c from 1 to 10. For instance, a 3-way split of ridges might include high elevation-steep, low elevation-steep, and low elevation-gentle classes. Beier and Brost (2010) explain why fuzzy c-means cluster analysis (Bezdek 1981, Dimitriadou et al. 2009) is superior to hierarchical cluster analysis, nonmetric multidimensional scaling, and two-step cluster analysis.
3. Identify the number of classes, c, that best corresponds to the natural multivariate “lumpiness” in the continuous variables. This requires examining several goodness of fit metrics, evaluating interpretability of classes, draping maps of facet polygons over a topographic hillshade, plotting facet centroids in multivariate space, and inspection of the proposed class map by someone familiar with the landscape to assess whether the c clusters correspond to natural units or impose artificially discrete categories on a continuous landscape.
4. Use a confusion matrix to identify poorly classified pixels, such as slope pixels that assign with roughly equal probability to the “warm, steep, high elevation” and the “cold, steep, high elevation” classes. Remove poorly classified pixels from the analysis to produce a set of distinctive land facets.

These procedures will typically produce a set of 8-16 land facets, such as “high elevation, steep ridges” and “low elevation, gentle, hot, slopes.”

MAJOR STEP 2: DEVELOP MAPS OF RESISTANCE

In focal species approaches to designing linkages, the resistance of a cell represents the difficulty of movement through that cell for a focal species. For the land facet approach, the resistance of a cell is based on the departure of that cell from the prototypical cell of the focal land facet. Our procedures use Mahalanobis distance as the resistance metric. Mahalanobis distance can be thought of as the number of “multivariate standard deviations” between the attributes of a pixel and the characteristic values⁴ for the focal land facet type. For each land facet type, the procedures include the following steps:

- Calculate Mahalanobis distance for every pixel in the analysis area, using the following characteristic values:
 - Mean elevation of pixels of the focal land facet within the Wildland Blocks.
 - Mean insolation of pixels of the focal land facet within the Wildland Blocks.
 - Mean steepness of pixels of the focal land facet within the Wildland Blocks.

³ By default the procedure (kernel density estimation) identifies the most extreme 10% as outliers, but the user can over-ride this setting. Because outliers are defined relative to cells inside Wildland Blocks, the proportion of cells in the matrix classed as outliers will differ from 10% or other specified value.

⁴ For most variables used in a Mahalanobis distance analysis, the characteristic value is the mean. But when one of the variables is “% of pixels of this facet type within a moving window,” 100% is used as the characteristic or “ideal” value, even if the 100% value is far above the mean.

- 100% of pixels in a 100-m radius are pixels of the focal facet type.
- Use aerial photographs to digitize urban or developed areas such as mines that are unlikely to support wildlife movement, even if they otherwise are of a focal facet type. Assign “no data” resistance values (equivalent to infinite resistance) to these pixels. This prevents a corridor from being identified through areas unlikely to support species movements. We caution against wholesale exclusion of agricultural areas, especially if they can be restored to natural vegetation or occupy a large portion of the most productive land facets (those with gentle slopes and high soil moisture).

In addition to linkage for individual land facets, you can also design a single corridor with maximum interspersion of land facets. To do so, our procedures produce a resistance map as follows:

- Calculate Shannon's index, H' , of land facets in a 5-pixel radius (McCune & Grace 2002). Shannon's index incorporates richness and evenness into a single measure. Thus, a high index is achieved by not only maximizing the number of land facets within the neighborhood, but also by balancing representation of those facets.
- Calculate resistance of a pixel as $1/(H' + 0.1)$. This formula⁵ assigns low resistance to pixels with a high diversity index.
- As in designing linkages for individual land facets, remove areas unsuitable for connectivity from the resistance surface.

MAJOR STEP 3: LEAST-COST CORRIDOR MODELING

The procedures to produce a least-cost corridor for each land facet type are very similar to those used to develop least-cost corridors for focal species (Adriaansen et al. 2002, Beier et al. 2008):

- Define corridor termini (potential start and end points) as areas within the wildland blocks that contained the most occurrences of the focal land facet⁶.
- Calculate the cost-weighted distance (cumulative resistance) from each terminus and sum the two resulting raster outputs to produce the corridor results.
- Select a “slice” (cost contour) of the corridor output to delineate the least-cost corridor. We suggest selecting the slice with an approximate minimum width of 1 km over its length for corridors < 10 km long, increasing to an approximate minimum width of 2 km for much longer corridors. We chose these minima because they are similar to the widths recommended by Beier et al. (2008) for corridors for focal species.

To produce a single corridor with maximum interspersion of land facets, our procedures use the following steps:

- To define corridor termini, follow these steps within each Wildland Block separately:
 - Identify the half⁷ of all cells inside each Wildland Blocks with the highest H' values and aggregate them into polygons.

⁵ Adding 0.1 precludes undefined values which would occur in the unlikely event that all cells in a neighborhood are outliers.

⁶ By default, the procedure aggregates all cells with at least one occurrence of the facet within a 3-cell radius into polygons, and retains the largest 50% of these polygons in each respective wildland block as termini. The user can over-ride these settings. In 3 Arizona landscapes, the largest polygons produced by these settings always contained a high density of the focal facet type.

- Retain the largest 50% of the polygons as termini⁸.
- Calculate the cost-weighted distance (cumulative resistance) from each terminus and sum the two resulting raster outputs to produce the corridor results.
- Select a “slice” (cost contour) of the corridor output that is approximately 1 km to 2 km wide, as for the least-cost corridors for individual land facets.

MAJOR STEP 4: ADD A RIPARIAN CORRIDOR IF NEEDED

As stated above, we recommend using soil attributes to define land facets when good soils data are available, but often they are not available. When soil variables can't be used, we suggest using presence of streams, standing water, or riparian plants to map important moist soils. In arid southwestern United States, for example, typically only 1 or 2 of several watersheds in a potential reserve or linkage area support perennial stream flows. Thus, even without a good soil map, conservation planners can prioritize the impervious soils associated with these watersheds. Similarly, vernal pools and karst lakes are features related to soil and geology that are relevant to biodiversity and identifiable without a soil map. In the long term, better soil maps are needed to ensure rigorous mapping of land facets across the entire planning region. Rivers and ephemeral drainages span elevational gradients in a way that increases interspersed and promotes ecological processes and flows, such as movement of animals, sediment, water, and nutrients. Because mechanical geospatial algorithms may fail to identify important riverine connections that are obvious to a human expert, we recommend manual inclusion of riverine elements if necessary (e.g., Cowling et al. 1999, 2003).

MAJOR STEP 5: JOIN THE LAND FACET CORRIDORS AND CORRIDORS FOR HABITAT SPECIALIST SPECIES

The preliminary linkage design is the simple union of the least-cost corridors for all land facets, the land facet diversity corridor, and the major riverine or riparian corridors. In cases where corridors cannot be modeled for focal species (due to lack of land cover maps or lack of knowledge about habitat use or movement by potential focal species), this becomes the final linkage design. If you can model corridors for focal species, we recommend that you do so, creating a somewhat larger linkage design.

Brost (2010) developed linkage designs based on land facets for three landscapes in Arizona where linkage designs for focal species had previously been produced. Using two variables to measure linkage utility, Brost found that linkages designed for land facets served 25 of 28 focal species as well as or better than the focal species designs in these landscapes. The three species better served by the focal species approach had the most narrowly distributed habitat. Compared to land-facet designs, focal species linkages provided a similar degree for only about half the land facets.

These results suggest that a linkage design based on land facets will serve all or most focal species in most landscapes, but it will not serve focal species that have limited habitat available in the study landscape. Therefore, we recommend using the land facet approach to complement, rather than replace, focal species approaches. Because the land facet design tends to be larger than the focal species linkage design, and because the land facet design will serve most focal species, it is more efficient to start with the land facet design, and then overlaying the focal

⁷ The user can select a different threshold.

⁸ The user can select a different percentage.

species corridors, and expanding the design to better serve species not well served by the preliminary linkage design.

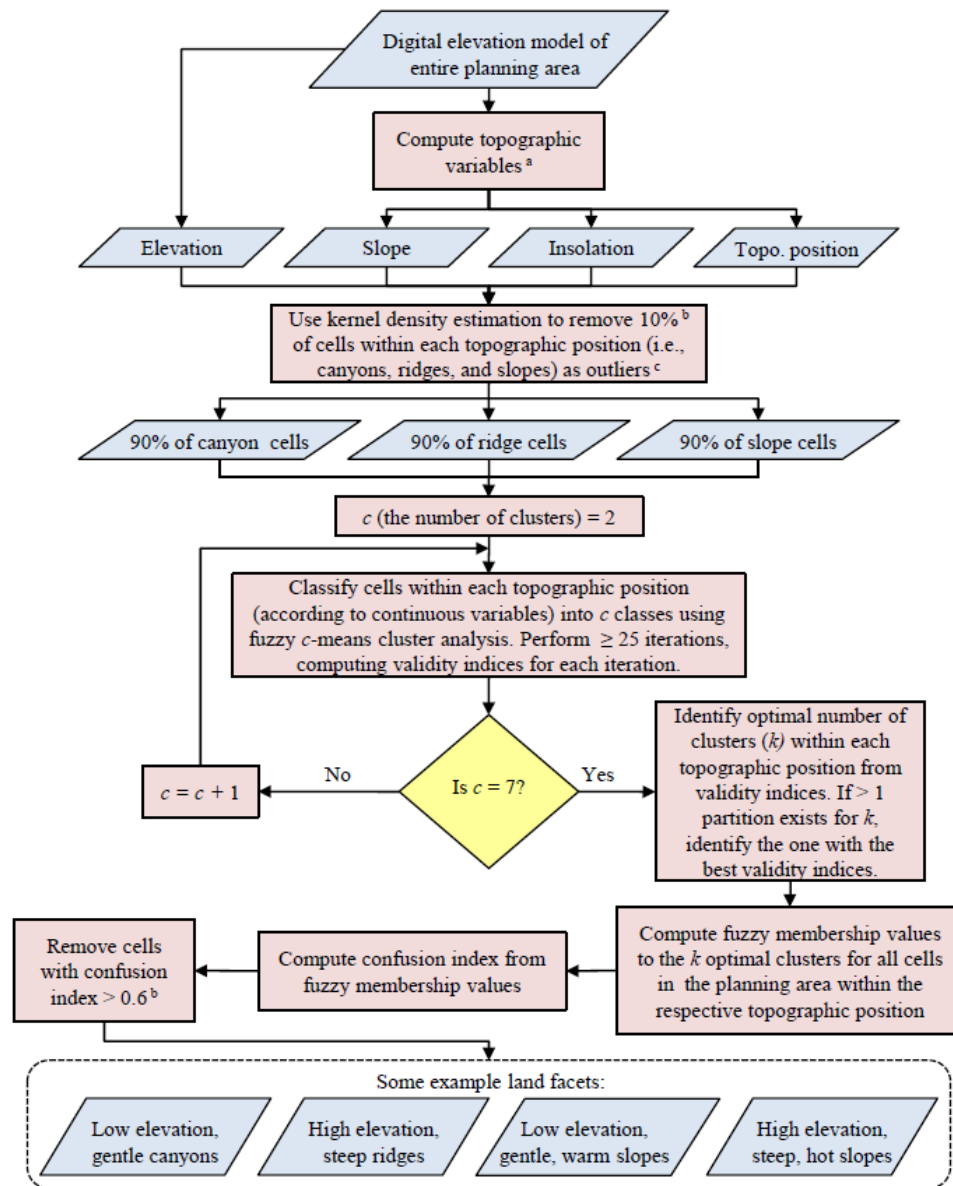


Figure 2. Sequence of operations used to define land facets. The procedures in the first 3 lines (calculation of topographic and soil variables) are conducted in ArcGIS, which exports the values of each variable for each pixel. These values are processed by the statistical package R, which carry out all the other procedures in this flow chart. The outputs from R (land facet code and mean value of each variable for each pixel) are then used by ArcGIS to carry out the procedures in Figure 3.

^a These 4 variables were useful in landscapes we analyzed; the analyst can select other topographic or soil variables.

^b The user can over-ride these default thresholds (10% of cells, 0.6 value of confusion index).

^c We identified outliers (and clusters) with respect to elevation and slope for cells within the canyons and ridges topographic positions. Elevation, slope, and insolation were used for cells within the slopes topographic position.

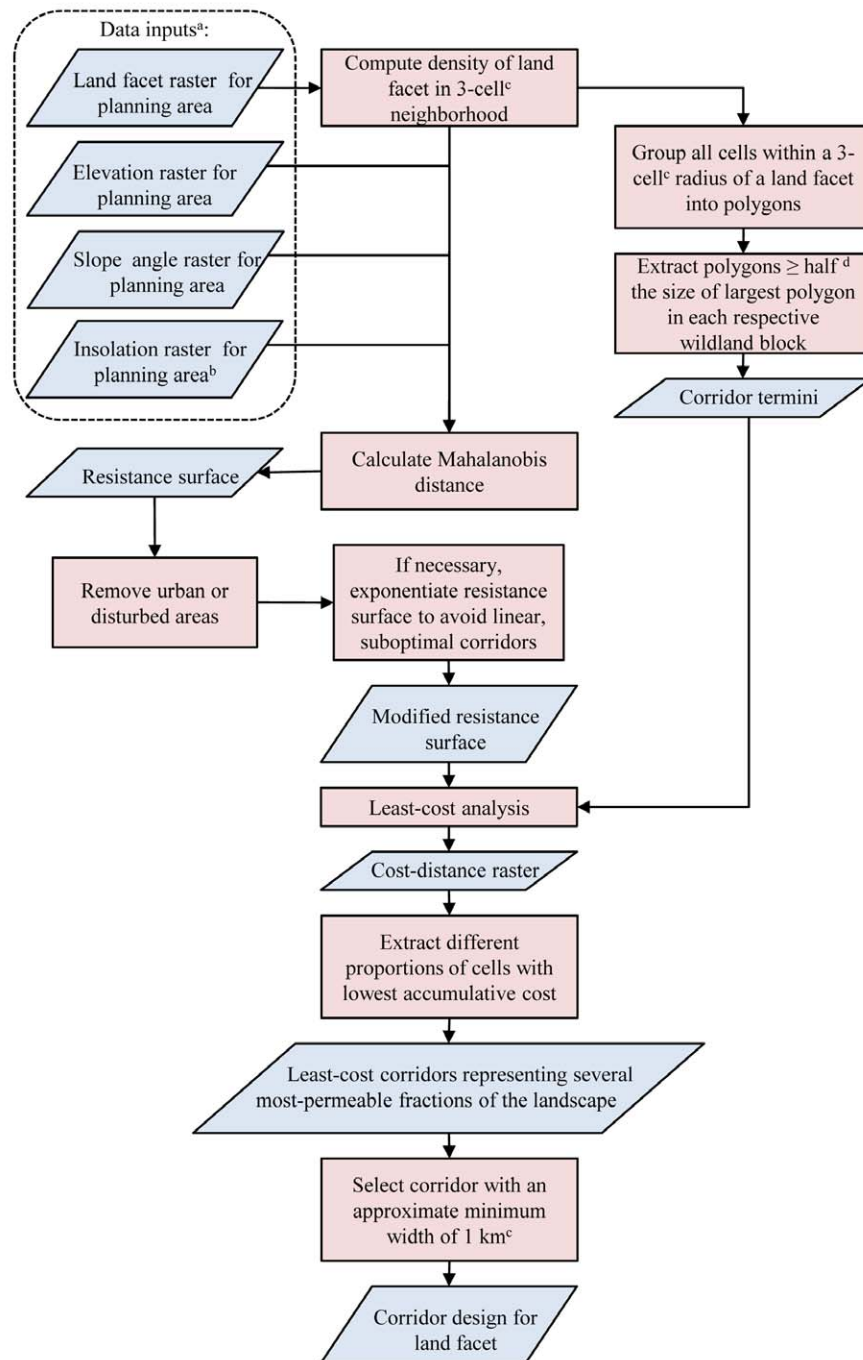


Figure 3. Sequence of operations used to design a corridor for one land facet. This process is repeated for each land facet. The resulting corridors, plus a corridor for high interspersion of land facets, and a corridor of riparian habitat, are then joined to create the linkage design. All procedures in this flow chart are carried out in ArcGIS 9.3.

^a The 3 variables are illustrative of the topographic or soil variables the analysts can use.

^b We used solar insolation to calculate resistance surfaces for land facets in the slopes topographic position only.

^c The user can over-ride these default thresholds (radius of 3 cells, largest 50% of polygons, 1-km width).

^d The area threshold for defining termini can be adjusted to avoid highly-linear corridors.

Web-based distribution of the tools

The materials available for download include:

- ArcGIS 9.3 tools for designing corridors of land facets, including an on-line User's Manual. These tools must be used in concert with certain statistical procedures outside ArcGIS.
- Source code for the ArcGIS tools.
- A package of statistical procedures in R, and an accompanying User's Manual. These procedures process outputs from ArcGIS to produce new data that can easily be imported back into ArcGIS for the final linkage design.
- Brian Brost's MS thesis, which describes how the procedures were developed. The thesis also applies the procedures to three landscapes in Arizona, and describes how well the linkage design for land facets matches linkage designs for multiple focal species in the same landscape.
- PDF reprint of a paper introducing the concept of using land facets to design linkages: Beier, P., and B. Brost. 2010. Use of land facets to plan for climate change: conserving the arenas, not the actors. *Conservation Biology*. DOI: 10.1111/j.1523-1739.2009.01422.x

Installation of *Land Facet Corridor Designer* Tools

Note: This extension is intended as a companion to *CorridorDesigner*⁹ available at <http://www.corridordesign.org>, and we recommend that you also download and install those tools. The tools in this extension will work fine without *CorridorDesigner*, but some of the general tasks (such as creating corridor polygons over a habitat suitability raster, or creating patch polygons) require functions from *CorridorDesigner*. The tools in *Land Facet Corridor Designer* provide an alternative way to create the “habitat suitability” raster (i.e. the cost surface), but using land facets rather than focal species. Once you have created that cost surface raster, then you can use the standard *CorridorDesigner* tools to create the corridor polygons.

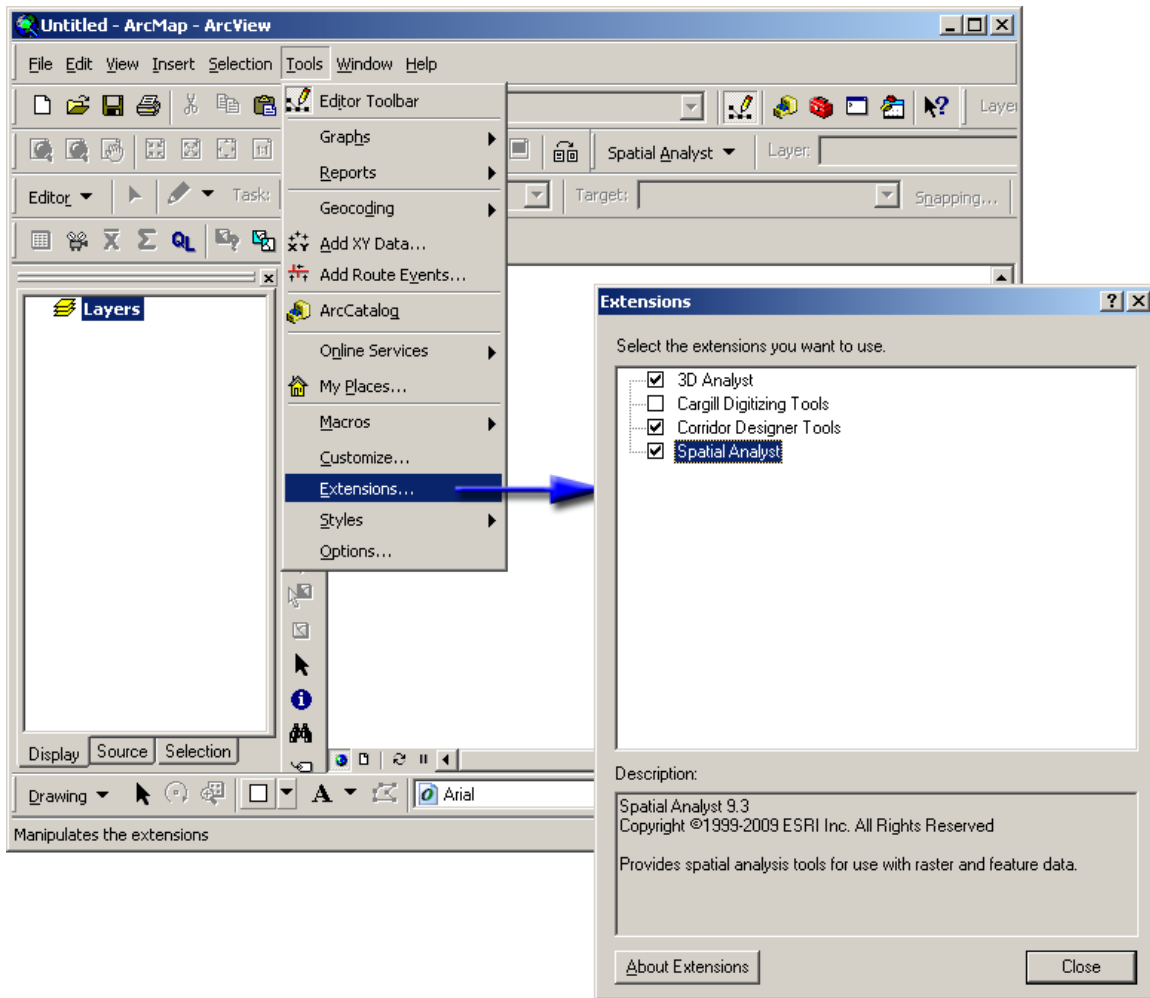
Step 1: First turn off ArcGIS

Step 2: Install the *Land Facet Corridor Designer* tools by double-clicking on the file “LandFacetCorridor.exe” and following the instructions. The installation routine will register the TopoCorridor.dll with all the required ArcMap components. The default install folder for the extension is named “Land_Facet_Corridors” and is located inside the folder “Program Files”. This folder will also include some additional files and this manual.

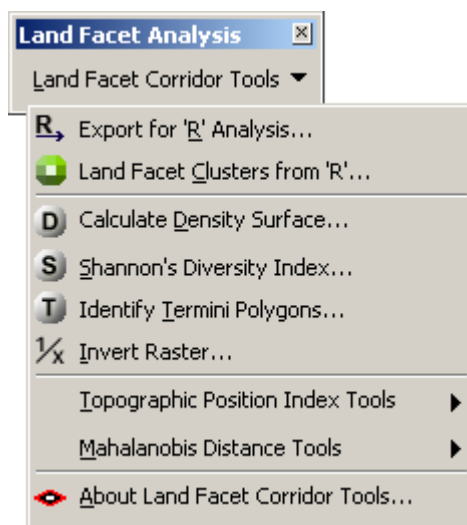
Step 3: Turn ArcGIS back on.

This tool requires some functions from the ESRI Spatial Analyst extension so you may need to turn on that extension in ArcMap after you have installed it.

⁹ *CorridorDesigner* refers to the ArcGIS tools to create linkage designs based on focal spp. *Land Facet Corridor Designer* refers to the tools described herein.



You should see the following new toolbar in your map (it may also be embedded in your standard ArcMap toolbars, rather than as a standalone object):

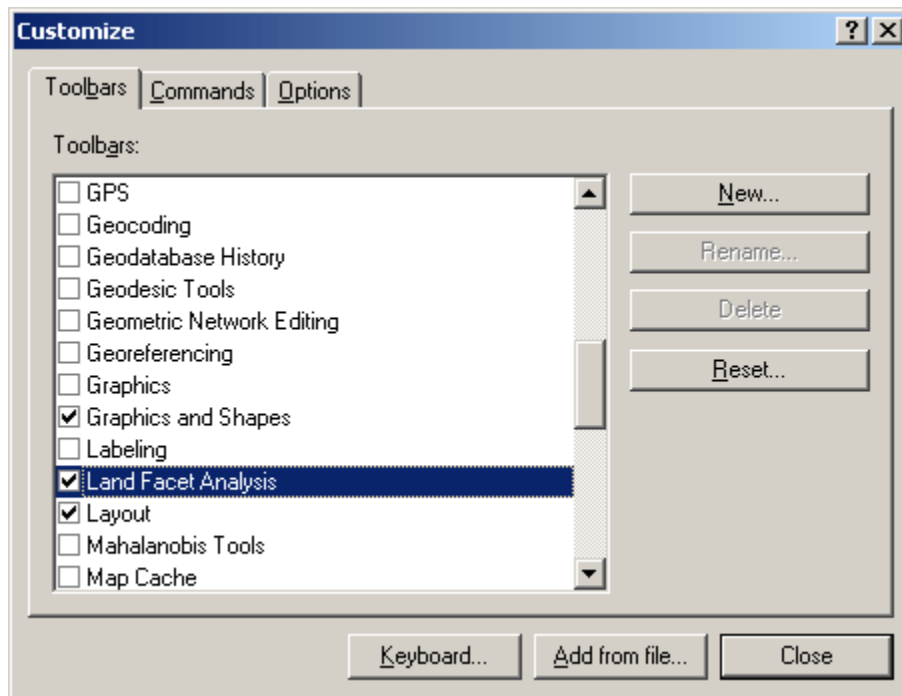


If you do not see this toolbar, then open your “Customize” dialog by:

- 1) Double-click on a blank part of the ArcMap toolbar, or

- 2) Click the “Tools” menu, then “Customize”.

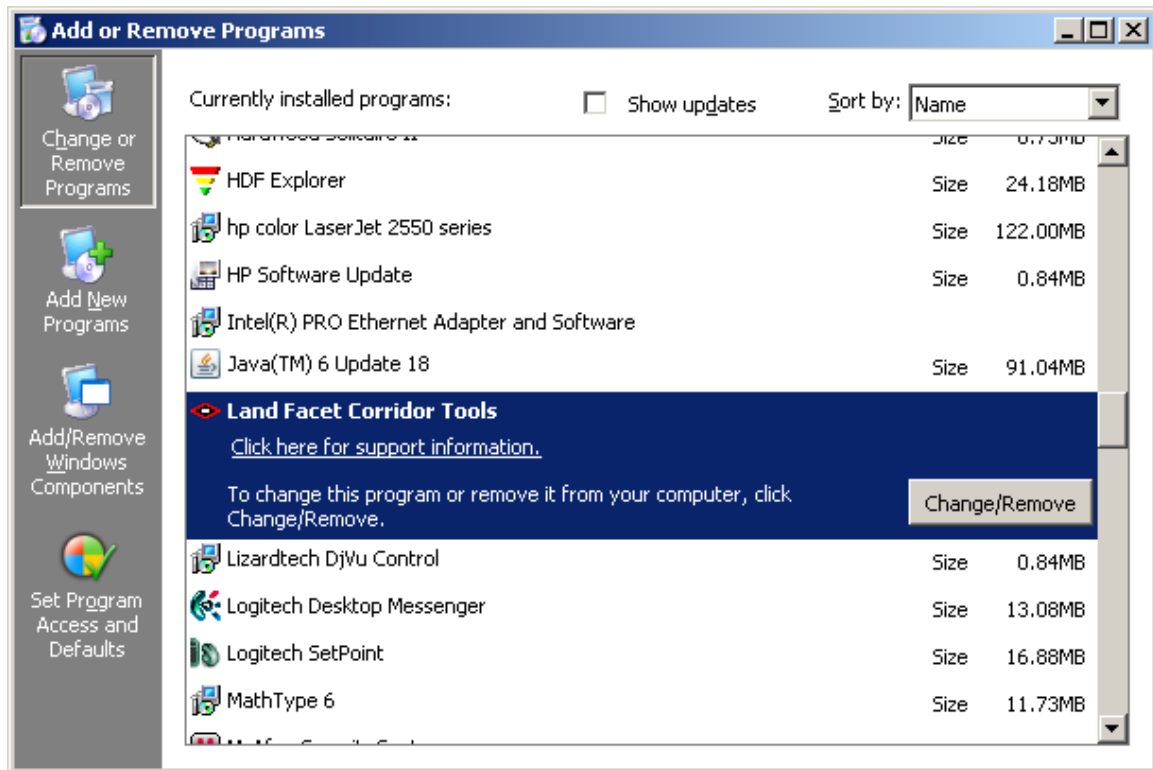
In the “Customize” dialog, click the “Toolbars” tab and check the box next to “Land Facet Analysis”:



You should now see the Land Facet Corridor Designer.

Uninstalling Land Facet Corridor Designer

- 1) Click the Start button.
- 2) Open your Control Panel.
- 3) Double-click “Add or Remove Programs”.
- 4) Scroll down to find and select “Land Facet Corridor Tools”.
- 5) Click the “Remove” button and follow the directions.



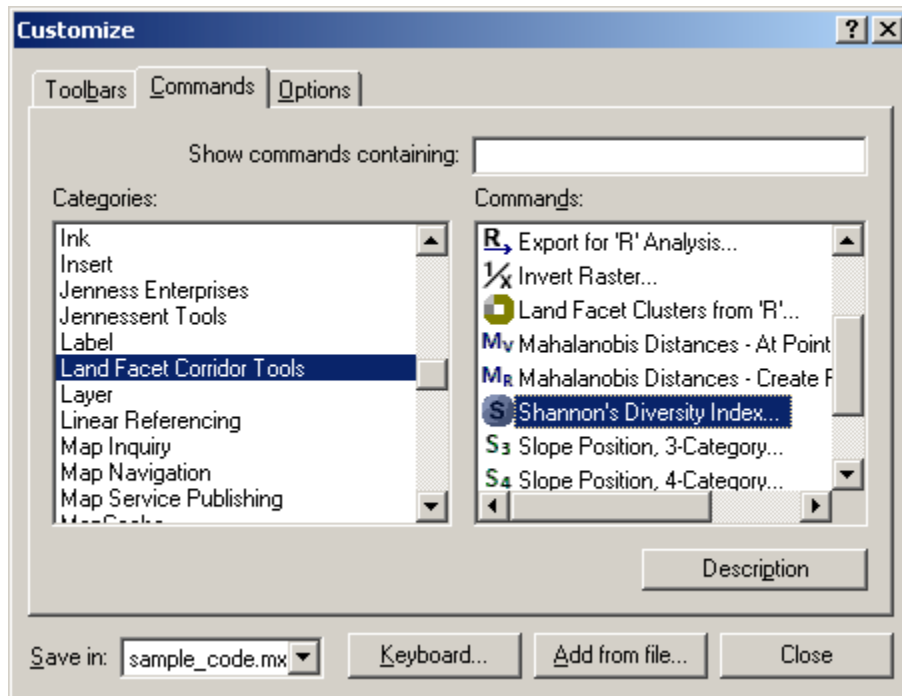
Copying Land Facet Corridor Designer Tools to Other Toolbars

Because of the way ArcGIS handles toolbars and command buttons, you may add any Land Facet Corridor Designer command buttons to any toolbar you wish. For example, if you would like to keep the *Shannon's Index* tool available even when the Land Facet Corridor Designer toolbar is not turned on, you may easily add that tool to any of the existing ArcGIS toolbars.

To do this, open your “Customize” tool by either:

- 1) Double-clicking on a blank part of the ArcMap toolbar, or
- 2) Clicking the “Tools” menu, then “Customize”.

In the “Customize” dialog, click the “Commands” tab and scroll down to select “Land Facet Corridor Tools”:












Finally, simply drag any of the commands out of the Customize dialog up into any of the existing ArcGIS toolbars.

If the Land Facet Corridor Designer Crashes

If the tool crashes, you should see a dialog that tells us what script crashed and where it crashed. I would appreciate it if you could take screenshots of those dialogs and email them to me at jeffj_LFCD@jennessent.com.




Sample Workflow

A typical Land Facet Corridor analysis might follow these steps¹⁰:

- 1) Select or Create an Initial Classification Raster. These classes are your first pass at classifying your landscape, and each class will be further divided into land facets.
 - a) If you prefer not to use an initial classification raster, then you will still need to use a raster which designates the entire landscape as a single class. A simple way to create this raster would be to use the raster calculator or the “Create Constant Raster” ArcTool (*ArcToolbox*, → *Spatial Analyst Tools*, → *Raster Creation*, → *Create Constant Raster*) to create a raster of some constant value across the entire study area. Make sure to set the raster to the appropriate cell size and extent.
 - b) If you already have a general classification raster (such as a soil type, landform or topographic position raster) you may use that.
 - c) Alternatively, use one of the Topographic Position Index tools (,  or ) to create either a 3-class, 4-class or 6-class Topographic Position raster (p. 40).
- 2) Use the *Export for R Analysis* tool  (p. 24) to export tables of data, one for each class in step (1) above, to R or some equivalent statistical software package. This tool also allows you to restrict exporting data to only those regions within wildland blocks (or any polygon layer).
- 3) For each Class from Step (1), do the following:
 - a) Use your statistical software to import the appropriate data table from Step (2), and perform Fuzzy C-Means Clustering to determine the appropriate number of clusters and the cluster centroids for this class. We have provided a set of R tools to assist with this (see *R Functions for Defining Land Facets*, p. 78).
 - b) Use the *Land Facet Clusters from R* tool  (p. 27) import the statistical output files and classify each original class from Step (1) into multiple land facet categories.
 - c) For each Land Facet category, do the following:
 - i) Use the *Calculate Density Surface* tool  (p. 58) to compute the density of this land facet within a specified neighborhood.
 - ii) Use the *Identify Termini Polygons* tool  (p. 36) to convert the Density surface into polygons and identify the largest polygons in each Wildland Block.
 - iii) Use the *Statistical Matrices, Vector and Raster Inputs* tool  (in the *Mahalanobis Distance Tools* menu, [p. 73]) to calculate a vector of mean values and a covariance matrix for all your variables.
 - iv) Change the mean value of the “Land Facet Density” variable to “1”, because 1 is the ideal Land Facet Density value.
 - v) Use the *Mahalanobis Distances – Create Raster Surface* tool  (p. 54) to calculate the Mahalanobis Distance value for all cells on the landscape. You will choose the

¹⁰ Please read the *Overview* (above) to understand the rationale for each step in the workflow.

option to use existing mean vector and covariance matrix tables, and you will use the data from steps (ii) and (iii) above.

- vi) Use the standard *CorridorDesigner* tools to create land facet corridors between your wildland blocks. Use the Mahalanobis Distance raster from step (iv) above as the cost surface.
- 4) Use standard ArcGIS tools to combine all land facet categories into a single raster (for example, the *Mosaic to New Raster* tool in *ArcToolbox*, → *Data Management Tools*, → *Raster*, → *Raster Dataset*, → *Mosaic to New Raster*). Make sure that all unique land facets from each raster have a unique value before you combine them.
- 5) Use the *Shannon's Index* tool  (p. 34) to calculate the diversity of land values within a specified neighborhood around all cells.
- 6) Use the *Identify Termini Polygons* tool  (p. 36) to convert the Diversity surface from step (5) into polygons and identify the largest polygons in each Wildland Block.
- 7) Use the *Invert Raster* tool  (p. 39) to invert the Diversity raster from step (5) above.
- 8) Use the standard *CorridorDesigner* tools to create a Diversity corridor between your wildland blocks. Use your inverted Shannon's Index raster from step (6) above as your cost surface.
- 9) Use standard ArcGIS tools to combine all individual corridors into a single linkage design.

Land Facet Corridor Analysis Tools

Export for R Analysis:

Land Facet definitions are based on Fuzzy C-Means clustering (often referred to in the literature as FCM clustering), which means that points on the landscape are clustered into relatively homogeneous groups based on the various data layers you are analyzing. For example, if you use slope, elevation and insolation to identify clusters within the “canyon bottom” topographic position, you might find many pixels of high elevation, gentle slope, and low solar insolation. These would become one of your land facets and you might name it “High elevation canyon bottoms.”

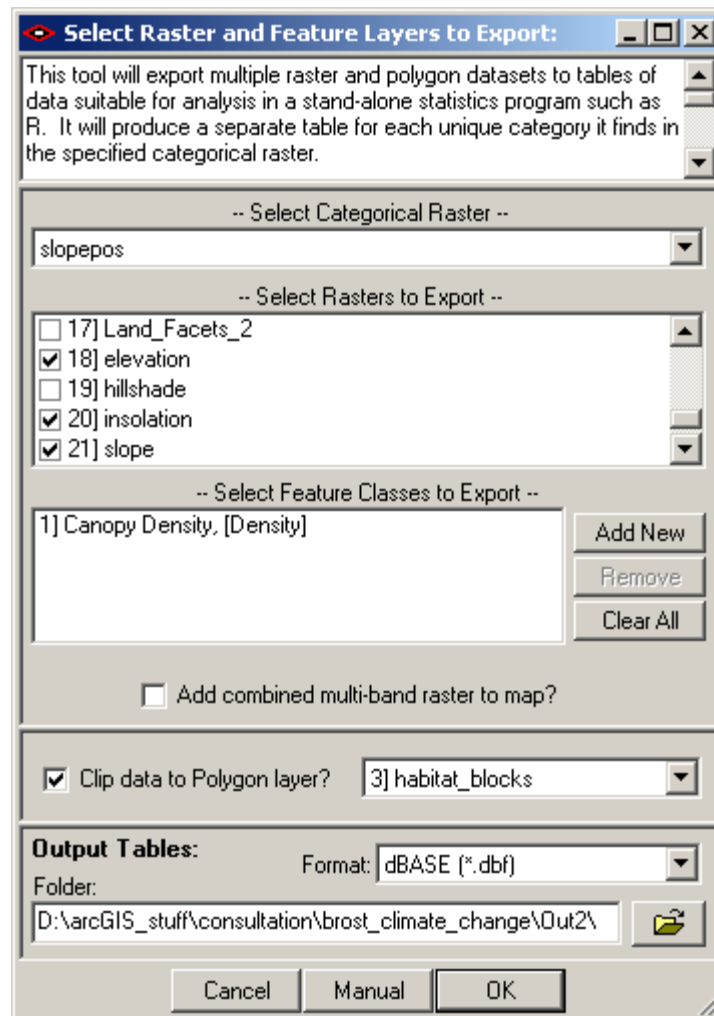
“Fuzzy” clustering means that all points on the landscape are assigned a “Strength of Membership” value to all clusters, rather than just assigning it to a specific cluster. The cluster assignment would be the one with the highest strength of membership, but we can (and will) exclude pixels that are not strongly identified with any single cluster.

This tool does not perform the actual Fuzzy Clustering analysis. Rather, this tool will export one or more tables of data that are suitable for analysis in R or some other statistical software package. Statistical software provides methods for both FCM clustering as well as metrics to help you decide what number of clusters is best. Please refer to the *R Functions for Defining Land Facets* (p. 78) for a discussion of the R tools provided with this extension.

This “Export for R Analysis” tool exports your data in a format appropriate for analysis in your statistical software. Specifically it creates a separate table of data for each unique initial landscape category (such as a TPI-based Slope Classification raster, or possibly a Soil Category raster). Each table contains records for each raster cell from that landscape category in your Wildland Blocks, with an attribute value for each analysis layer (i.e. values for elevation, slope, insolation, etc. at that location). **Note:** This tool does **not** require that all of your data have the same cell size and projection. All data will be internally reprojected and resized to match your initial categorical layer before the table is created.

This tool should be used in conjunction with the *R Functions for Defining Land Facets* (p. 78) and then the *Land Facet Clusters from R* tool (p. 27) to actually create your land facets on the landscape.

Click the  button to run the tool.



Select Categorical Raster: You **must** provide an initial categorical raster. This breaks up the landscape into your initial categories (e.g., Topographic Position Classes or Soil Classes). This tool will generate a separate table for each unique category value it finds in your raster. Later you will generate separate sets of land facets within each category.

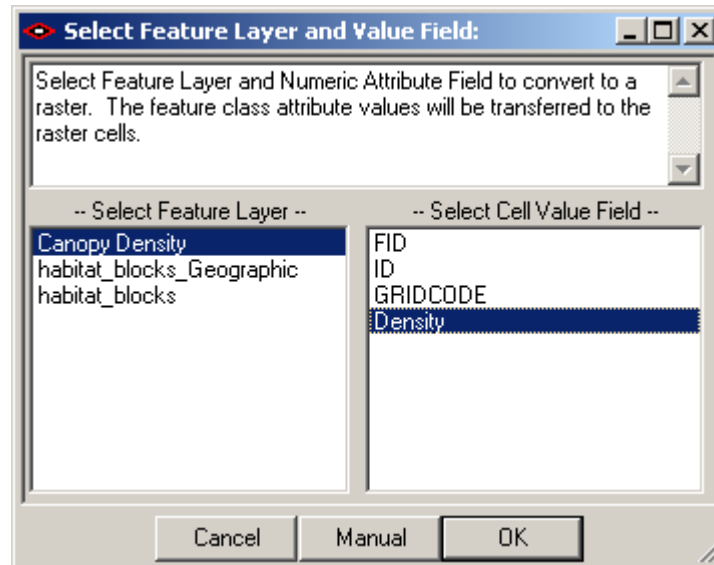
This initial categorical raster is also used as the template for all other data used in the analysis. The output tables produced by this tool will have rows of data reflecting cell locations from this raster. If your other data are in different projections or have different extents or cell sizes, then those other data will be reprojected, resized and rescaled to match this initial raster. If you use any polygon layers, then those polygon layers will be converted to a raster with the same extent, projection and cell size of this initial raster.

If you do not wish to use any initial categorization of your landscape (i.e. if you just want to consider the entire landscape as a single category), you still **must** specify a raster which designates the entire landscape as a single class because the tool needs to use this raster as a template. You can easily create a constant-value raster with the raster calculator or the ArcTool “Create Constant Raster” (*ArcToolbox*, → *Spatial Analyst Tools*, → *Raster Creation*, → *Create Constant Raster*). Make sure to set the raster to the appropriate cell size and extent.

You can use the *Topographic Position Index* tools (p. 40) to create topographic position class categorical rasters.

Rasters To Export: This list shows all rasters in your active map. Select all the ones you wish to include in the data tables.

Feature Class to Export: If you wish, you may also add data from polygon feature classes. Click the ‘Add New’ button to show a list of polygon layers in your map, and select both the layer and appropriate attribute field.



Add combined multi-band raster to map: This option will add a multi-band raster layer to your map containing all the analysis layers included as separate bands. This is not necessary for the analysis, but it might be informative to you just to see how the tool reprojects, resizes, rescales and clips all data layers to a common format.

Clip data to Polygon Layer: This option is recommended for Land Facet analysis. This will clip the input layers so that only those regions that lay within the Wildland Blocks are exported to the output tables. By using this option, you ensure that the cluster analysis produces clusters that represent regions inside the Wildland Blocks rather than the entire study area.

Output Tables: This tool will produce a separate table for each unique category in your initial categorical raster. Each table will be named “FuzzyData_ClassX”, where “X” is the numeric value of the category from the initial categorical raster. If a table already exists with that name in your specified folder, then this tool will automatically append a numeric value to make the name unique (i.e. “FuzzyData_ClassX_2”, “FuzzyData_ClassX_3”, etc.) The tool will open these tables in your map document so you can review them before analyzing them in your statistical software.

Upon completion the tool will give you a report summarizing all the input parameters and showing where all the output tables were saved.

Land Facet Clusters from R:

This tool uses the parameter files produced by your statistical software to generate a set of land facets for a single landscape category (e.g., for the *ridgetop* topographic position, or a particular soil category). You will need to repeat this process for each landscape category.

The final land facet classification for any particular point on the landscape will be based on the highest cluster membership value at that point, whether or not the combination of landscape variables makes the point an outlier (as determined by the R analysis), and whether the confusion index at that point is below a specified threshold. Points that are considered outliers and points that exceed the confusion index threshold will be assigned NoData values in the land facet raster. All other points will be assigned a land facet category according to the highest cluster membership value.

Note: This tool requires 4 – 5 files from your statistical output. These files **must** be formatted correctly in order to be read by this tool. If you use the R tools supplied with this extension (see p. 78), then your data files should all be formatted correctly for this tool. Otherwise you will need to make sure the files are formatted correctly yourself. The required files are:

1. A file of the **cluster centroids**, as a comma-delimited text file (*.csv). The first row of this file should contain the variable names, and each row thereafter should contain the X- and Y-coordinates of the centroids. **Note:** These centroids are in **graph space** (or **multivariate space**) – *not* geographic space. They are also based on standardized variable data, not the original data. For example, a file containing 4 centroids derived from Elevation and Slope layers will look like the following:

```
"elevation","slope"
1.64018638860946,1.04783261529517
0.539214631963649,-0.595812897281045
-0.884427408396287,-0.900497532396411
-0.302027659811837,0.85184747241411
```

2. A file of the **standardization parameters** (i.e. the mean and standard deviation of each variable) as a comma-delimited text file (*.csv). These values are in units of the original data, e.g., meters of elevation. This file will have exactly 3 rows. The first row should contain an empty text value, then the name of each variable. The second row should contain the word “mean”, then the mean for each variable. The third row should contain the word “sd”, and then the standard deviation for each variable. For example, a standardization parameters file for the same analysis illustrated in [1] above will look like the following:

```
","elevation","slope"
"mean",1420.50778137251,16.564496811089
"sd",205.77177104164,8.38386627343209
```

3. A file of the **bin widths** used in the cluster analysis, as a comma-delimited text file (*.csv). As discussed in the section on *R Functions for Defining Land Facets* (p. 78), the data are binned to speed up the processing time. This file will have exactly 2 rows. The

first row should contain the variable names, and the second row should contain the bin width of each variable. For example:


```
"elevation", "slope"
6.10668600994654, 0.248883798708814
```

4. A file of the **bin coordinates** for all the non-outlier bins used in the cluster analysis, as a comma-delimited text file (*.csv). The R tools should have excluded a percentage of the most extreme bins as outliers. This file of bin coordinates contains all the bins that were not excluded. The tool will use this list of non-extreme bin coordinates, along with the bin widths, to determine which regions on your landscape should also be excluded as outliers. This file will typically have hundreds or thousands of bin centerpoint coordinates. The first row should include the variable names and all subsequent rows should include the centerpoint coordinates for each bin. For example:

```
"elevation", "slope"
1065.683075, 2.546923765
1065.683075, 3.044691363
1065.683075, 3.54245896
...
...
...
2103.819696, 29.42637403
2103.819696, 29.92414162
2152.673184, 30.42190922
```

5. **Optional:** A file of the **FCM Fuzziness parameter** used in the analysis, as a standard ASCII text file (*.txt). This file should have only a single row with a single numeric value. The tool requires that you use the same fuzziness parameter here that you used in the FCM analysis, but you can either enter it manually or load the value from a file. A file indicating a fuzziness parameter of 1.5 will look like the following:

```
1.5
```

Click the  button to run the tool. You will need to step through 4 dialogs in order to specify all the required analysis parameters.

Step 1: Identify the same categorical raster used in the *Export for R Analysis* tool (p. 24). You will also need to identify specifically which landscape category you are creating land facets for. Recall that you need to repeat this process for each landscape category.

Also specify where to save your new land facet raster and in what format. All land facets for this landscape category will be in this single raster.

Optional - Save Table with Fuzzy Cluster Statistics: Optionally you can generate a table with all the data necessary to create the land facets yourself. This is not necessary but it is useful if you want to confirm the output or if you want to know more about the cluster properties of any of the pixels. This table will contain one row for each cell in this landscape category. The attribute fields will include X- and Y-coordinates, an ID value for the landscape category, values for all input variables, cluster membership values for all clusters, Cluster ID values for the clusters with 1st and 2nd highest strengths of membership, the confusion index value at this cell, and whether or not R classified the cell as an outlier.

Classify Land Facets, Step 1 of 4:

This tool will classify the study area into land facets, based on output from R or a similar statistical package. In this first step, you will select the region to consider for this classification. If you have divided the landscape into topographic position categories, and are now planning to classify land facets within a particular

-- Select Categorical Raster --

- 5] Land_Facet_11
- 6] Land_Facets_7
- 7] comb_facets
- 8] Polylines_Po
- 9] Land_Facet_Clip
- 10] Land_Facets_6
- 11] Land_Facets_2
- 12] slopepos

-- Select Raster Attribute Field --

- VALUE
- COUNT

Category Value = 2

Output Land Facet Dataset:

Output Raster Format: ESRI GRID

Output Raster Dataset Name: D:\arcGIS_stuff\consultation\brost_climate_change\TPI_out\Land_Facets

☒ Save Table with Fuzzy Cluster Statistics

Output Table Format: dBASE (*.dbf)

Output Table Name: D:\arcGIS_stuff\consultation\brost_climate_change\Output\Cell_Stats_6.dbf

Buttons: Cancel, Manual, Next -->

Step 2: Identify the *.CSV files containing the cluster centroids, standardization parameters, bin widths and bin locations. As you select each file, the tool will show you the information included in that file as well as the actual file text.

Classify Land Facets, Step 2 of 4:

Your statistical analysis should have produced four *.csv files. The "Centroids" file contains the cluster centroid coordinates for all of your clusters. The "Bin Widths" file contains the parameters used to determine the bin sizes, and the "Eval Points" file contains the bin centroids which are used to determine which values are outliers and are therefore excluded from the analysis. The "Params" file contains the mean and standard deviation of all variables, and is used to standardize the data.

<p><input checked="" type="radio"/> Load Centroids File <input type="radio"/> Clear Centroids Data</p> <p>-- Centroids --</p> <p>Filename = <i>centroids.csv</i> Variable Count = 2 1) elevation 2) slope Centroid Count = 4</p> <p>Centroid #1 -- elevation: 1.64018639 -- slope: 1.04783262</p>	<p><input checked="" type="radio"/> Load Params File <input type="radio"/> Clear Params Data</p> <p>-- Params --</p> <p>Filename = <i>param.csv</i> Variable Count = 2 1) elevation 2) slope Variable Params: -- elevation: -- Mean = 1420.50778137 -- Standard Deviation = 205.77177104 -- slope:</p>
<p><input checked="" type="radio"/> Load Bin Width File <input type="radio"/> Clear Bin Width Data</p> <p>-- Bin Widths --</p> <p>Filename = <i>bin_width.csv</i> Variable Count = 2 1) elevation 2) slope Bin Widths -- elevation = 6.10668601 -- slope = 0.24888380</p> <p>----- Actual File Text:</p>	<p><input checked="" type="radio"/> Load Eval Points File <input type="radio"/> Clear Eval Points Data</p> <p>-- Eval Points --</p> <p>Filename = <i>eval_points.csv</i> Variable Count = 2 1) elevation 2) slope Bin Count = 4422</p> <p>----- Actual File Text:</p>

Step 3: Identify the layers associated with the input variables. These input variable names are extracted from the files you selected in step [2] above. You may select either raster or polygon vector layers.

Classify Land Facets, Step 3 of 4:

Select Layers that Correspond with Variables:

Variable #1: **elevation**
 elevation.....RASTER

Variable #2: **slope**
 slope.....RASTER

<-- Back Cancel Manual Next -->

Step 4: Enter the fuzziness parameter used in the original FCM analysis (you may also load this value from a file), and the confusion index threshold. Only raster cells with a confusion index below this threshold will be included in the Land Facet raster.

Classify Land Facets, Step 4 of 4:

Fuzzy C-Means Clustering (FCM) is a method for separating data into some pre-determined number of relatively homogeneous clusters. FCM does not simply assign each cell to a cluster, but rather calculates the strength of membership of that cell to all clusters. Cells are generally assigned to the cluster with the highest cluster membership value.

Fuzziness Parameter: The fuzziness parameter φ affects how the algorithm classifies data. When performing the FCM analysis in R, you must

Cluster membership μ for cell i to cluster c , calculated as

$$\mu_{ic} = \frac{\left((d_{ic})^2\right)^{-1/(\varphi-1)}}{\sum_{c=1}^k \left((d_{ic})^2\right)^{-1/(\varphi-1)}}$$

where:

- d_{ic} = Euclidian distance between cell i and cluster c centroid
- φ = Fuzziness parameter (we use $\varphi = 1.5$)
- k = Number of clusters

Confusion Index = $\frac{2^{nd} \text{ Highest membership value}}{\text{Highest membership value}}$

Fuzziness Parameter = 1.5 Load

Confusion Index Threshold = 0.6

<-- Back Cancel Manual OK

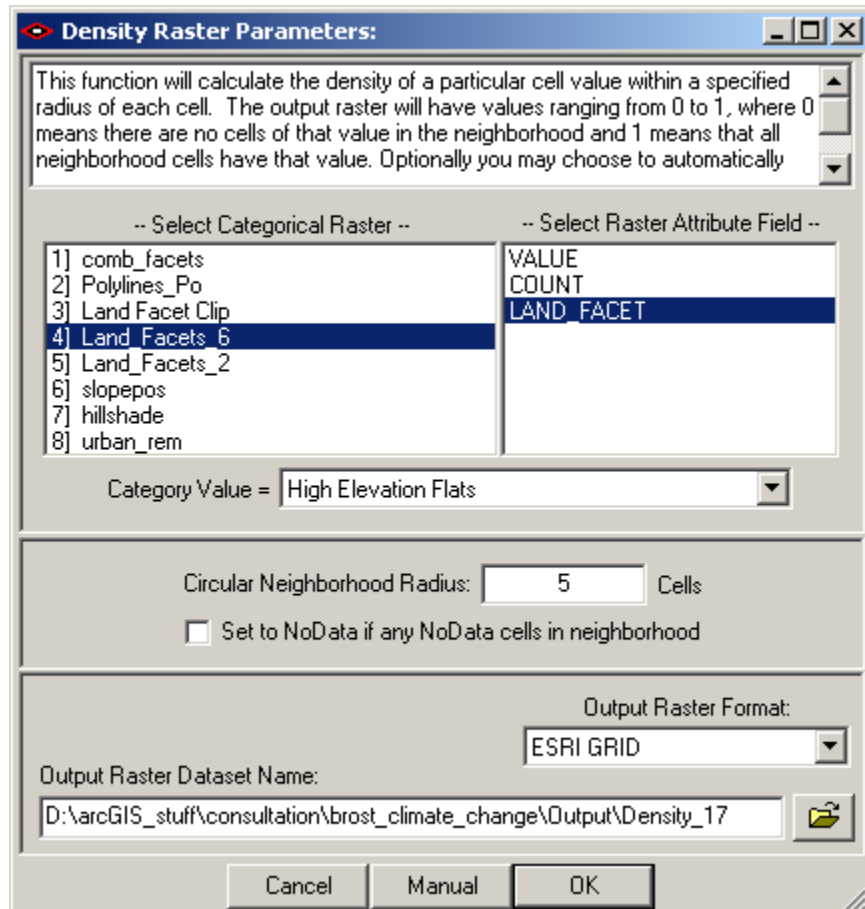
Density Surface Tool:

The land facet density surface reflects the proportion of a neighborhood that is composed of a particular land facet. If half the cells around a particular cell were composed of Land Facet X, then the density of Land Facet X at that point would be 0.5. The density values will range between 0 and 1.

The density surface will be used in two procedures:

1. Areas of high density within Wildland Blocks will be selected as corridor termini (see p. 36), and
2. Density is one of the variables used to build the Mahalanobis Cost Surface (see p. 54)

Click the  button to run the tool.



Density Raster Parameters:

This function will calculate the density of a particular cell value within a specified radius of each cell. The output raster will have values ranging from 0 to 1, where 0 means there are no cells of that value in the neighborhood and 1 means that all neighborhood cells have that value. Optionally you may choose to automatically

-- Select Categorical Raster --	-- Select Raster Attribute Field --
1) comb_facets	VALUE
2) Polyline_Po	COUNT
3) Land Facet Clip	LAND_FACET
4) Land_Facets_6	
5) Land_Facets_2	
6) slopepos	
7) hillshade	
8) urban_rem	

Category Value = High Elevation Flats

Circular Neighborhood Radius: 5 Cells

☐ Set to NoData if any NoData cells in neighborhood

Output Raster Format: ESRI GRID

Output Raster Dataset Name: D:\arcGIS_stuff\consultation\brost_climate_change\Output\Density_17

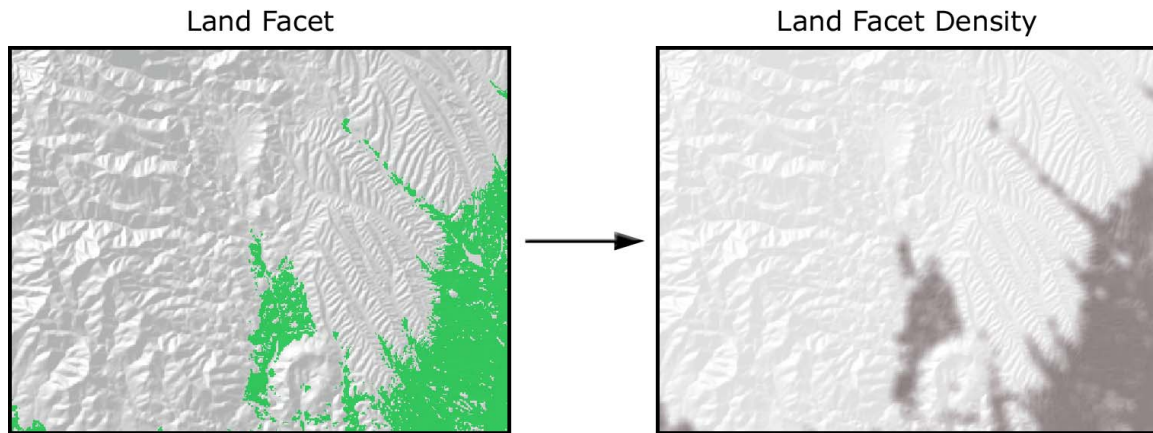
Cancel Manual OK

The “Select Categorical Raster” listbox will contain a list of all rasters that have attribute tables. Chose a raster, then select the appropriate raster attribute field, and finally select the category value you wish to analyze. As you select an attribute field, the category value list will regenerate itself with a list of all unique values in that attribute field.

Choose the neighborhood radius you wish to use. This tool is written to use circular neighborhoods, and the radius units are in cells. The actual neighborhood will consist of all cells whose cell centers are \leq the radius distance of the focal cell center. **Note:** Neighborhood analysis at the edges of the raster are automatically adjusted so that the neighborhood size only reflects the portion of the neighborhood inside the raster. In other words, the density of a cell at

the edge or corner of the raster is only based on those neighborhood cells actually inside the raster.

Optionally you may force the tool to set the density value to NoData if there are any NoData cells in the neighborhood. This option is **not** recommended for the Land Facet corridor functions because NoData cells have infinite resistance in the corridor function, essentially excluding them from corridor analysis. Furthermore, if your land facet type is sparsely distributed across the landscape or you use a large neighborhood, you could end up with a raster composed entirely of NoData cells.



Shannon's Index Tool:

Shannon's Index H is a measure of diversity and evenness that reflects both the number and the balance of unique values within an area (in this case, the area is a moving window). H values increase with both the number of classes observed and with how evenly distributed they are. There are alternative methods for calculating this index and this tool uses the following:

$$\text{Shannon's Index } H = -\sum_{i=1}^S p_i \ln p_i$$

where:

$$p_i = \frac{n_i}{N} = \text{Proportion of observations in land facet } i$$

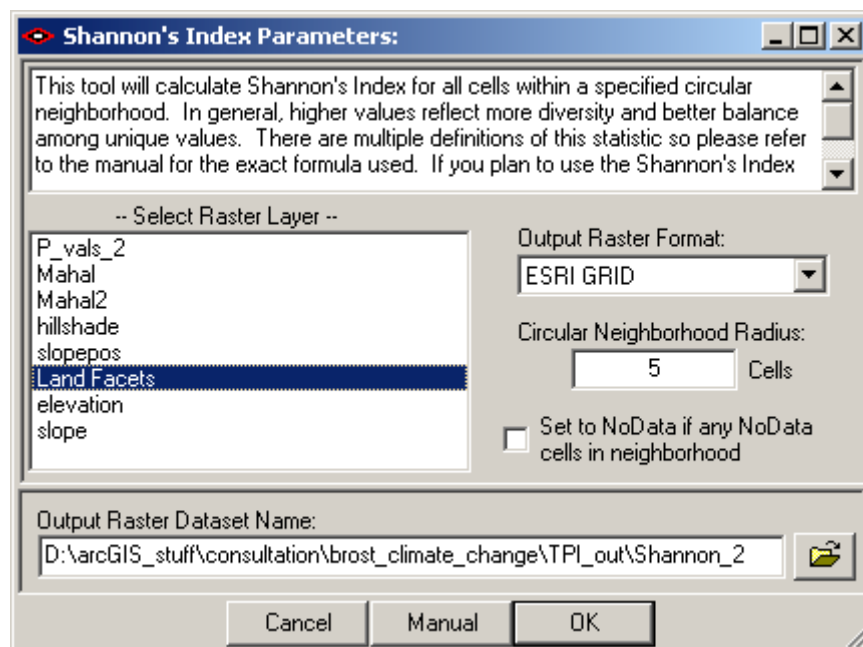
n_i = number of observations in land facet i

N = Total number of observations

S = Number of land facets

By this formula, Shannon's Index values range from 0 to $\ln(S)$, where S = the number of unique categories (i.e. land facets) that occur in the landscape.

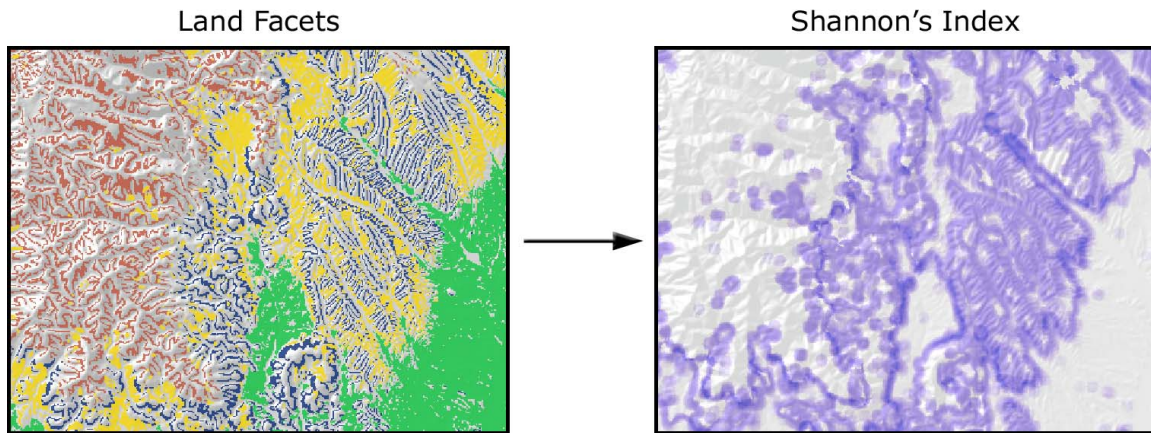
Click the  button to run the tool.



You must select the raster you wish to analyze, the output format for your Shannon's Index Surface, and the neighborhood radius size. This tool uses a circular neighborhood.

If only NoData values are observed in the neighborhood, the tool will assign a Diversity value of 0. Otherwise NoData values will be ignored. NoData values will **not** be counted as an additional "NoData" class. Optionally you may force the tool to assign NoData values if any NoData values are found in the neighborhood.

Click 'OK' and the tool will generate the Shannon's Index raster and add it to your map document.



Identify Termini Polygons Tool:

Corridor polygons do not run simply from the edge of one Wildland Block to the edge of the other Wildland Block, but instead run between land facet polygons within the Wildland Blocks. If there are no land facet polygons within the blocks, then there is little sense in creating a land facet corridor to connect them.

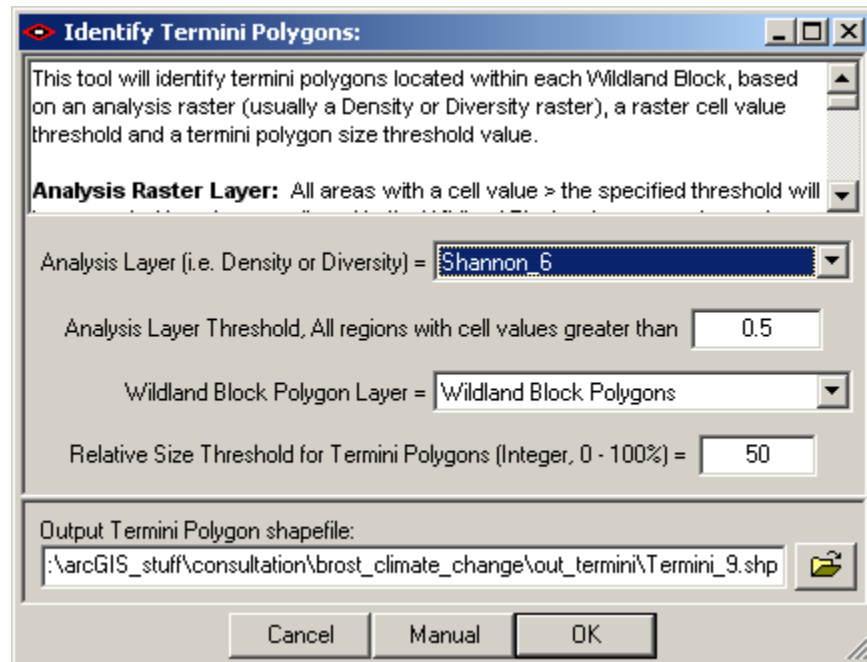
This tool creates land facet termini polygons within the Wildland Blocks based on a raster surface (such as the Density surface [p. 24] or the Shannon's Index surface [p. 34]). All regions with cell values greater than some specified value are considered *eligible* to become termini polygons. In practice, we recommend using $X > 0$ for Density surfaces, and $H' > \text{Median}(H')$ for Diversity surfaces

Not all regions that are *eligible* to become termini polygons are necessarily *desirable* as corridor termini. A very small island of a land facet within a Wildland Block may be too small to be a meaningful corridor terminus. Generally we want to connect the largest concentrations of land facet type within each Wildland Block, and therefore we only want to retain the larger termini polygons.

This tool takes several steps to identify the appropriate termini polygons within each Wildland Block:

1. First it identifies all cells above the specified threshold within each Wildland Block (i.e. with a *Density* value above 0, or with a *Diversity* value above the median value).
2. It then aggregates those cells into disconnected polygons. Cells that touch along an edge or at a corner are considered part of the same polygon.
3. It then calculates the area of the largest polygon within each Wildland Block.
4. Analyzing each Wildland Block separately, it compares the area of each polygon in that Wildland Block with the area of the largest polygon in that block (from Step [3]), and retains only those polygons that are larger than some specified proportion value. For example, if the largest polygon in a Wildland Block was 100 hectares in size, and the user had specified a size threshold of 50%, then the tool would retain all polygons that were ≥ 50 hectares. These polygons are potential termini for the corridor.

Click the  button to run the tool.



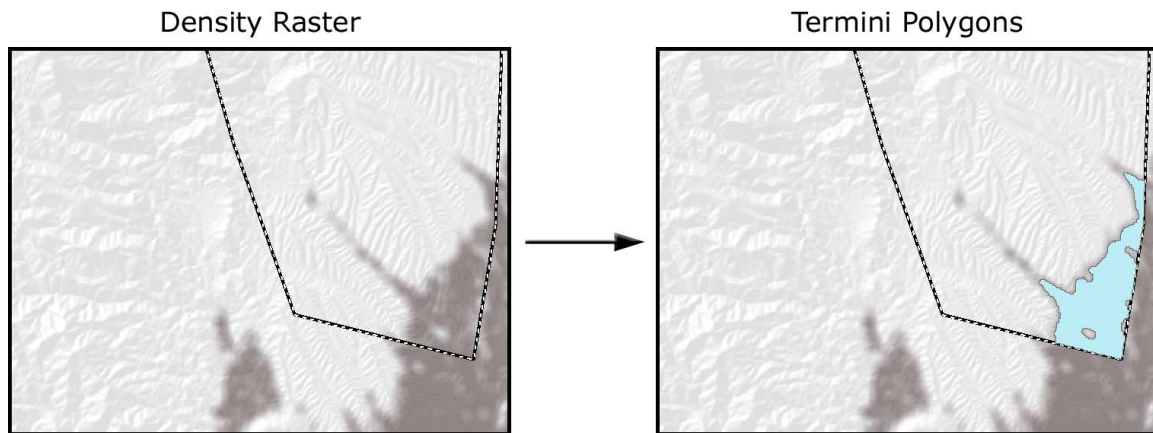
The **Analysis Layer** dropdown box lists all rasters in your active map. Select the raster you wish to analyze (typically a Density or Diversity raster).

The **Analysis Layer Threshold** is the cut-off value. Only portions of the raster greater than this threshold value are converted to polygons. Typically we recommend using a threshold value of 0 for *Land Facet Density* rasters (so that all regions with any density > 0 are used), or a value the median H' value for *Diversity* rasters (so that approximately the greatest 50% of diversity values are used).

The **Wildland Block Polygon Layer** dropdown box lists possible Wildland Block polygon layers in your map. **Note:** Only polygon layers containing **exactly two polygons** are listed! If your Wildland Blocks are not available in this format, then the following standard ArcGIS tools may be helpful:

1. **Append:** If your Wildland Blocks are in separate feature classes, then this tool may be used to add features from one feature class to the other..
Location: *ArcToolbox* → *Data Management Tools* → *General* → *Append*
2. **Merge:** If your Wildland Blocks are in separate feature classes, then this tool may be used to combine them into a new feature class.
Location: *ArcToolbox* → *Data Management Tools* → *General* → *Merge*
3. **Dissolve:** If your Wildland Blocks are composed of multiple discrete polygons, this tool will combine them into a single multi-part polygon object.
Location: *ArcToolbox* → *Data Management Tools* → *Generalization* → *Dissolve*
4. **Multipart to Singlepart:** If both of your Wildland Blocks are combined into a single multi-part object, this tool will split them into separate objects.
Location: *ArcToolbox* → *Data Management Tools* → *Features* → *Multipart to Singlepart*

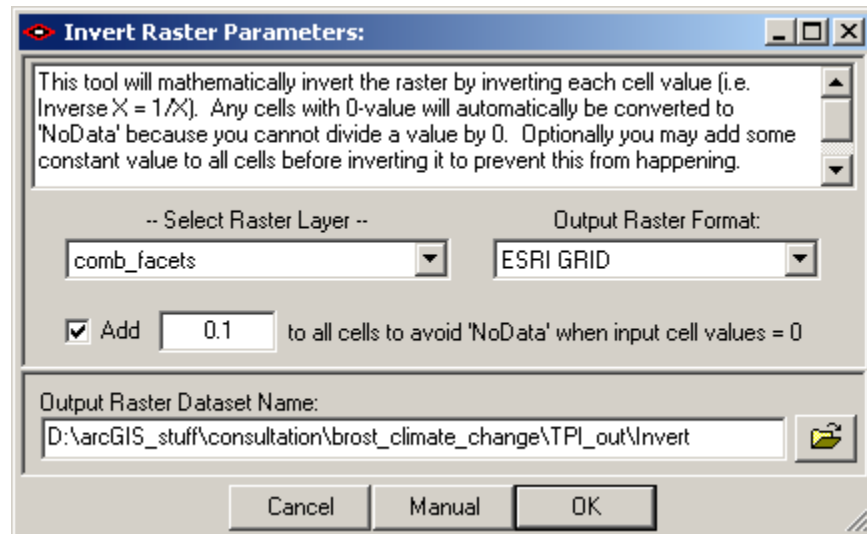
The **Relative Size Threshold for Termini Polygons** specifies how large a polygon must be, as a percent of the size of the largest polygon in the Wildland Block, to be considered a terminus. This value should be between 0 and 100%.



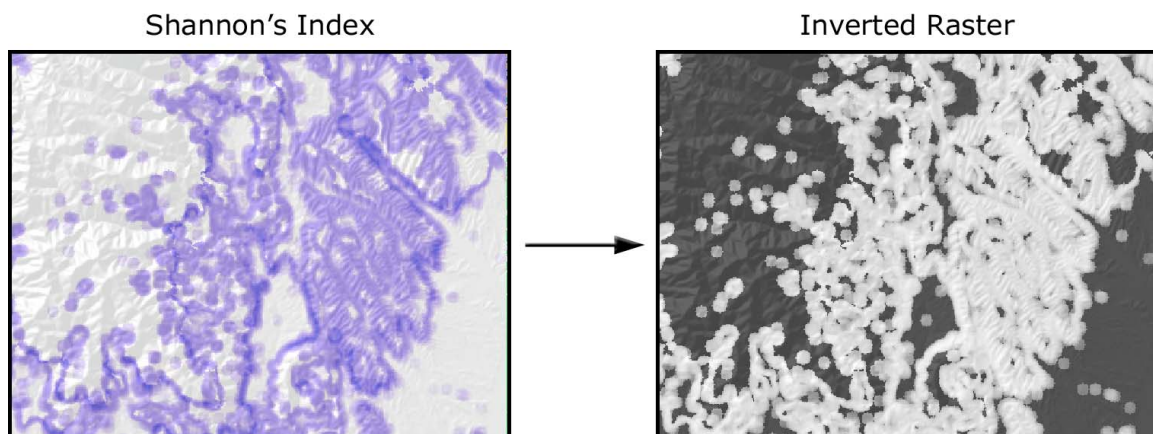
Invert Raster Tool:

This tool will numerically invert any raster (i.e. each new cell value = $\frac{1}{x}$, where x is the original cell value), but it is specifically intended to invert the Shannon's Index raster (see p. 34) in order to use it as a cost surface in Corridor Designer. This tool also lets you add a small constant to each raster value before inverting it, to prevent "division by zero" problems which will result in "NoData" values in your inverted raster. We strongly recommend using this option; we find that 0.1 is a good default value for the constant.

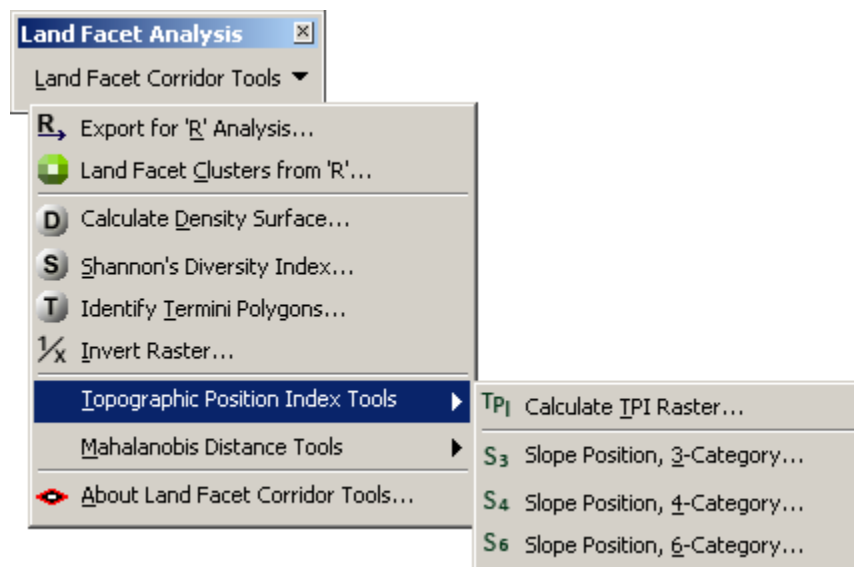
Click the $\frac{1}{x}$ button to run this tool.



Simply select the raster to invert, the output format, whether you wish to add a value to each cell, and finally the output filename. The tool will then invert the raster and add it to your map document.



Topographic Position Index Tools

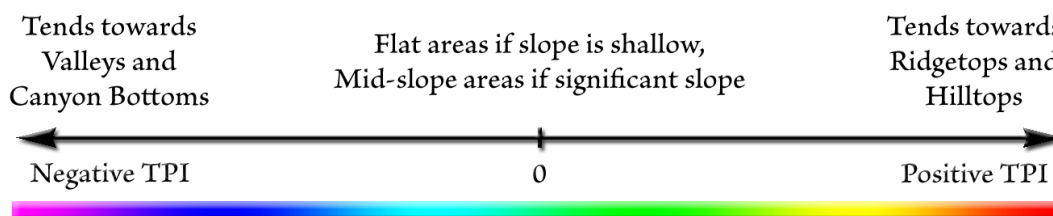


Description

Andrew Weiss presented an interesting and useful poster at the 2001 ESRI International User Conference describing the concept of Topographic Position Index (TPI) and how it could be calculated (Weiss 2001; see also Guisan et al. 1999 and Jones et al. 2000). Using this TPI at different scales, plus slope, users can classify the landscape into both topographic position (i.e. ridge top, valley bottom, mid-slope, etc.) and landform category (i.e. steep narrow canyons, gentle valleys, plains, open slopes, mesas, etc.). **In designing corridors for land facets**, we have simply used the Topographic Position Index to classify the landscape into three broad topographic positions (namely, ridges, canyon bottoms, and slopes), but we describe other options for users that may wish to use TPI in other ways.

The algorithms are clever and fairly simple. The TPI is the basis of the classification system and is simply the difference between a cell elevation value and the average elevation of the neighborhood around that cell. Positive values mean the cell is higher than its surroundings while negative values mean it is lower.

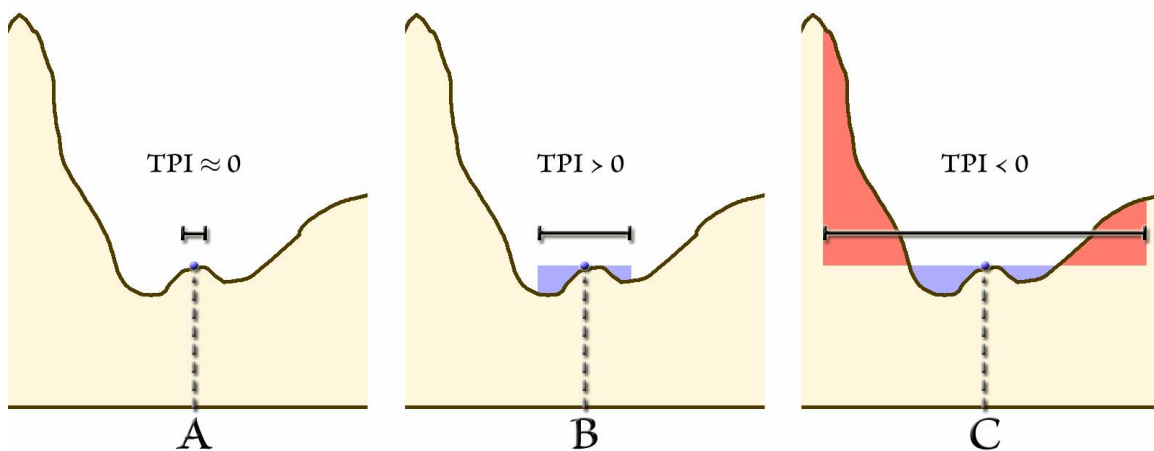
The degree to which it is higher or lower, plus the slope of the cell, can be used to classify the cell into slope position. If it is significantly higher than the surrounding neighborhood, then it is likely to be at or near the top of a hill or ridge. Significantly low values suggest the cell is at or near the bottom of a valley. TPI values near zero could mean either a flat area or a mid-slope area, so the cell slope can be used to distinguish the two.



SCALES AND NEIGHBORHOODS: TPI is naturally scale-dependent. The same point at the crest of a mountain range might be considered a ridgetop to a highway construction crew or a flat plain to an insect living in the soil. The classifications produced by this tool depend entirely on the scale you use to analyze the landscape.

For example, in the illustration below, TPI is calculated for the same point on the landscape using 3 different scales. In each case, the point is located on top of a small hill set inside a larger valley. In Case A, the scale is small enough that the point is at about the same elevation as the entire analysis region so the TPI value would be approximately 0. In Case B, the analysis region is big enough to encompass the entire small hill, and the point is consequently much higher than its neighbors and has a correspondingly high TPI value. In Case C, the neighborhood includes the hills on either side of the valley, and therefore the point is lower than its neighbors and has a negative TPI value.

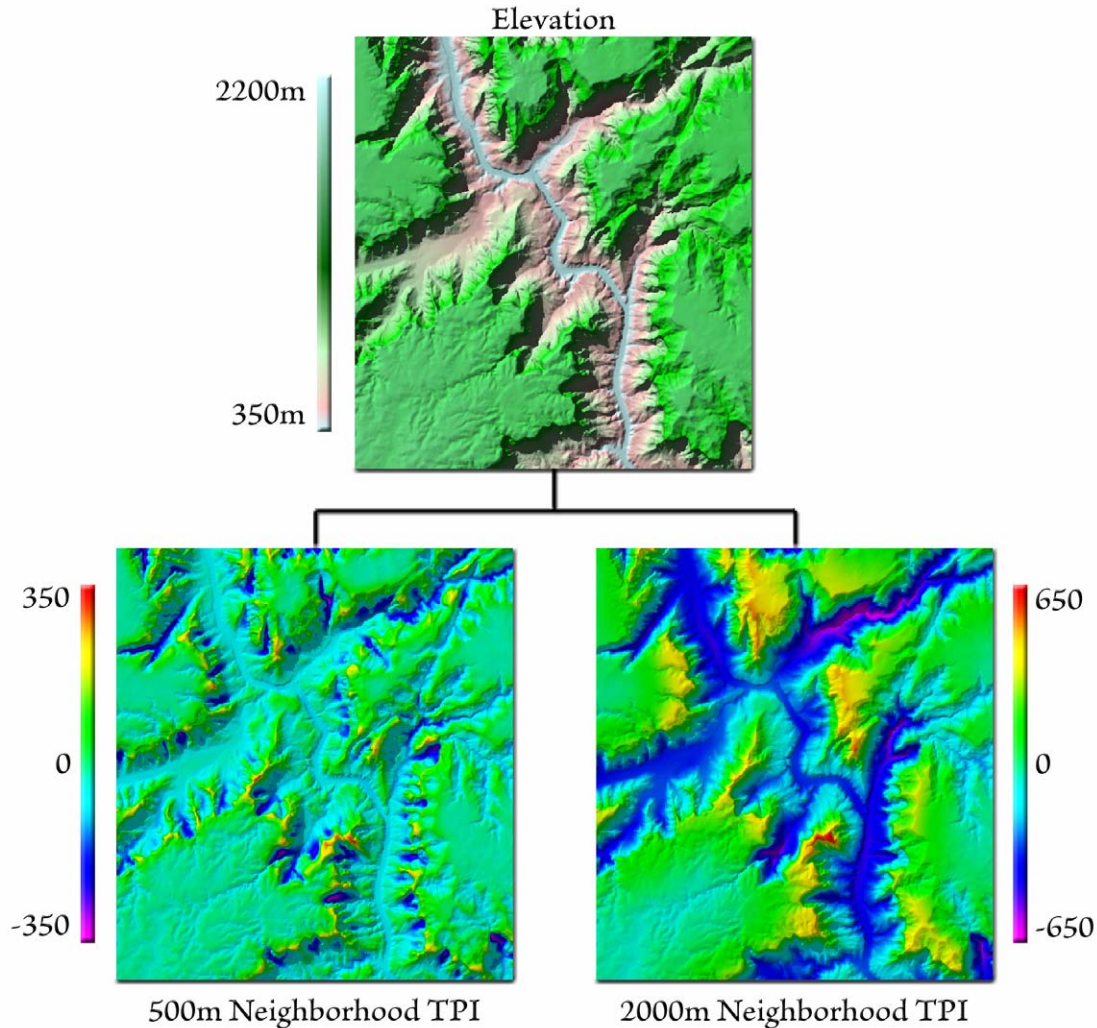
TPI Values at 3 Different Scales



Users should consider what scale is most relevant for the phenomenon being analyzed. If you are interested in topographic habitat characteristics of large, wide-ranging animals, you would likely define your landscape classifications in terms of large, distinctive topographic features. Cougars, for example, may be influenced by a tall ridgeline on the horizon more than by minor ripples immediately surrounding them. Furthermore, a point on top of a small hill at the bottom of a canyon may be classified as a canyon bottom at one scale, or a hilltop at a different scale. Both are valid classifications; the user must decide what scale is reasonable for their analysis.

Scale is determined by the neighborhood used in the analysis. The TPI values reflect the difference between the elevation in a particular cell and the average elevation of the cells around that cell. The Neighborhood defines what cells are considered to be “around” that cell.

In the illustration below, TPI values were calculated using 2 different neighborhoods. The left example used a circular neighborhood with a 500m radius, meaning that the TPI value for each cell reflected the difference between the elevation of that cell and the average elevation of all cells within 500m of that cell. The example on the right used a circular neighborhood with a 2000m radius.



These examples used circular neighborhoods, but other options are available. Weiss' examples used annular (ring- or doughnut-shaped) neighborhoods where only cells within a specified distance range are considered. Some researchers use rectangular neighborhoods, although in most cases circular or annular neighborhoods are more reasonable.

Wedge-shaped neighborhoods are useful for restricting your analysis to a particular direction. Weiss' poster discusses some ideas for future research in which he plans to compare directional TPI values in order to distinguish saddles from flat areas, ridges from hilltops and valleys from local depressions, as well as identify the general aspect of landforms.

CLASSIFYING BY TOPOGRAPHIC POSITION: TPI values can easily be classified into topographic position classes based on (a) how much a pixel's elevation differs from the mean of its neighbors and (b) the steepness (slope angle) at each point. There are a couple of strategies you can take to do this.

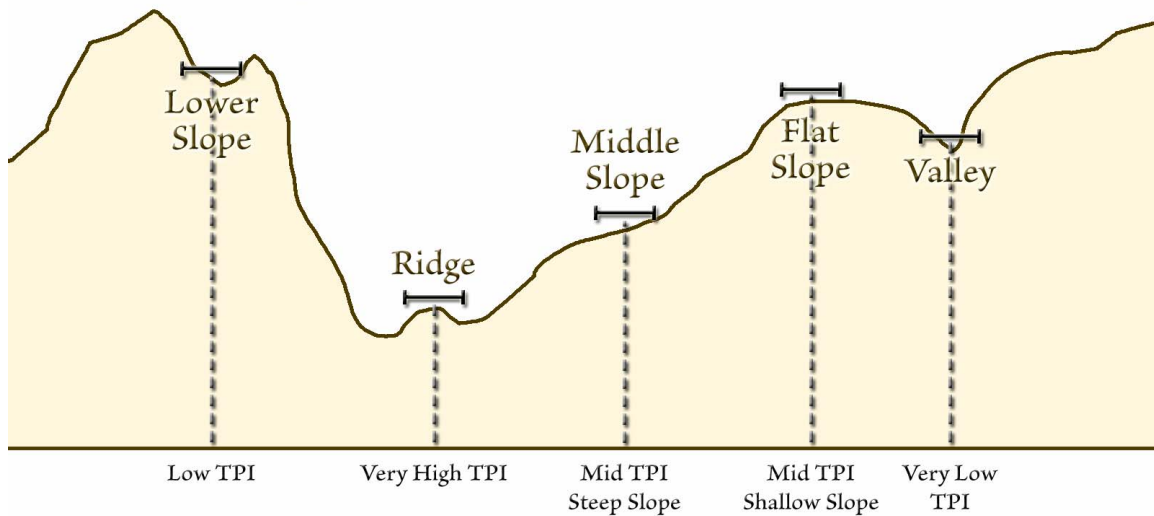
The easiest way is simply to set threshold values for the TPI grids themselves. TPI values above a certain threshold might be classified as ridgetops or hilltops, while TPI values below a threshold might be classified as valley bottoms or depressions. TPI values near 0 could be classified as flat plains (if the slope angle is near 0) or as mid-slope areas (if steeper than a specified threshold).

Dickson and Beier (2006) used this method in a study of the influences of topography on cougar movement.

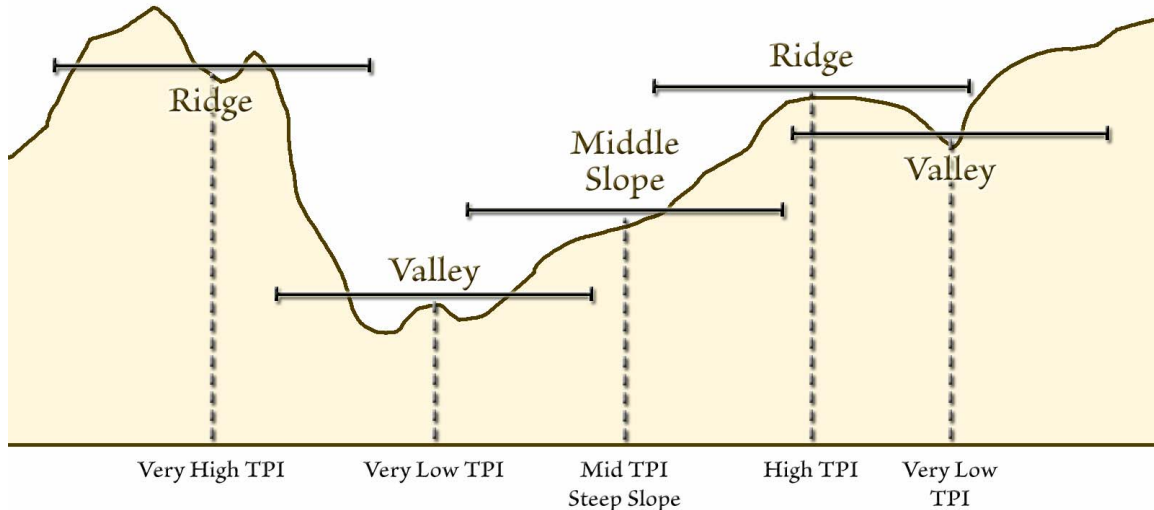
A somewhat more sophisticated method, illustrated by Weiss in his poster, is to define threshold TPI values in terms of standard deviations from the elevation, which therefore take into account the variability of elevation values within that neighborhood. This means that grid cells with identical TPI value may be classified differently in different areas, depending on the variability in their respective neighborhoods. This method may or may not be useful in your analysis. You would use this method if you felt that cells with high neighborhood elevation variability should have to meet a higher TPI threshold in order to be classified into some category.

As with TPI values in general, neighborhood size is also a critical component of the Slope Position classification process. Small neighborhoods capture small and local hills and valleys while large neighborhoods capture larger-scale features.

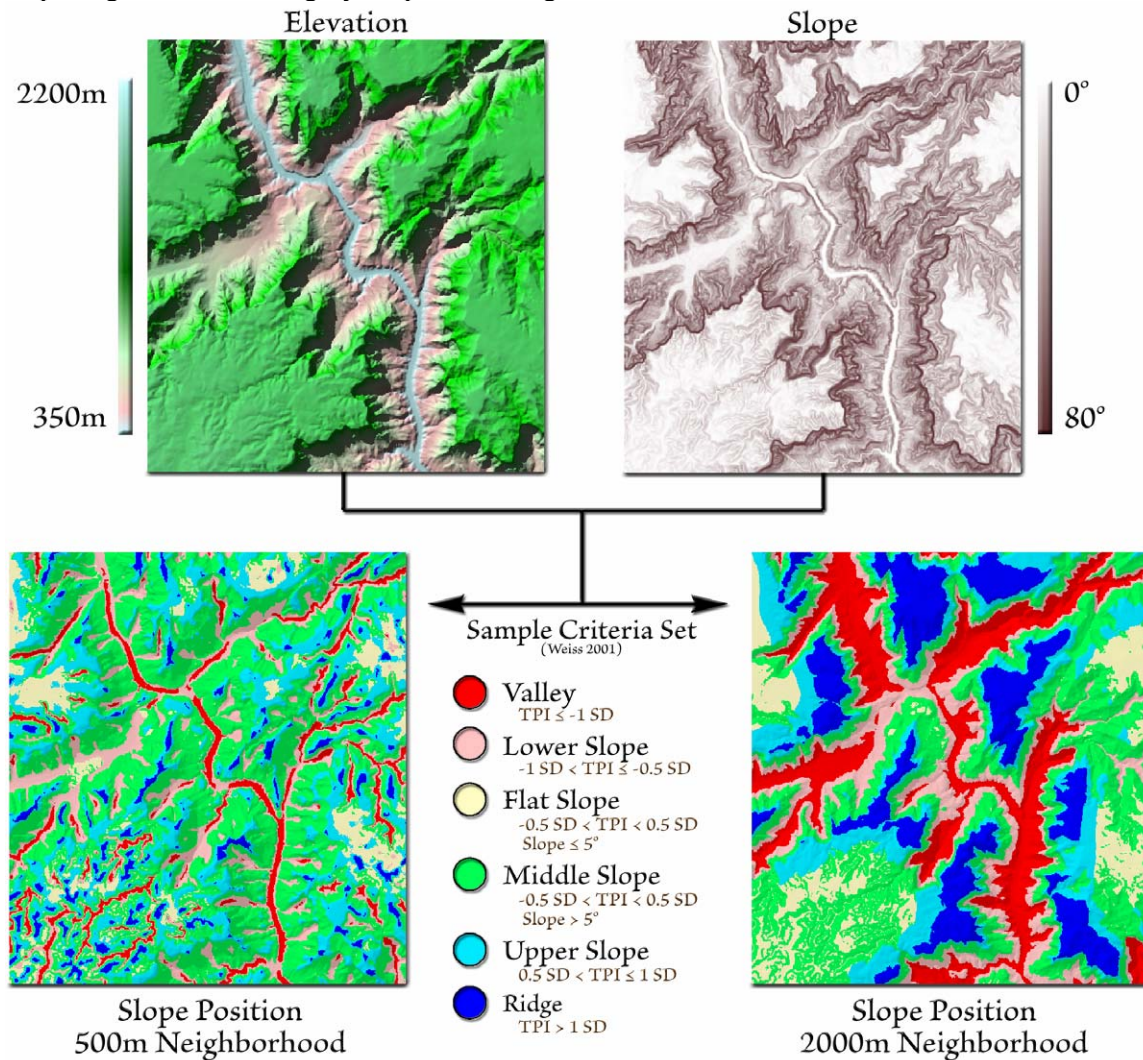
Small-Neighborhood Slope Position Classification



Large-Neighborhood Slope Position Classification



TPI values near 0 mean only that the elevation is close to the mean elevation of the neighborhood cells, and this could happen if that cell is in a flat area or if it is on a slope. An easy way to distinguish between these 2 possibilities is to check the slope angle at that point. If the angle is near 0, then the point is probably on a flat area. A high slope angle means that the point is on a slope. In his poster, Weiss demonstrates one possible classification process using both TPI and slope to generate a 6-category Slope Position grid:



TPI Types:

This tool offers three variations of TPI.

1. **TPI:** This is the traditional definition of TPI, where each cell is defined as the difference between the elevation cell value and the average elevation of all cells in the neighborhood. TPI units are in elevation units, such that a TPI value of 10 would mean that this particular cell is 10 units (generally meters or feet) higher than the average elevation of the neighborhood.
2. **Standardized Elevation:** This is very similar to TPI, but taken one step farther. This takes the TPI (defined as [Elevation cell value – Neighborhood Average Elevation]), and divides it by the Neighborhood Standard Deviation. Units are in standard deviations,

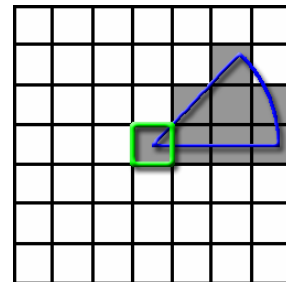
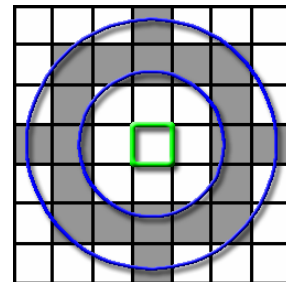
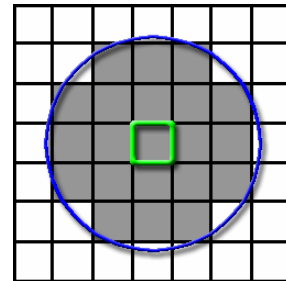
such that a Standardized Elevation value of 1 would mean that this particular cell is 1 standard deviation higher than the average elevation in the neighborhood.

3. **Standardized TPI:** This option takes the TPI values from option 1 above, and standardizes them by the mean and standard deviation of all TPI values in the raster. A value of 1 would imply that this cell is one standard deviation higher than the average TPI value of the entire TPI raster. **Note:** This option is probably less useful than Options 1 and 2 in most analyses, and we only offer it because users have requested it. This particular option can classify ridges as valleys and vice versa. In most types of analyses Options 1 and 2 will make far more sense.

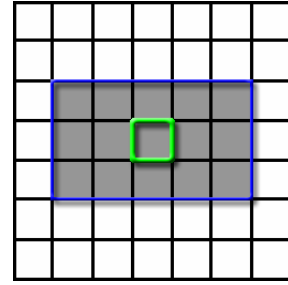
Neighborhood Types:

When generating TPI or Slope Classification rasters, you will be asked to define your neighborhood. You can choose between a circle, annulus (doughnut-shape), rectangle or wedge. You can also enter your neighborhood parameters in units of either grid cells or map units (i.e. meters, feet, etc.).

1. Circle: A circular neighborhood defined by a radius length extending outward from the cell center. This neighborhood is composed of all grid cells whose cell centers lie within that distance of the focal cell center.
2. Annulus: An annular neighborhood looks like a ring or doughnut defined by an inner and outer radius length extending outward from the cell center. This neighborhood is composed of all cells whose cell centers lie within this ring.
3. Wedge: A wedge-shaped neighborhood looks like a slice of pie cut out of a circular neighborhood and is defined by a starting angle, and ending angle, and a radius.

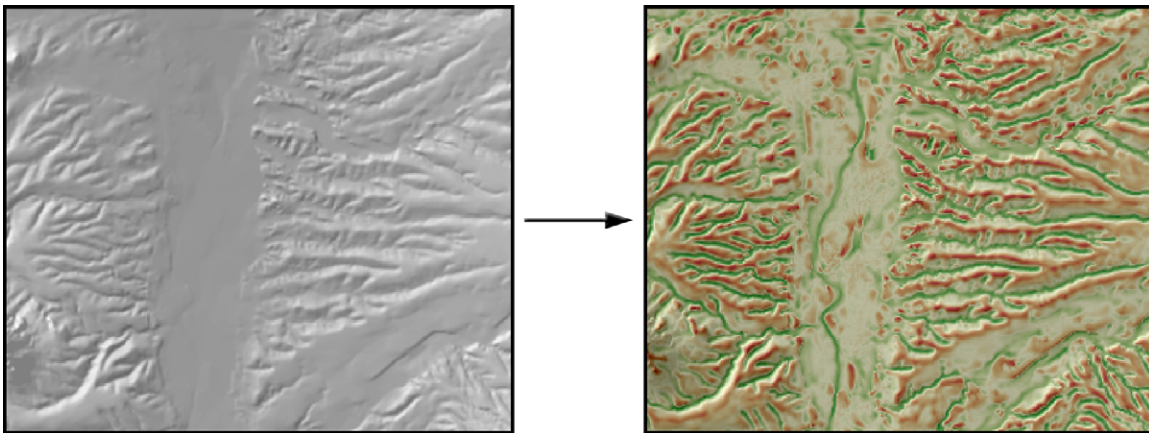


4. Rectangle: A square or rectangular neighborhood defined by width and height, which will be centered around your focal cell center. Cells will be included in the neighborhood if the cell centers lie within this rectangle.



Using the tools:

CALCULATE A TPI RASTER: This tool simply converts an elevation (DEM) raster into a TPI raster. No further classification or categorization is done

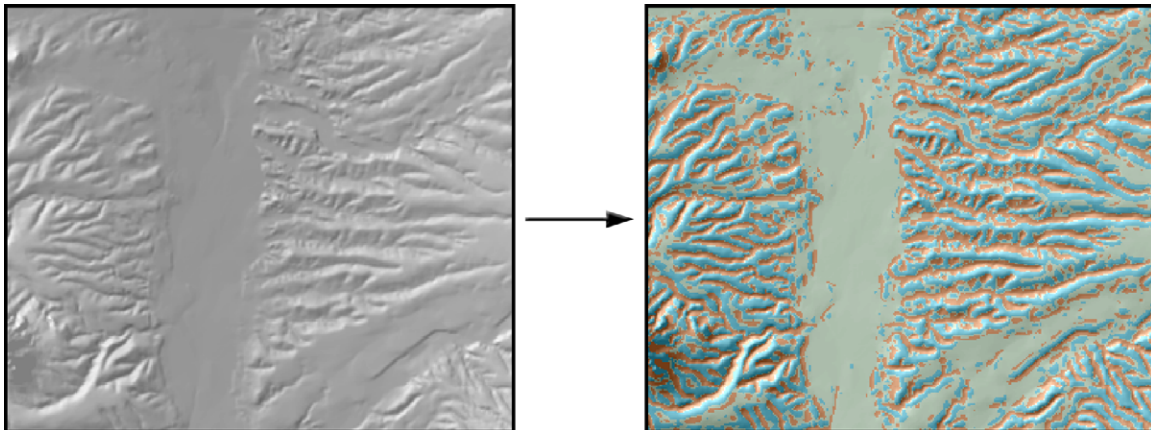



Click the  button to run the tool.

The dialog box is titled "Topographic Position Index Parameters:". It contains a text area with the following text: "The topographic position index reflects the difference in elevation between a focal cell and all cells in the neighborhood. This tool offers three methods for calculating TPI, which differ in units of the final TPI raster. 1) Type TPI: Units are in elevation units (usually meters or feet)". Below the text area are two dropdown menus: "-- Select DEM Raster Layer --" with "elevation" selected, and "-- Select TPI Type --" with "Standardized Elevation" selected. Below these are two sections: "Neighborhood Shape" with a "Circle" dropdown, "Neighborhood Size Units" with a "Cells" dropdown, and "Radius =" with a value of "5". There is also a checkbox labeled "Set to NoData if any NoData cells in neighborhood" which is currently unchecked. Below these sections is a section for "Output Raster Format:" with a dropdown set to "ESRI GRID". Below that is a text field for "Output Raster Dataset Name:" containing the path "D:\arcGIS_stuff\consultation\brost_climate_change\Output\TPI_2". At the bottom are three buttons: "Cancel", "Manual", and "OK".

Simply select your analysis parameters and click 'OK'. Please see the sections above on TPI types (p. 44) and Neighborhood types (p. 45) if you have any questions on these parameters. The output raster will be a continuous floating-point raster.

CREATE A 3-CATEGORY TOPOGRAPHIC POSITION RASTER:



This tool will create a 3-class Topographic Position raster based on TPI values. Click the  button to run the tool. **We used this tool in all of our land facet analyses.**

3-Category Slope Position Parameters:

This tool will create a 3-category Slope Classification raster based solely on the Topographic Position Index of each cell. Depending on your threshold values, low TPI values will be classified as "Canyons", TPI values around 0 will be classified as "Slopes", and high TPI values will be classified as "Ridges". You may change the

Class 1: Canyons
TPI <= [-1] units

Class 2: Slopes
[-1] units < TPI <= [1] units

Class 3: Ridges
TPI > [1] units

-- Select DEM Raster Layer --
Slope_4_3

-- Select TPI Type to create --
Standardized Elevation

Neighborhood Options

Neighborhood Shape
Circle

Neighborhood Size Units
Cells

Radius = 5

[A] = -1 [B] = 1

☐ Set to NoData if any NoData cells in neighborhood

Output Raster Format: ESRI GRID

Output Raster Dataset Name:
D:\arcGIS_stuff\consultation\brost_climate_change\TPI_out\Slope_3_4

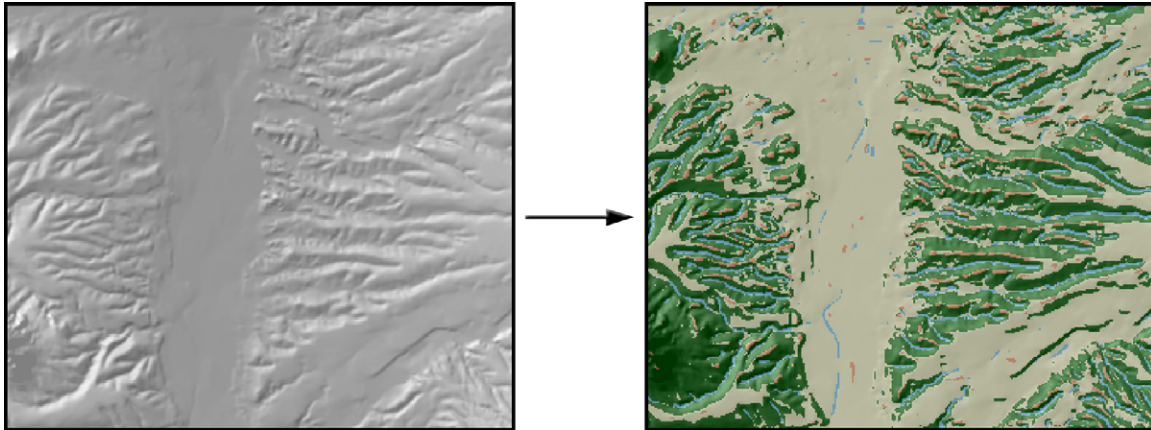
The three classes are named *Canyons*, *Slopes* and *Ridges* by default, but you can change the names by clicking the “Reset Class Names” button. In general, the classes are defined as follows:

Canyons: $TPI \leq [A]$
Slopes: $[A] < TPI \leq [B]$
Ridges: $TPI > [B]$

where **[A]** and **[B]** are threshold TPI values set by the user. The threshold units should be the same as the units of the TPI type. Please see the sections above on TPI types (p. 44) and Neighborhood types (p. 45) if you have any questions on these parameters. The output raster will be a 3-Category Integer raster with the class names in the attribute table.

In our work designing land facet corridors, we experimented with various neighborhood sizes in three diverse landscapes. A radius of 5 cells produced land facets that made sense to end-users who were familiar with the landscapes we analyzed. We used “raw” (not standardized) TPI. We typically used -6 m and +6 m for A and B, respectively, but users should experiment with values that work in their landscapes.

CREATE A 4-CATEGORY TOPOGRAPHIC POSITION RASTER:



This tool will create a 4-class Topographic Position raster based on combinations of TPI values and Slope Angle. Click the **S4** button to run the tool.

4-Category Slope Position Parameters:

This tool will create a 4-category Slope Classification raster based on the Topographic Position Index and the Slope of each cell. Depending on your threshold values, low TPI values will be classified as "1) Canyons", TPI values around 0 will be classified as either "2) Gentle Slopes" or "3) Steep Slopes"

Class 1: 1) Canyons
TPI \leq [-1] units

Class 2: 2) Gentle Slopes
[-1] units $<$ TPI \leq [1] units
Slope \leq [6] degrees

Class 3: 3) Steep Slopes
[-1] units $<$ TPI \leq [1] units
Slope $>$ [6] degrees

Class 4: 4) Ridges
TPI $>$ [1] units

[A] = [-1] [B] = [1]
[S] = [6]

Reset Class Names ☐ Set to NoData if any NoData cells in neighborhood

-- Select DEM Raster Layer --
DEM

-- Select TPI Type to create --
TPI

Neighborhood Options
Neighborhood Shape: Circle
Neighborhood Size Units: Cells
Radius = 5

Output Raster Format: ESRI GRID

Output Raster Dataset Name:
D:\arcGIS_stuff\consultation\brost_climate_change\TPI_out\Slope_4

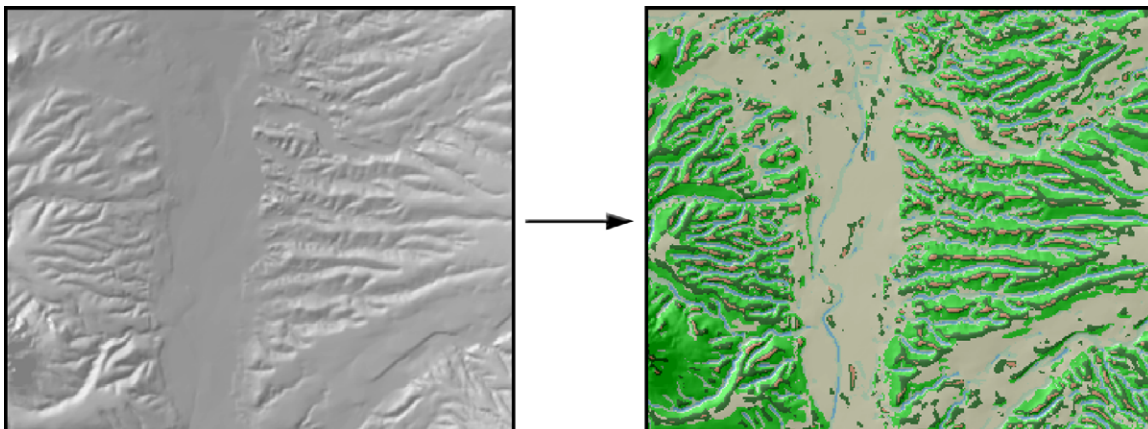
Cancel Manual OK

The four classes are named *Canyons*, *Gentle Slopes*, *Steep Slopes* and *Ridges* by default, but you can change the names by clicking the “Reset Class Names” button. In general, the classes are defined as follows:

Canyons: $TPI \leq [A]$
Gentle Slopes: $[A] < TPI \leq [B]$, $Slope\ Angle < [S]^{\circ}$
Steep Slopes: $[A] < TPI \leq [B]$, $Slope\ Angle \geq [S]^{\circ}$
Ridges: $TPI > [B]$

where **[A]** and **[B]** are threshold TPI values and **[S]** is the threshold slope angle. TPI threshold units should be the same as the units of the TPI type, and Slope angle threshold units should be in Degrees. Please see the sections above on TPI types (p. 44) and Neighborhood types (p. 45) if you have any questions on these parameters. The output raster will be a 4-Category Integer raster with the class names in the attribute table.

CREATE A 6-CATEGORY TOPOGRAPHIC POSITION RASTER:



This tool will create a 6-class Topographic Position raster based on TPI values and Slope Angle. Click the **S6** button to run the tool.

6-Category Slope Position Parameters:

This tool will create a 6-category Slope Classification raster based on the Topographic Position Index and the Slope of each cell. Depending on your threshold values, extreme low TPI values will be classified as "Valleys", moderately low TPI values will be classified as "Lower Slopes", TPI values around 0 will be

Class 1: Valleys
TPI \leq [-1] units

Class 2: Lower Slopes
[-1] units < TPI \leq [-0.5] units

Class 3: Gentle Slopes
[-0.5] units < TPI \leq [0.5] units
Slope \leq [5] degrees

Class 4: Steep Slopes
[-0.5] units < TPI \leq [0.5] units
Slope > [5] degrees

Class 5: Upper Slopes
[0.5] units < TPI \leq [1] units

Class 6: Ridges
TPI > [1] units

-- Select DEM Raster Layer --
Slope_4_3

-- Select TPI Type to create --
Standardized Elevation

Neighborhood Options

Neighborhood Shape
Circle

Neighborhood Size Units
Cells

Radius = 5

[A] = -1 [B] = -0.5
[C] = 0.5 [D] = 1
[S] = 5

Reset Class Names ☐ Set to NoData if any NoData cells in neighborhood

Output Raster Format: ESRI GRID

Output Raster Dataset Name:
D:\arcGIS_stuff\consultation\brost_climate_change\TPI_out\Slope_6_3

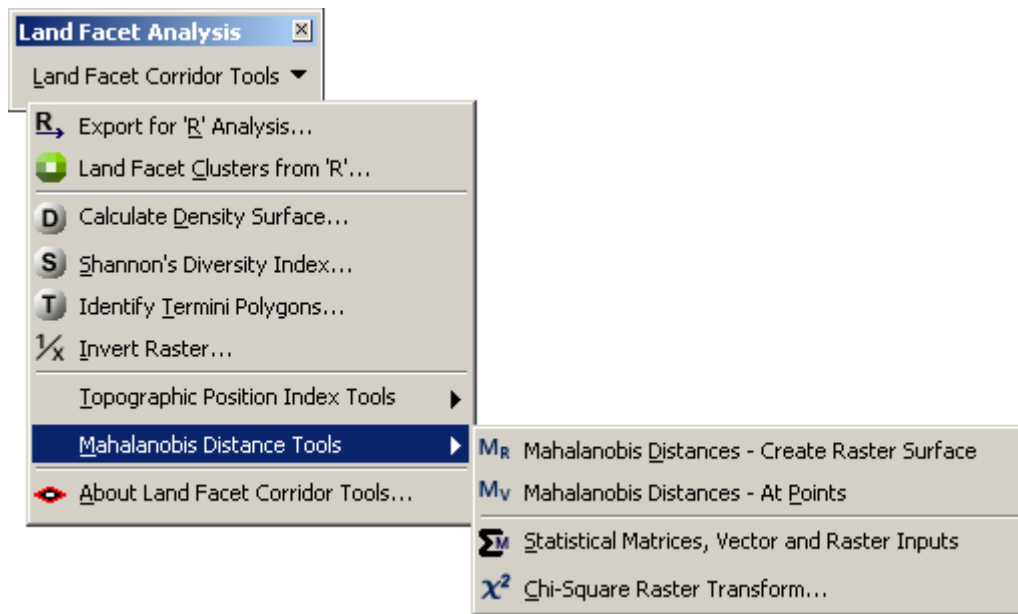
Cancel Manual OK

The six classes are named *Valleys*, *Lower Slopes*, *Gentle Slopes*, *Steep Slopes*, *Upper Slopes* and *Ridges* by default, but you can change the names by clicking the “Reset Class Names” button. In general, the classes are defined as follows:

Valleys: $TPI \leq [A]$
Lower Slopes: $[A] < TPI \leq [B]$
Gentle Slopes: $[B] < TPI \leq [C]$, *Slope Angle* $< [S]^{\circ}$
Steep Slopes: $[B] < TPI \leq [C]$, *Slope Angle* $\geq [S]^{\circ}$
Upper Slopes: $[C] < TPI \leq [D]$
Ridges: $TPI > [D]$

where **[A]**, **[B]**, **[C]** and **[D]** are threshold TPI values and **[S]** is the threshold slope angle. TPI threshold units should be the same as the units of the TPI type, and Slope Angle threshold should be in Degrees. Please see the sections above on TPI types (p. 44) and Neighborhood types (p. 45) if you have any questions on these parameters. The output raster will be a 6-Category Integer raster with the class names in the attribute table.

Mahalanobis Distance Tools



Discussion of Mahalanobis Distances:

GENERAL CONCEPTS:

Mahalanobis distances provide a powerful tool for describing how similar some set of conditions is to an “ideal” or “prototypical” set of conditions, and can be very useful for identifying which regions in a landscape are most similar to a prototype (in this case, a land facet).

For example, in the field of wildlife biology we might define an “ideal” landscape as that which best fits the niche of some wildlife species. Through observation, we may find that a wildlife species typically occurs within a particular elevation range, on slopes of a particular steepness, and perhaps within a certain vegetation density. Using Mahalanobis distances, we can quantitatively describe the entire landscape in terms of how similar it is to the ideal elevation, slope and vegetation density of that animal.

Moreover, Mahalanobis distances are based on both the mean and variance of the predictor variables, plus the covariance matrix of all the variables, and therefore take advantage of the variable covariance. The region of constant Mahalanobis distance around the mean forms an ellipse in 2D space (i.e. when only 2 variables are measured), or an ellipsoid or hyperellipsoid when more variables are used.

Mahalanobis distances are calculated as:

$$D^2 = (\mathbf{x} - \mathbf{m})^T \mathbf{C}^{-1} (\mathbf{x} - \mathbf{m})$$

where:

D^2 = Mahalanobis distance

\mathbf{x} = Vector of data

\mathbf{m} = Vector of mean values of independent variables

\mathbf{C}^{-1} = Inverse Covariance matrix of independent variables

\mathbf{T} = Indicates vector should be transposed

For example, suppose we took a single observation from a bivariate population with Variable X and Variable Y, and that our two variables had the following characteristics:

Variable X: mean = 500, SD = 79.32

Variable Y: mean = 500, SD = 79.25

Variance/Covariance Matrix		
	X	Y
X	6291.55737	3754.32851
Y	3754.32851	6280.77066

If, in our single observation, X = 410 and Y = 400, we would calculate the Mahalanobis distance for that single value as:

Given that Mahalanobis Distance $D^2 = (\mathbf{x} - \mathbf{m})^T \mathbf{C}^{-1} (\mathbf{x} - \mathbf{m})$

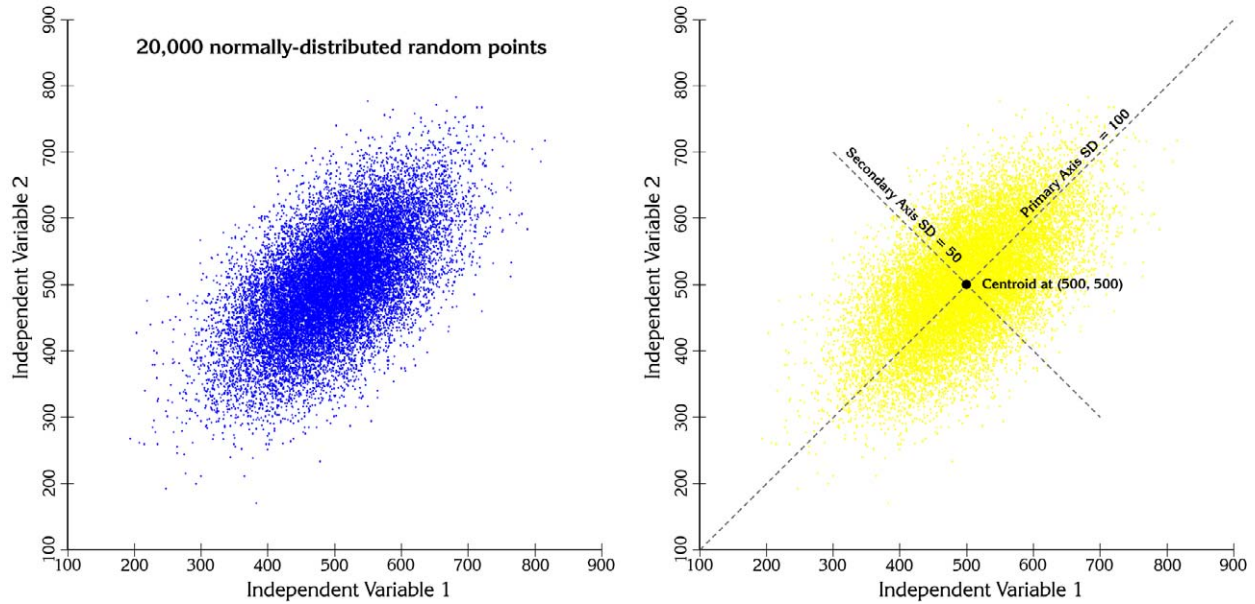
$$(\mathbf{x} - \mathbf{m}) = \begin{pmatrix} 410 - 500 \\ 400 - 500 \end{pmatrix} = \begin{pmatrix} -90 \\ -100 \end{pmatrix}$$

$$\mathbf{C}^{-1} = \begin{pmatrix} 6291.55737 & 3754.32851 \\ 3754.32851 & 6280.77066 \end{pmatrix}^{-1} = \begin{pmatrix} 0.00025 & -0.00015 \\ -0.00015 & 0.00025 \end{pmatrix}$$

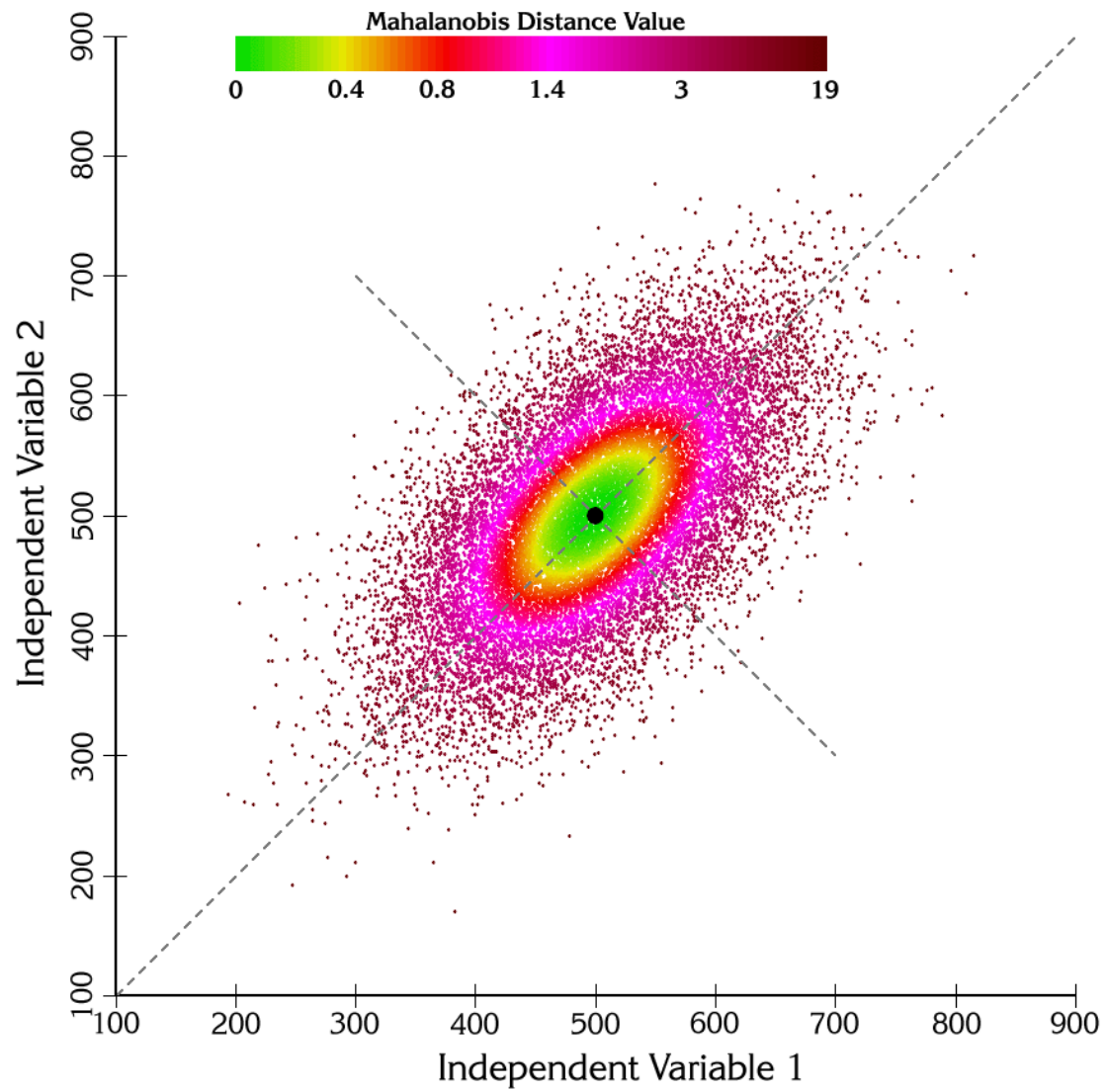
$$\begin{aligned} \text{Therefore } D^2 &= (-90 \quad -100) \times \begin{pmatrix} 0.00025 & -0.00015 \\ -0.00015 & 0.00025 \end{pmatrix} \times \begin{pmatrix} -90 \\ -100 \end{pmatrix} \\ &= 1.825 \end{aligned}$$

Therefore, our single observation would have a distance of 1.825 standardized units from the mean (mean is at X = 500, Y = 500).

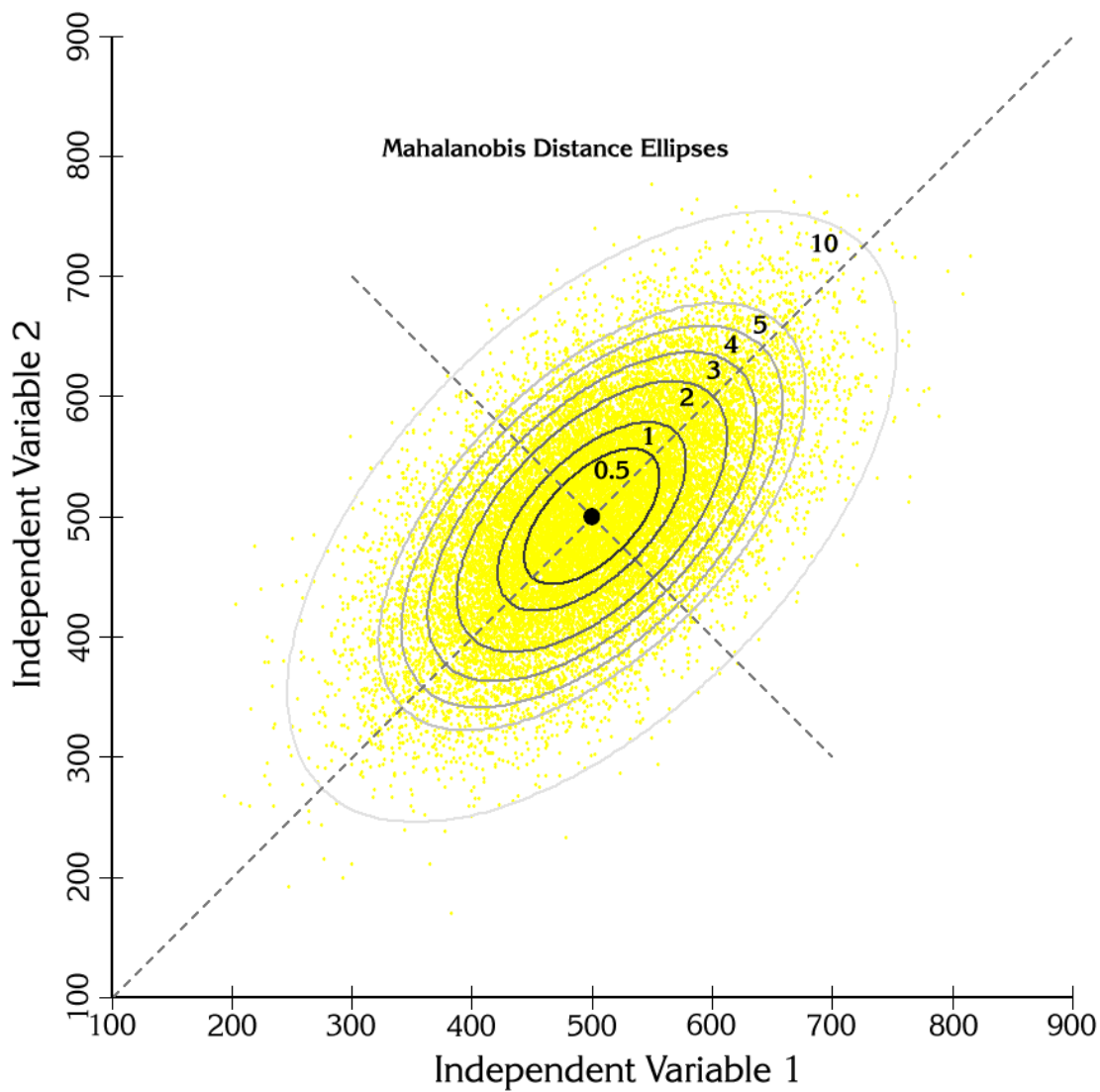
If we took many such observations, graphed them and colored them according to their Mahalanobis values, we can see the elliptical Mahalanobis regions come out. For example, the cloud of data points below are randomly generated from the bivariate population described above:



If we calculate Mahalanobis distances for each of these points and shade them according to their distance value, we see clear elliptical patterns emerge:



We can also draw actual ellipses at regions of constant Mahalanobis values:



One interesting feature to note from this figure is that a Mahalanobis distance of 1 unit corresponds to 1 standard deviation along both primary axes of variance.

RE-SCALING MAHALANOBIS DISTANCES USING CHI-SQUARE P-VALUES:

Mahalanobis distances are occasionally converted to Chi-square p -values for analysis (see Clark et al. 1993). When the predictor variables are normally distributed, the Mahalanobis distances do follow the χ^2 distribution with $N - 1$ degrees of freedom (where $N = \#$ of habitat variables; 2 in the example above). Although wildlife habitat variables often fail to meet the assumption of normality (Farber and Kadmon 2003), the conversion to Chi-square p -values is nonetheless a valid way to re-scale Mahalanobis distances to a 0-1 scale. Mahalanobis distances themselves have no upper limit, so this rescaling may be convenient for some analyses.

In general, the p -value reflects the probability of seeing a Mahalanobis value as large or larger than the actual Mahalanobis value, assuming the vector of predictor values that produced that Mahalanobis value was sampled from a population with an ideal mean (i.e. equal to the vector of

mean predictor variable values used to generate the Mahalanobis value). P -values close to 0 reflect high Mahalanobis distance values and are therefore very dissimilar to the ideal combination of predictor variables. P -values close to 1 reflect low Mahalanobis distances and are therefore very similar to the ideal combination of predictor variables. The closer the p -value is to 1, the more similar that combination of predictor values is to the ideal combination.

Because P -values close to 0 correspond with high Mahalanobis values, while P -values close to 1 correspond with low Mahalanobis values, this transformation also inverts the order of values. High cell values in the P -value raster surface will correspond with low values in the Mahalanobis raster and vice versa.

APPLICATIONS TO LANDSCAPE ANALYSIS:

Suppose we have a grid of elevation values and a grid of slope values, and we are interested in identifying those regions on the landscape that have similar slopes and elevations to a mean slope and elevation characteristic of a land facet:

:

$$\text{Vector of Mean Values} = \begin{pmatrix} \text{Elevation} = 2121 \\ \text{Slope} = 18 \end{pmatrix} \quad \text{Covariance Matrix} = \begin{pmatrix} 1931 & -54 \\ -54 & 87 \end{pmatrix}$$

We can then enter the Elevation and Slope rasters directly into the Mahalanobis equation to produce a Mahalanobis raster:

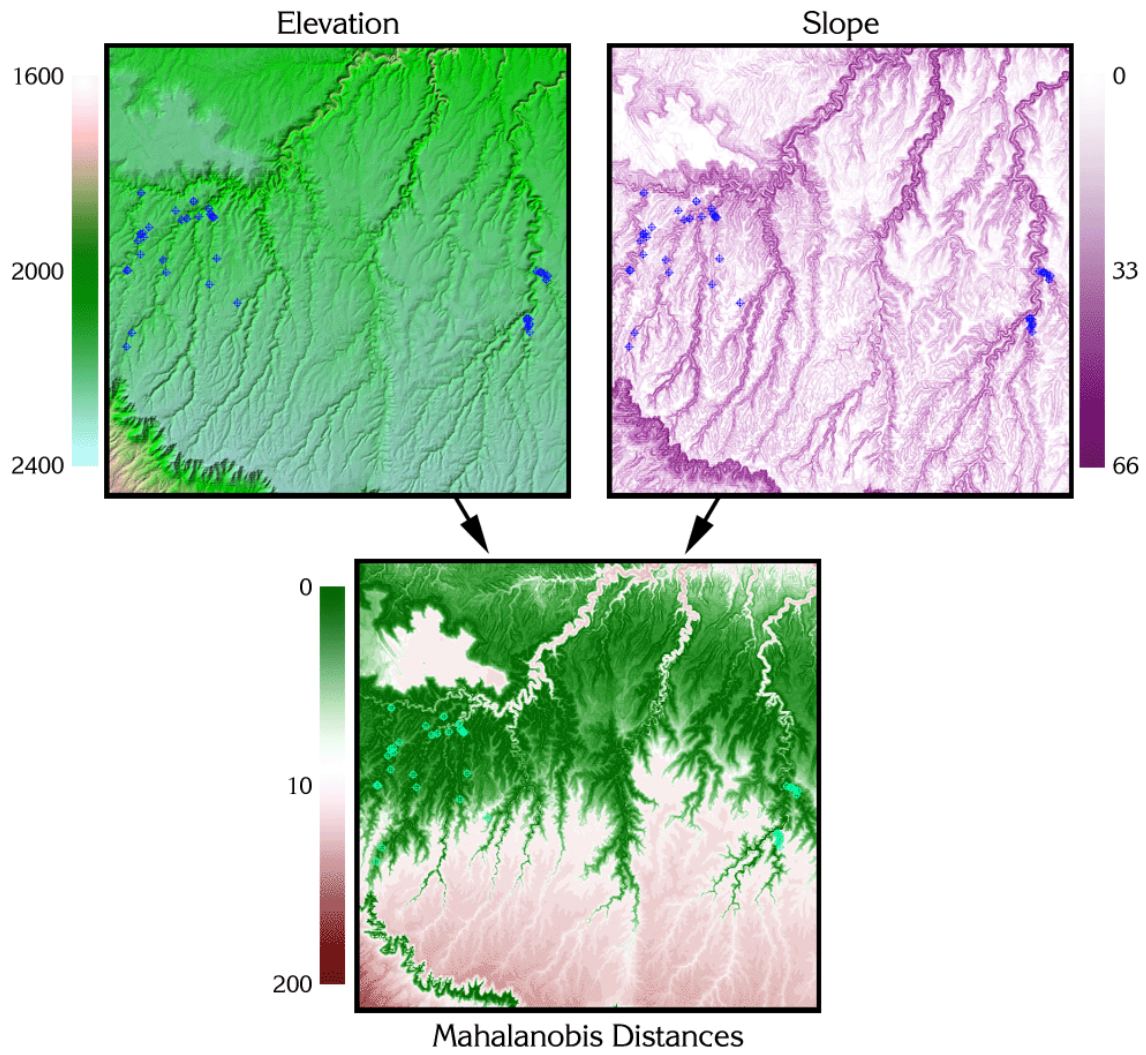
$$\text{Given that } D^2 = (\mathbf{x} - \mathbf{m})^T \mathbf{C}^{-1} (\mathbf{x} - \mathbf{m})$$

$$(\mathbf{x} - \mathbf{m}) = \begin{pmatrix} [\text{Elevation Raster}] - 2121.41667 \\ [\text{Slope Raster}] - 18.18997 \end{pmatrix}$$

$$\mathbf{C}^{-1} = \begin{pmatrix} 1931 & -54 \\ -54 & 87 \end{pmatrix}^{-1} = \begin{pmatrix} 0.00074 & 0.00046 \\ 0.00046 & 0.01173 \end{pmatrix}$$

$$\text{Therefore } D^2 = \begin{pmatrix} [\text{Elevation Raster}] - 2121.41667 \\ [\text{Slope Raster}] - 18.18997 \end{pmatrix}^T \times \begin{pmatrix} 0.00074 & 0.00046 \\ 0.00046 & 0.01173 \end{pmatrix} \times \begin{pmatrix} [\text{Elevation Raster}] - 2121.41667 \\ [\text{Slope Raster}] - 18.18997 \end{pmatrix}$$

$$= [\text{Mahalanobis Distance Raster}]$$



MEAN VECTOR AND COVARIANCE MATRIX TABLES:

The Mahalanobis tools included with this extension require a vector of mean values and a matrix of variance/covariance values. The *Mahalanobis Raster* tool (p. 65) can calculate these means and covariances on-the-fly while it conducts the Mahalanobis analysis, or extract them from existing tables in your map document. The *Mahalanobis Values at Sample Points* tool (p. 69) requires that you use existing tables. If you use the Covariance tools provided with this extension (see *Generating Statistical Matrices*, p. 73), then the tables will be formatted correctly. However, if you have used another statistical software package to create these tables, then make sure the tables are formatted as follows:

Formatting Rules for the Mean Vector Table:

1. Must have only a single attribute field, which contains the mean values for each variable.
2. This single field must be numeric.
1. There is no restriction on the name of this field.
3. If importing the table from a Comma-Delimited Text file (*.csv), then the field name should occupy the first row.
4. This tool will ignore any OID fields that may be in the table. If the table has an OID field in addition to the field of Mean values, then the tool will still recognize this table as a valid Mean Vector table.
5. The following text is an example of a valid Mean Vector table in Comma-Delimited Text format (*.csv).

```
Means
1747.993290
25.533938
```

Formatting Rules for the Covariance Matrix Table:

2. Must have only numeric fields in the table.
3. The number of rows in the table must be exactly the same as the number of attribute fields. Each field represents one variable, as does each row.
4. There are no restrictions on the field names.
5. If importing the table from a Comma-Delimited Text file (*.csv), then the field names should occupy the first row.
6. This tool will ignore any OID fields that may be in the table. If the table has an OID field in addition to the Variable Covariance fields, then the tool will still recognize this table as a potential Covariance Matrix table.
7. The following text is an example of a valid Covariance Matrix table in Comma-Delimited Text format (*.csv).

```
Elevation,Slope
13341.396994,-41.471005
-41.471005,22.228850
```

Formatting Rules for Both Tables:

1. Both tables must have the same number of rows. If they do not, then they must not describe the same set of variables and the tool will not let you proceed to the next dialog.

STATISTICAL MATRIX DEFINITIONS AND FORMULAE:

- *Mean:* $\frac{\sum_{i=1}^n X_i}{n}$

- *Variance/Covariance Matrix:*

Variance of variable $X = \sigma_{xx} = \sigma^2$; estimated by $\frac{\sum_{i=1}^n (X_i - \bar{X})^2}{n-1}$

Covariance between x and $y = \sigma_{xy}$; estimated by $\frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{n-1}$

Therefore, given p variables:

$$\text{Covariance Matrix Cov}(\mathbf{X}) = \begin{bmatrix} \sigma_{11} & \sigma_{12} & \cdots & \sigma_{1p} \\ \sigma_{21} & \sigma_{22} & \cdots & \sigma_{2p} \\ \vdots & \vdots & \ddots & \vdots \\ \sigma_{p1} & \sigma_{p2} & \cdots & \sigma_{pp} \end{bmatrix}$$

$$\text{estimated by} = \begin{bmatrix} \frac{\sum_{i=1}^n (x_{i1} - \bar{x}_1)^2}{n-1} & \frac{\sum_{i=1}^n (x_{i1} - \bar{x}_1)(x_{i2} - \bar{x}_2)}{n-1} & \cdots & \frac{\sum_{i=1}^n (x_{i1} - \bar{x}_1)(x_{ip} - \bar{x}_p)}{n-1} \\ \frac{\sum_{i=1}^n (x_{i2} - \bar{x}_2)(x_{i1} - \bar{x}_1)}{n-1} & \frac{\sum_{i=1}^n (x_{i2} - \bar{x}_2)^2}{n-1} & \cdots & \frac{\sum_{i=1}^n (x_{i2} - \bar{x}_2)(x_{ip} - \bar{x}_p)}{n-1} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\sum_{i=1}^n (x_{ip} - \bar{x}_p)(x_{i1} - \bar{x}_1)}{n-1} & \frac{\sum_{i=1}^n (x_{ip} - \bar{x}_p)(x_{i2} - \bar{x}_2)}{n-1} & \cdots & \frac{\sum_{i=1}^n (x_{ip} - \bar{x}_p)^2}{n-1} \end{bmatrix}$$

- *Inverse Covariance Matrix:* Matrix inversion is computationally complex, and the author refers interested readers to the Lower/Upper (LU) Decomposition method in chapter 2 of Press et al (2002).
- *Pearson Correlation Matrix:*

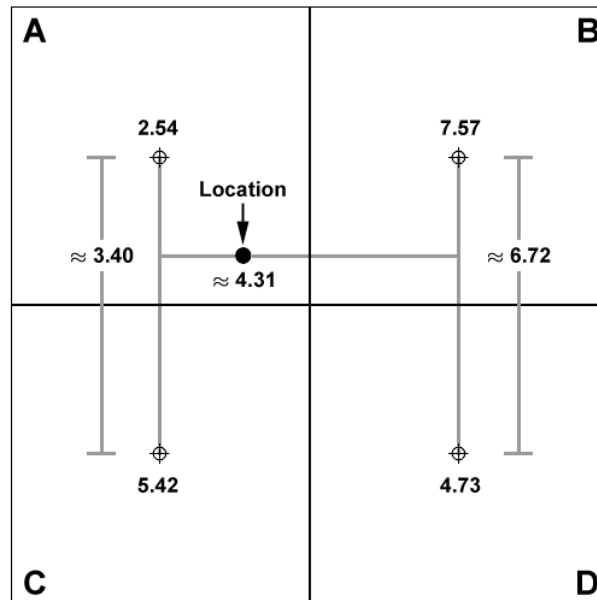
Given a Covariance Matrix $\text{Cov}(\mathbf{X}) = \begin{bmatrix} \sigma_{11} & \sigma_{12} & \cdots & \sigma_{1p} \\ \sigma_{21} & \sigma_{22} & \cdots & \sigma_{2p} \\ \vdots & \vdots & \ddots & \vdots \\ \sigma_{p1} & \sigma_{p2} & \cdots & \sigma_{pp} \end{bmatrix}$

the Pearson Correlation Matrix = $\begin{bmatrix} \frac{\sigma_{11}}{\sqrt{\sigma_{11}}\sqrt{\sigma_{11}}} & \frac{\sigma_{12}}{\sqrt{\sigma_{11}}\sqrt{\sigma_{22}}} & \cdots & \frac{\sigma_{1p}}{\sqrt{\sigma_{11}}\sqrt{\sigma_{pp}}} \\ \frac{\sigma_{21}}{\sqrt{\sigma_{11}}\sqrt{\sigma_{22}}} & \frac{\sigma_{22}}{\sqrt{\sigma_{22}}\sqrt{\sigma_{22}}} & \cdots & \frac{\sigma_{2p}}{\sqrt{\sigma_{22}}\sqrt{\sigma_{pp}}} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\sigma_{p1}}{\sqrt{\sigma_{11}}\sqrt{\sigma_{pp}}} & \frac{\sigma_{p2}}{\sqrt{\sigma_{22}}\sqrt{\sigma_{pp}}} & \cdots & \frac{\sigma_{pp}}{\sqrt{\sigma_{pp}}\sqrt{\sigma_{pp}}} \end{bmatrix}$

Spearman Correlation Matrix: Computationally identical to the Pearson Correlation Matrix except that ranks are used in place of original values. For example, the list of values {12, 3, 56, 23, 1} would be replaced with {3, 2, 5, 4, 1}, and the replacement list would then be used to generate the correlation matrix.

EXACT VALUES VS. INTERPOLATED VALUES:

You have the option to use the exact cell value for each of your point locations, or interpolated values based on the 4 closest cells to that point. For interpolated values, ArcView uses a 2-step method whereby values are interpolated first vertically and then horizontally. For example, given 4 cells around a particular location:



Lines are first generated between the cell centers of cells A and C, and between cells B and D, and values are interpolated along these lines at the Y-coordinate of the point location. Then a final value is interpolated along the X-axis between these two interpolated values. In this case, the interpolated value of the point is approximately 4.31, while the exact cell value of the point is 2.54.

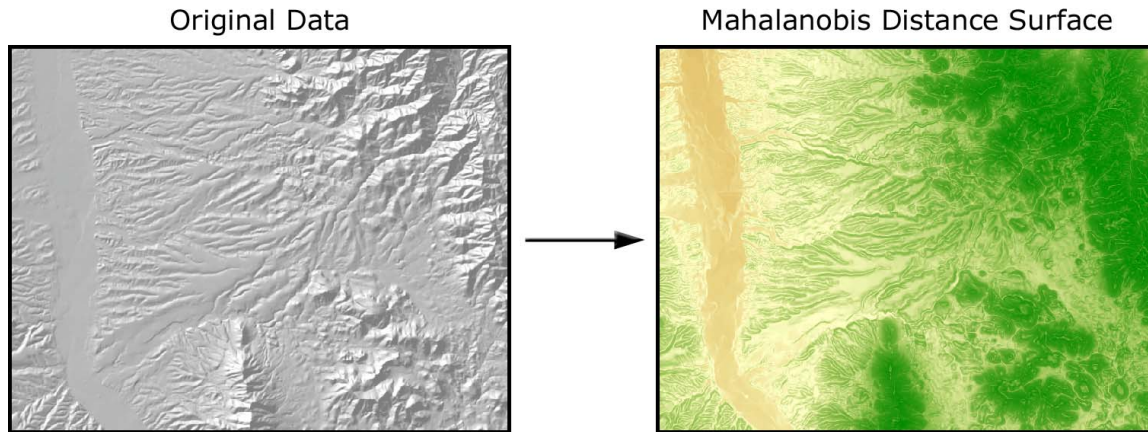
ADDITIONAL READING:

The author recommends Clark et al. (1993), Knick & Dyer (1997), and Farber & Kadmon (2002) for a few good papers illustrating the use of Mahalanobis distances in ecological applications. For anyone interested in the details of matrix algebra and computational/statistical algorithms, the author recommends Conover (1980), Neter et al. (1990), Golub and Van Loan (1996), Draper and Smith (1998), Meyer (2000) and Press et al. (2002).

Using the Tools:

CREATE MAHALANOBIS RASTER SURFACE

This is the primary tool used to generate the cost surface for the Land Facet corridors.



Mahalanobis distances are calculated based on the means and covariances of a set of variables, and therefore you must either specify existing tables containing the mean vector and covariance matrix, or create them on-the-fly. This tool allows both options. If you calculate the data on the fly, you have the option to define your sample locations by either a point layer or a single category in a categorical raster.

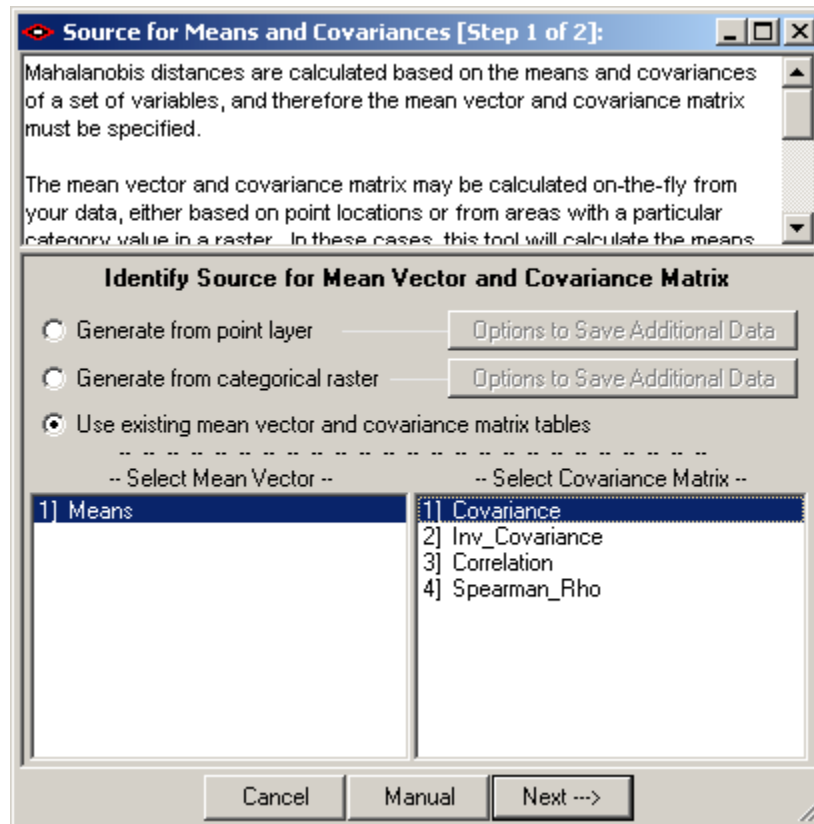
Note: If you are generating Land Facet corridors using the methods outlined in this document, and if you are using **Land Facet Density** as one of your input variables, do **not** calculate the mean vector and covariance matrix on-the-fly, but rather generate them using the *Calculating Statistical Matrices* tools included with this extension (see p. 73). Alternatively, if you have a large sample size ($N > \sim 20,000$ or so – and you often will), then it might be quicker to use the *Export to R* tool (p. 24) to create a table of values suitable for analysis in statistical software.

In general, if you have $< 20,000$ observations, we recommend you use the *Calculating Statistical Matrices* tool included in this extension because it ensures that the matrices will be formatted correctly. If you have a larger sample, then we recommend you use your statistical software to calculate the data, and follow the examples on p. 61 to make sure the data are formatted correctly.

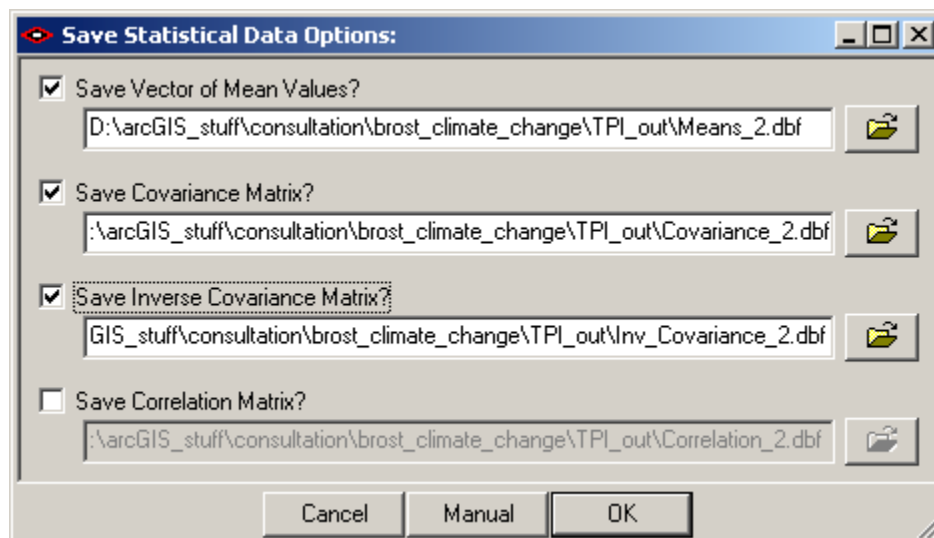
Mahalanobis values typically reflect the multivariate similarity to the vector of *ideal* values, which are typically, but not always, the *mean* values. Although the mean elevation, slope angle, and insolation are meaningful descriptors of a land facet, the mean Land Facet Density does *not* represent the ideal. The ideal land facet density would be when the neighborhood was completely covered with this particular land facet (i.e. a land facet density = 1). Therefore, after you create the mean vector, you must change the ideal Land Facet Density value to “1” before running the Mahalanobis analysis.

Important: If you select existing tables for your mean vector and covariance matrix, then you must make sure that the order of variables in the tables is the same as the order of variables you use to calculate your Mahalanobis surface. Please refer to the discussion of the *Mean Vector and Covariance Matrix* tables on p. 61 for a more detailed explanation of these tables.

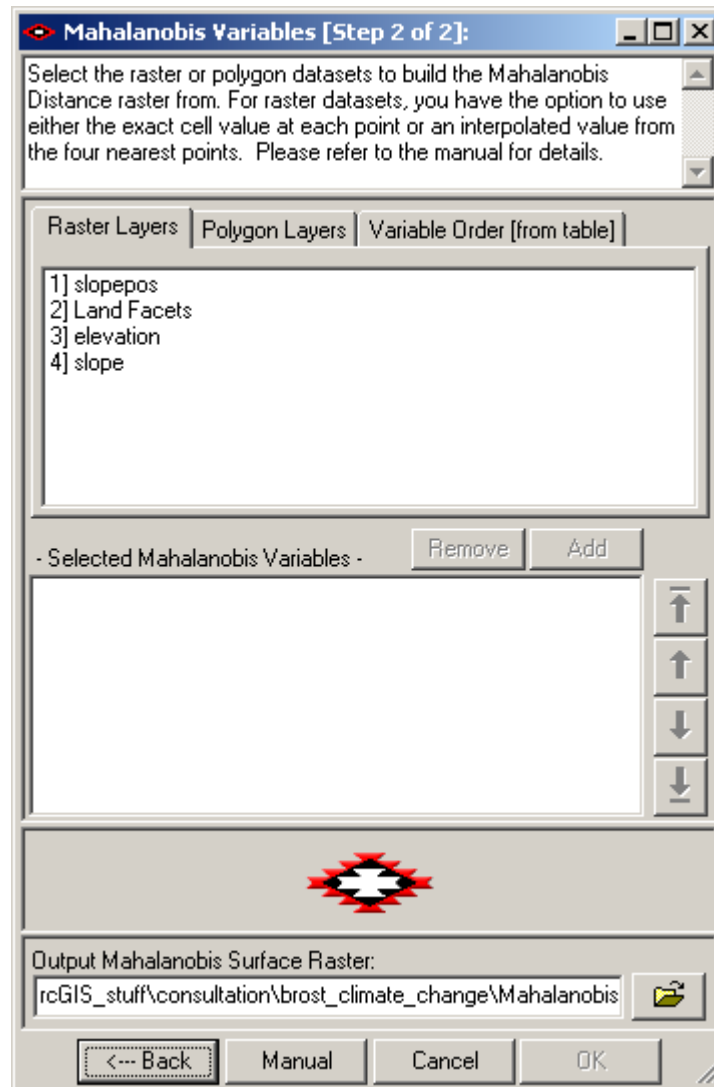
Click the  button to run the tool.



In the first dialog, select the source for your Mean Vector and Covariance Matrix. You may either generate them on-the-fly or extract them from existing tables. If you create them on-the-fly, you will have the option to save them as standalone tables by clicking the “Options to Save Additional Data” button.

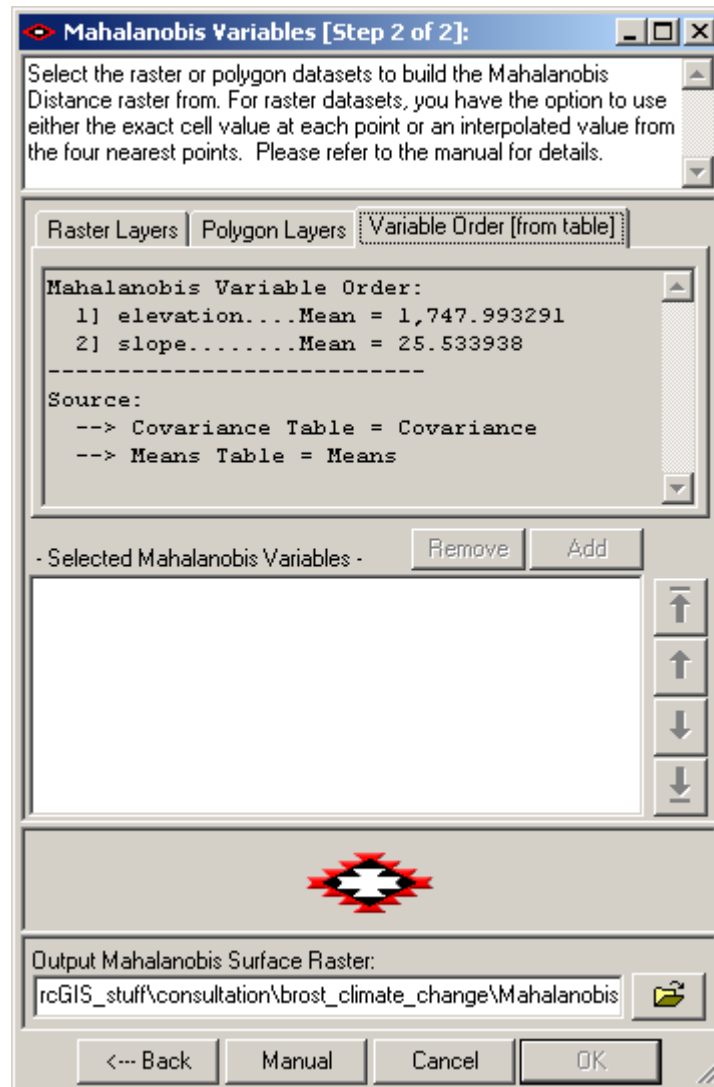


After you have specified the source for your mean vector and covariance matrix, click the “Next” button to move to the next dialog.



Select the raster or polygon datasets to use in the analysis. These layers should correspond with the variables used to generate the mean vector and covariance matrix. In our analyses using land facets to design corridors, we used the density of the land facet, slope, elevation, and insolation as variables for land facets within the Canyon Bottom or Ridge topographic positions. We used these variables plus insolation for land facets within the Slopes topographic position (See the *Overview* for an explanation).

Important: Be sure to sort these layers into the correct order! Click the "Variable Order" tab to see the order of variables listed in the specified Covariance Matrix (selected in the previous dialog).



You may select both Raster and Polygon Vector datasets for your input variables. For raster datasets, you might have the option to use either the exact cell value at each point or an interpolated value from the four nearest points. This option is only available if you are generating your mean vector and covariance matrix on-the-fly from a set of sample points extracted from a point layer. Please see the discussion on *Exact Values vs. Interpolated Points* on p. 63 for more details on this concept. **Note:** If you are performing a Land Facet analysis using Density as one of your variables, then you are likely using existing mean and covariance data and therefore you will not see this option.

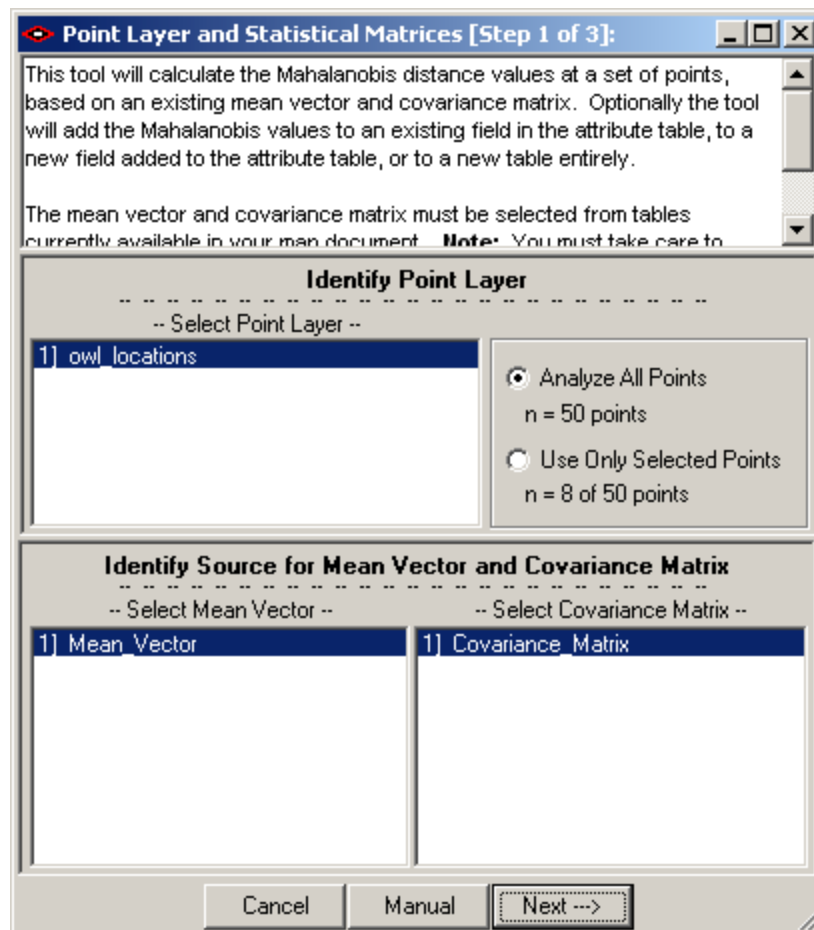
Click 'OK' and the tool will produce the Mahalanobis Raster surface and add it to your map.

CALCULATING MAHALANOBIS VALUES AT SAMPLE POINTS

This tool will calculate Mahalanobis distance values at a set of points, based on an existing mean vector and covariance matrix. See *Generating Statistical Matrices* on p. 73 for a tool to calculating these data. Optionally the tool will add the Mahalanobis values to an existing field in the Point layer attribute table, to a new field added to the attribute table, or to a new table entirely.

The mean vector and covariance matrix must be selected from tables currently available in your map document. **Note:** You must take care to ensure that the order of variables in the tables is the same as the order of variables you use to calculate your Mahalanobis surface. If the variable layers are not entered in the same order as they exist in the mean vector and covariance matrix, then the Mahalanobis Distance values will be incorrect.

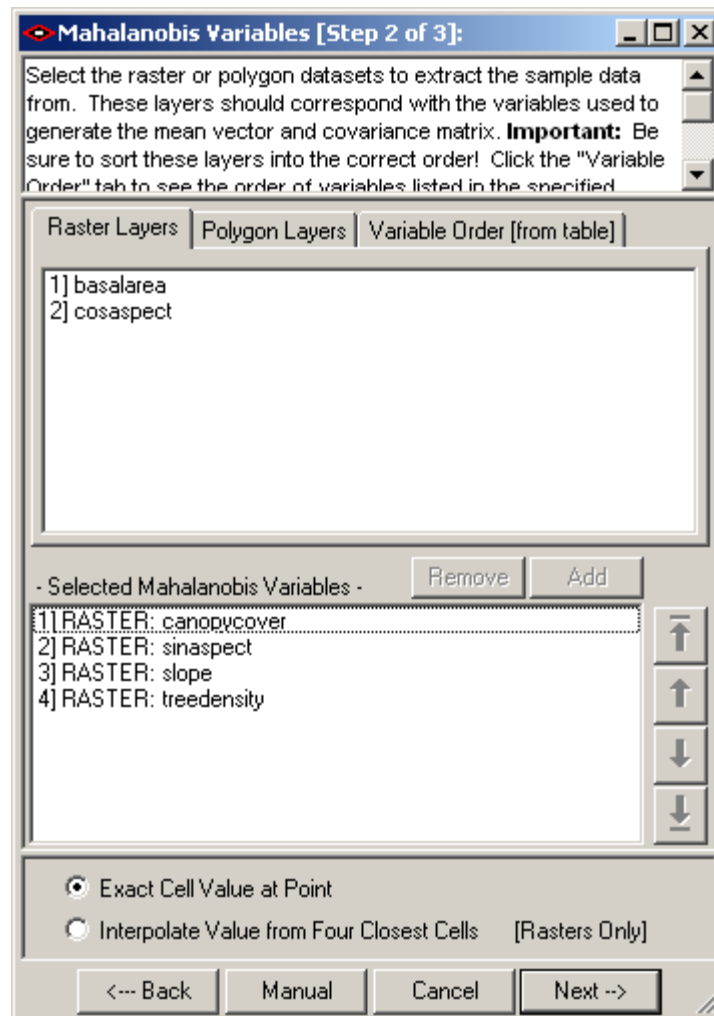
Click the  button to run the tool.



In the first dialog, identify the point layer you wish to analyze. If any of your points are selected, then you have the option to analyze only those selected points.

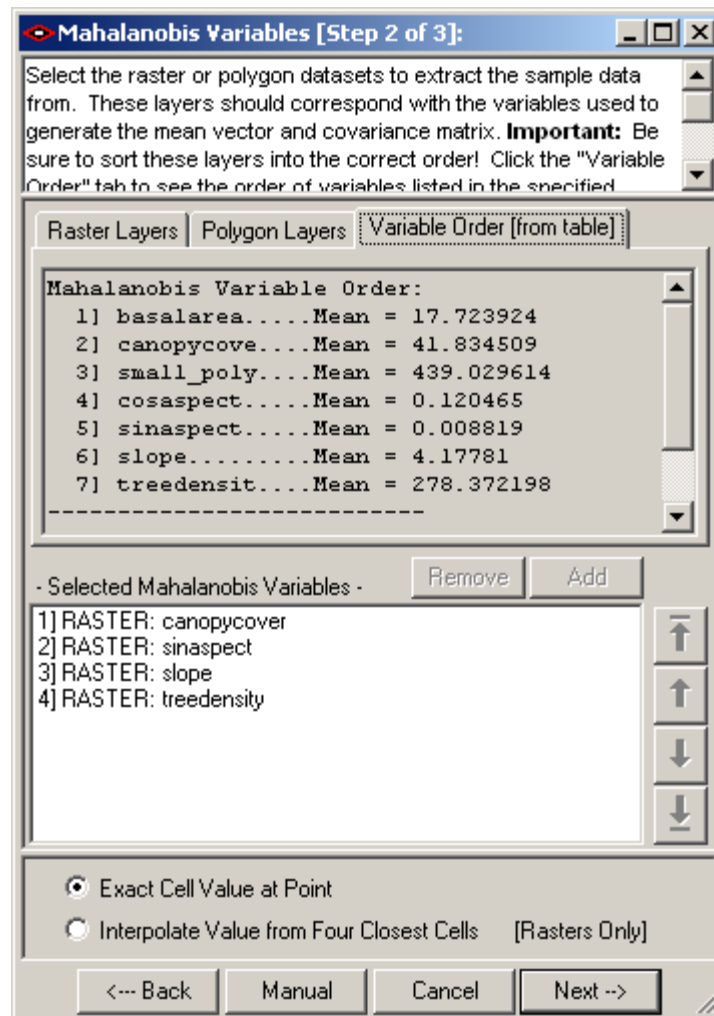
Next specify the correct mean vector and covariance matrix. These objects must be available as tables in your map document, and they must be formatted correctly in order to be recognized as potential Mean and Covariance tables. Please see the discussion of the *Mean Vector* and *Covariance Matrix* tables on p. 61 for explanations of these tables.

After you have selected your sample point layer, mean vector table and covariance table, click the “Next” button to move to the next dialog.



Select the raster or polygon datasets to extract the sample data from. These layers should correspond with the variables used to generate the mean vector and covariance matrix.

Important: Be sure to sort these layers into the correct order! Click the "Variable Order" tab to see the order of variables listed in the specified Covariance Matrix (selected in the previous dialog).



You may select both Raster and Polygon Vector datasets for your input variables. For raster datasets, you also have the option to use either the exact cell value at each point or an interpolated value from the four nearest points. Please see the discussion on *Exact Values vs. Interpolated Points* on p. 63 for more details on this concept.

After you have selected your variable layers, click the “Next” button to move on to the last dialog.

Output Options [Step 3 of 3]:

Point Layer = owl_locations

☐ Create New Table

Point Layer Unique ID Field = 1: [FID]

New Mahalanobis Distances Table Location:

D:\arcGIS_stuff\general_tools\Mahalanobis\TopoCorridor.dbf

☐ Add Data to Existing Field

Mahalanobis Distance Field = 1: [UNIQUE_ID]

☒ Create New Field in Point Layer

Enter New Field Name: Mahal

Note on Field Name Restrictions

<-- Back Cancel Manual OK


Use this dialog to specify where you want to save your Mahalanobis values. Optionally you may save them to a new table, to an existing numeric attribute field in your Point feature class, or to a new attribute field in your Point feature class.

GENERATING STATISTICAL MATRICES:

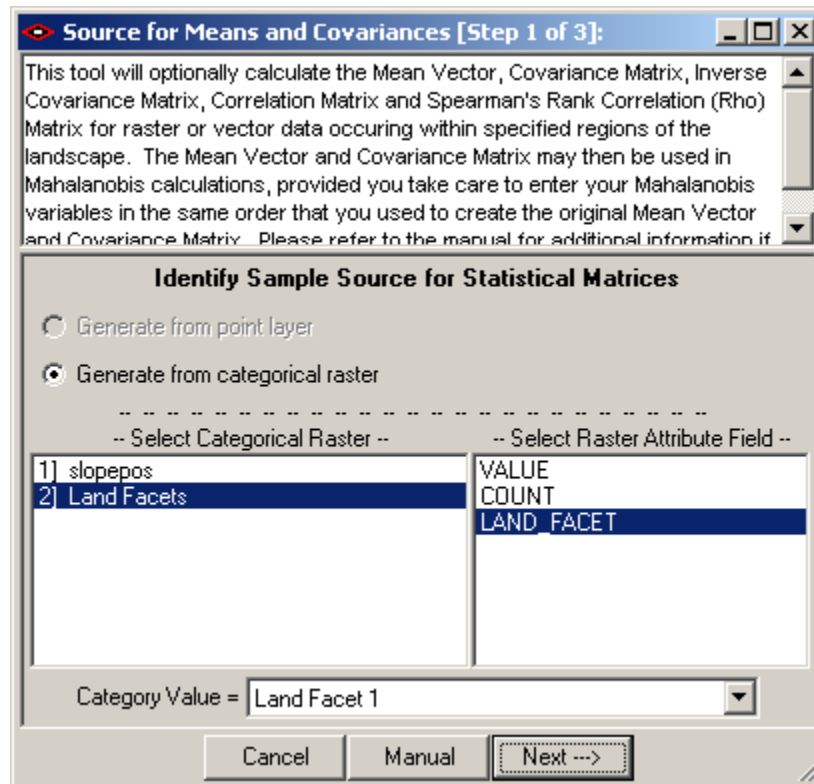
This function provides a quick way to generate tables containing the mean vector, covariance matrix, inverse covariance matrix, Pearson's r correlation matrix, and Spearman's rho rank correlation matrix from multiple raster and polygon datasets in your map. The mean vector and covariance matrix tables can be used with the Mahalanobis functions described elsewhere in this manual.

Pearson's r correlations measure how much one variable changes as a second variable changes, and in which direction. Values range between -1 and 1, with negative values implying a negative relationship (i.e. as one variable increases, the other decreases). Values close to 1 or -1 have high correlation while values close to 0 have low correlation. Spearman's rho correlations are identical to Pearson's r except that they are calculated from the relative rank of each value rather than the value itself (see Conover 1980:252). Spearman's rho correlations are generally considered more appropriate when the variables are not normally distributed or when the researcher wants to reduce the importance of outliers.

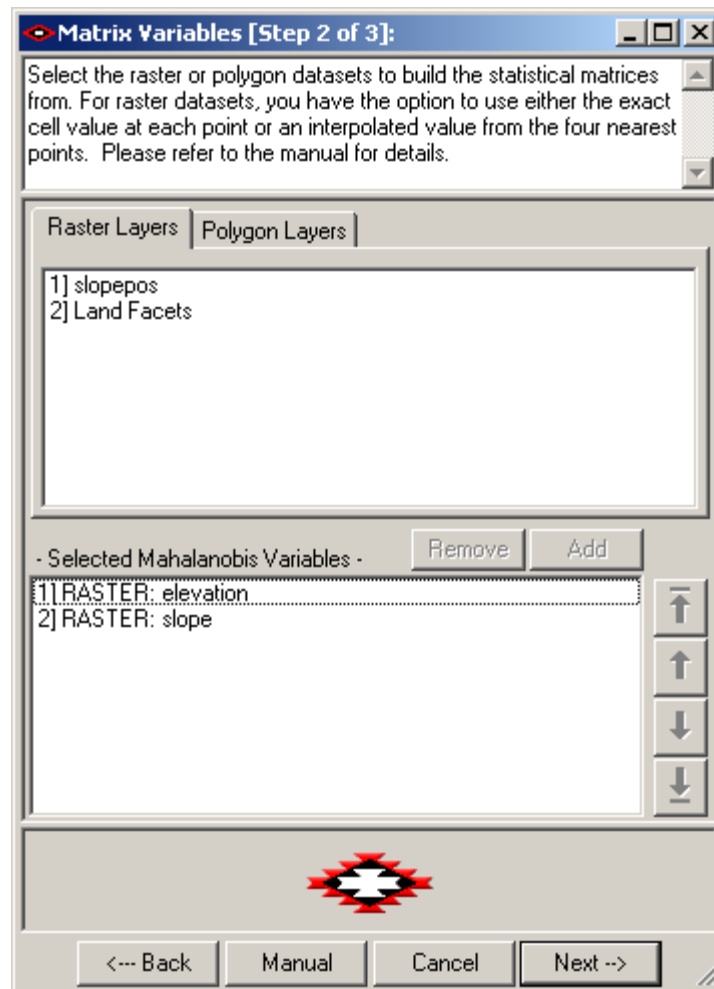
Warning: This tool works well with relatively small datasets ($N < 20,000$ sample points or so). However, if you need to calculate statistical matrices for large regions which will require hundreds of thousands or millions of sample locations, then we recommend you use the *Export to R* tool (p. 24) to create a table of values suitable for analysis in statistical software, then use that statistical software to create the matrices. See p. 61 for a discussion of formatting tips to make sure the tool can read the matrices correctly.

Click the  button to start the process.

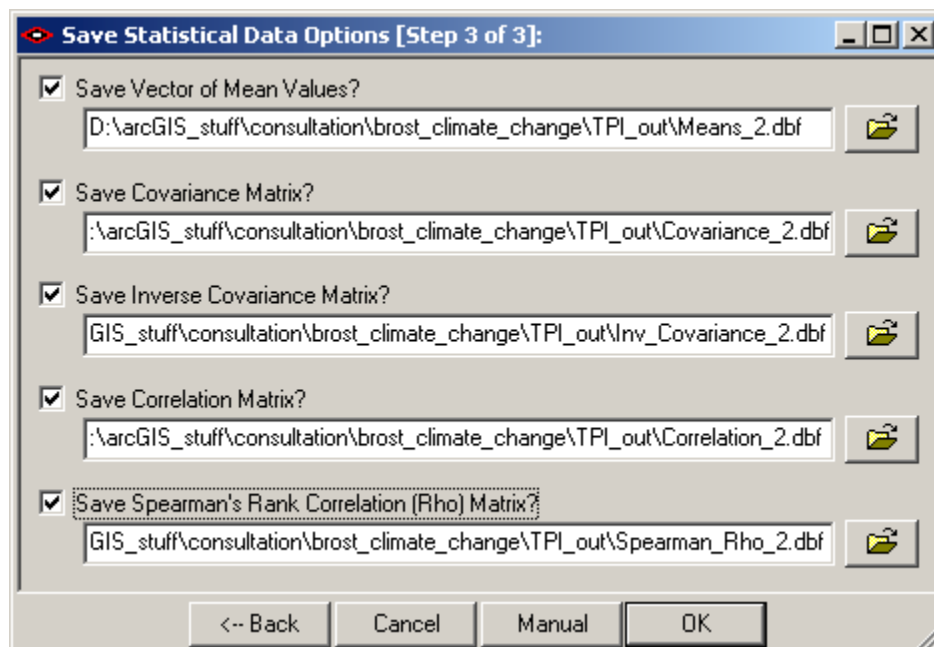
First select the region containing the sample locations. If you select a point layer, then your statistical matrices will be generated from all your datasets that intersect those points. If you select a categorical raster, then your statistical matrices will be generated from all datasets that intersect the specific raster category you select. For example, if we wanted to generate statistical matrices for Land Facet 1, then we would fill out the dialog as follows:



Next, choose the layers containing the variables you wish to analyze. If you select polygon layers, then you will also need to select the attribute field containing the variable data. **Note:** If you plan to use these statistical matrices in a Mahalanobis analysis, make sure to keep track of the order of the variables. The variables will need to be entered in the same order in the Mahalanobis dialogs.



Finally, choose which statistical matrices you wish to generate and where you want to save them.



Upon completion, the tool will add these tables to your map document and open them.

The image displays five separate window screenshots, each showing a table of statistical results. Each window has a title bar with a list icon, a maximize button, and a close button. Below the table is a 'Record:' field with navigation arrows and a 'w:' dropdown menu.

Attributes of Means

OID	Means
0	1747.993291
1	25.533938

Record: 1 w: ▼

Attributes of Covariance

OID	elevation	slope
0	13341.396995	-41.471005
1	-41.471005	22.228851

Record: 1 w: ▼

Attributes of Inv_Covariance

OID	elevation	slope
0	0.000075	0.000141
1	0.000141	0.045249

Record: 1 w: ▼

Attributes of Correlation

OID	elevation	slope
0	1	-0.076153
1	-0.076153	1

Record: 1 w: ▼

Attributes of Spearman_Rho

OID	elevation	slope
0	1	-0.086413
1	-0.086413	1

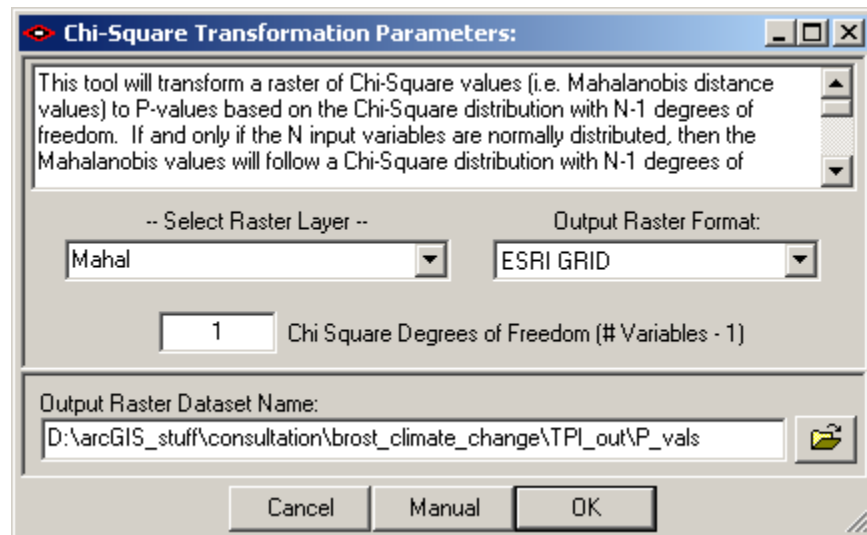
Record: 1 w: ▼

Note: If you plan to use these tables in the Mahalanobis analysis, and if you are using *Land Facet Density* as one of your variables, then you **must** change the “mean” density value to 1 before you run the analysis, so that the Mahalanobis Distance value will reflect the distance from “1” (i.e. the ideal density value) rather than the actual mean.

CHI-SQUARE RASTER TRANSFORM:

This tool will transform a raster of Chi-Square values (i.e. Mahalanobis distance values) to P-values based on the Chi-Square distribution with $N - 1$ degrees of freedom. **If and only if** the N input variables are normally distributed, then the Mahalanobis values will follow a Chi-Square distribution with $N - 1$ degrees of freedom. Farber and Kadmon (2003) warn that wildlife habitat variables often fail to meet the assumption of normality, so in this case the conversion to Chi-square p -values serves only to recode the Mahalanobis distances to a 0-1 scale. Mahalanobis distances themselves have no upper limit, so this rescaling may be convenient for some analyses. Please see the discussion on Chi-Square transformation on p. 58 for more details.

Click the  button to run the tool.



Select the raster layer of Chi-Square values (i.e. the Mahalanobis raster) layer from the list, and enter the number of degrees of freedom to use in the Chi-Square transformation. The degrees of freedom should be equal to [Number of Variables - 1] used in the original Mahalanobis analysis. For example, if 6 rasters were used to create the Mahalanobis raster, then the Degrees of Freedom would be $[6 - 1] = 5$. Finally, specify the name of your new raster and where to save it.

R Functions for Defining Land Facets

This section documents the functions used to define land facets, or recurring polygons of relatively homogenous topography and soils. These functions are implemented in R, a widely-used computer language for data manipulation, calculation, and graphical display. It is an environment within which many classical and modern statistical techniques are implemented. R has a steeper learning curve than other statistical software packages because of its command-line interface; however, R offers nearly unlimited capabilities for data analysis. R is distributed for free from www.r-project.org, the R Project for Statistical Computing website. It is compatible with Windows, MacOS X, and Linux operating systems.

There are two R functions used for identifying outliers in a data set, one function for classifying the data set into land facets, and a final function for exporting products of the classification in a format compatible with the “Land Facet Clusters from R” tool of the Land Facet CorridorDesigner extension to ArcGIS. The input data for these functions is generated by the “Export for R Analysis” tool of the same extension. Prior to describing the R functions for defining land facets, I briefly introduce those features of R statistical language essential for using these functions. *An Introduction to R* by Venables and Smith offers a more comprehensive introduction to the R language. It is free and available on the R website (under the Manuals section). An excellent (but not free) reference that covers data handling, graphics, mathematical functions, and a wide range of statistical techniques in R is *The R Book* by Michael Crawley.

An R Primer

After installation, R can be started like any other application, that is by double-clicking the “R” icon. This opens the R Console, the window through which the user communicates with R. The “>” symbol at the beginning of the input line in the R Console is the prompt from the application, after which an expression is entered for R to evaluate. If the expression is complete, R returns its product. If it is incomplete, the prompt changes to a “+” to indicate more input is required. Any text after a “#” is ignored by R, which is a simple way of embedding comments in lines of R code.

USING R AS A CALCULATOR

Arithmetic expressions can be typed directly into the R console. If the expression (in red) is complete, the line is evaluated and the result (in blue) is printed. The “[1]” at the beginning of the response is an index indicating that what follows is the first (and in this case only) element of a numeric vector. For example:

5-1

[1] 4

7*10/2

[1] 35

ASSIGNING VALUES TO OBJECTS

R is an object-oriented language, which means that variables, data, functions, and results are stored in the form of objects. All currently-defined R objects are contained in the R workspace. Objects have a name and the user can act on them with operators (arithmetic, logical, etc.) and functions. Note that R is case-sensitive. The assignment operator is the two-character sequence

“<-“. Typing the name of the object will cause R to print out the contents of the object. The function `ls` lists the names of objects in the current workspace, whereas the `rm` function removes objects. For example:

```
x <- 3 #assign the object x a value of 3
x
[1] 3

y <- 5
x-y
[1] -2

ls() #list all objects in the current workspace
[1] "x" "y"

rm(x) #remove the object x from the workspace
ls()
[1] "y"
```

Multiple values can be assigned to a single object using the concatenate function, `c`. For example:

```
y <- c(2, 5, 7) #assign the object y the values 2, 5, and 7
y
[1] 2 5 7
```

To assign a sequence of integer values to an object, place a colon between the first and last numbers of the sequence, like this:

```
y <- c(2:7) #assign the object y the integer values 2-7
y
[1] 2 3 4 5 6 7
```

USING R FUNCTIONS

The structure of a typical R statement is

```
new.object <- function(arguments)
```

where “function” is the name of a previously-defined (or built-in) function, “arguments” is a list of one or more arguments specific to that function, and “new.object” is the name of a new object containing the product(s) of the function. To illustrate, the following statement is used to read data in the format of a comma-separated value (csv) file into R:

```
data <- read.csv(file="C:/land_facets/example_data.csv")
```

The function is called `read.csv` and its `file` argument is the location and name of the csv file to be read into R. Notice that branches in the file directory containing `example_data.csv` are separated by forward slashes, not backslashes. After executing this line, the object `data` contains the information stored in the csv file. `data` is a dataframe, which is an object that has rows and columns. The rows contain values for different observations (i.e., raster cells) and the columns contain the values of different variables. The function `head` returns the first six lines of the object for inspection:

```
head(data)
  elevation slope
1 1655.584 29.4104
2 2484.788 32.2004
3 2057.512 20.6244
4 2044.320 13.4432
5 1308.766 16.5707
6 1473.009 25.7639
```

This shows that `data` contains two variables, elevation and slope. The first column of numbers indexes the rows in `data`. To refer to a single variable within a dataframe, one would type `dataframe$variable`. For example, `data$elevation` pulls out the column of elevation values from the `data` dataframe. The number of rows in `data` is:

```
nrow(data)
[1] 100000
```

ISOLATING SUBSETS OF DATA IN A DATAFRAME:

Subscripts are used to reference subsets of data in a dataframe. In R, subscripts appear in square brackets (i.e., `[]`). The rows of a dataframe are referenced by the first (left-hand) subscript and the columns by the second (right-hand) subscript. For example,

```
data[2,1]
[1] 2484.788
```

is the value in `data` at the intersection of row 2 and column 1. To select all entries in a row or column, leave the respective subscript blank. For example, `data[2,]` would return all values in the second row of `data`, and `data[,2]` would return all values in its second column.

Logical subscripts can be used to isolate subsets of a dataframe that satisfy a specified condition. For example, `data[data$elevation > 1000,]` selects only those rows in `data` that have an elevation value greater than 1000. Other logical operators include `<=` for “less than or equal to” or `==` (that’s two equal signs back-to-back) for “equal to,” just to name a couple.

INSTALLING AND LOADING R PACKAGES

Many functions are built into the base R environment (i.e., functions that automatically come with R). Many more functions are supplied as add-on packages. To install an add-on package, use the `install.packages` command. For example,

```
install.packages(pkgs="ks")
```


installs the **ks** package for multivariate kernel density estimation. You will be asked to select the mirror (or repository) nearest you for fast downloading. Everything else is automatic. To use the package, the user first needs to load it into the workspace using the **library** function. For example,

```
library(package=ks)
```

loads the **ks** package into the workspace, allowing R to access the functions that it contains. Note that packages only need to be installed once, but they need to be loaded into the R workspace during each new R session.

GETTING HELP IN R

Help files for R functions can be accessed by typing a question mark followed by the function name. So,

```
?read.csv
```

opens the R reference manual for the function **read.csv**. Help files contain a description of the function, information on its usage including the arguments it accepts, and the value(s) that it returns.

SOME SUGGESTIONS

Although commands can be typed directly into the R Console, it is often useful to use R's built-in text editor (click on "New Script..." under the "File" menu). Not only can commands be typed and edited in the editor, but selected lines of code can be executed directly from the editor, too. Simply highlight the code of interest and press CTRL+R. "Scripts" (lines of commands) can also be saved, making it easy to document your work or re-run the commands at a later date.

If you read from or write files to the same path frequently, it is sensible to set the working directory using the **setwd** function:

```
setwd(dir="C:/land_facets/")
```

Now, to read a csv file into R from the working directory, just type:

```
data <- read.csv(file="example_data.csv")
```

When you exit R, you are given the option of saving the workspace. If you do save it, the contents of the workspace will be restored when you open R again. To limit the clutter in your workspace, I recommend not saving on exit. Instead, use the "Save Workspace" option under the "File" menu to save the workspace for your current project under a name you specify; that named workspace can then be restored if necessary by using the "Load Workspace" option under the same menu. This lets you choose the amount of clutter – or useful information – in your workspace.

Overview Of R Functions For Defining Land Facets

The “Land Facet Clusters from R” tool provides four new R functions, namely:

- two functions to identify outliers in a data set (**LF.kde** and **LF.outlier**),
- one function to classify a data set into land facets (**LF.cluster**), and
- one function (**LF.export**) to export the products of the classification, which is necessary for compatibility with the “Land Facet Clusters from R” tool of the Land Facet CorridorDesigner extension to ArcGIS.

Unlike built-in R functions or those in add-on packages, **?function.name** will not access Help files for these four functions. Thus, documentation is provided below in a format similar to R reference manuals. Documentation for each function includes five sections. The “Description” and “Usage” subsections describe the function and illustrate its structure, respectively. The “Arguments” subsection lists and describes the arguments to each function, whereas “Details” provides information about the function. If the function automatically outputs information for compatibility with the Land Facet CorridorDesigner extension to ArcGIS, these files are described in the “Output” subsection. Finally, the “Values” subsection lists and describes the values returned by the function. The functions are presented in the order in which they are intended to be used. They depend on R packages **ks**, **e1071**, **lattice**, **clusterSim**, and **nnclust**. The last part of this Section, *Workflow for Defining Land Facets*, illustrates how these functions are implemented.

KERNEL DENSITY ESTIMATION: FUNCTION LF.KDE

Description

Function `LF.kde` is the first step in identifying outliers, or cells with combinations of values for continuous variables that rarely occur in a data set. Outliers occupy the tails of the (multivariate) distribution generated from a kernel density estimation, a non-parametric procedure that estimates the probability density function of a random variable or group of variables. This function automatically plots the kernel density estimation, allowing the user to determine an appropriate density threshold (contour) beyond which cells are identified as outliers. An appropriate threshold separates regions in attribute space densely populated by cells from those more sparsely populated. You will use this threshold as an argument in `LF.outlier`, the next function.

Function `LF.kde` implements the `Hpi.diag` and `kde` functions of package `ks` for bandwidth selection and multivariate kernel density estimation, respectively. Because raster data sets are large, this function “bins” the data set (individual cells in the raster are grouped according to their attribute values into bins of equal interval across the range of each variable). Kernel density estimation is performed on these bins, reducing computation time by several orders of magnitude. We experimented with different numbers of bins to develop the recommendations below; specifying more bins (larger grid size) greatly increases computation time without increasing your ability to identify outliers. `LF.kde` automatically outputs to the working directory information on the bins used for the kernel density estimation.

Usage

`LF.kde(x, gridsize)`

Arguments

- | | |
|-----------------|--|
| x | the matrix or dataframe containing topographic and/or soil data. Consists of one row per raster cell and one column per topographic or soil variable. |
| gridsize | The number of equal intervals into which the range of each variable will be split for the purpose of creating bins. Due to memory constraints, gridsize=151 is appropriate for 2-dimensional data; in this case kernel density estimation is performed on a 2-dimensional array of 151^2 bins (22,801 bins). For 3-dimensional data, gridsize=91 is appropriate; in this case kernel density estimation is performed on a 3-dimensional array of 91^3 bins (753,571 bins). If you are using more than 3 continuous variables to define outliers (i.e., your multivariate space has more than 3 dimensions), you will require a smaller gridsize less than 91; we have not experimented with datasets of dimension > 3 . |

Details

`LF.kde` is functional for 1- to 6-dimensional data sets.

This function automatically plots the objects in `x` and the density estimation. For 1-dimensional data sets, the plot shows the univariate density curve and a rug plot of objects in `x`. For 2-dimensional data sets, density contours are overlaid onto the bivariate plot of objects in `x`. The

contours have an interval of 10% from 10% to 70%, and a 5% interval from 70% to 100%. The contour labeled “10” contains the 10% of objects occurring at highest density.

For 3-dimensional data, this function plots the objects in **x** and the 3-dimensional density contours. For visual clarity, only the 25, 50, 75, 90, and 100% density contours are displayed, but you can use the plot and data to specify a density threshold other than one of these values.

Output

This function writes to the working directory `bin_width.csv`, a comma delimited file that contains the (multidimensional) half-width of bins used in the kernel density estimation.

Value

x	dataframe containing topographic and/or soil data--same as input.
width	(multidimensional) half-width of bins used in the kernel density estimation. Same as values outputted in <code>bin_width.csv</code> .
eval.points	points at which the density estimate is evaluated. For each bin, this is the center point (not the centroid of observations falling in the bin).
estimate	kernel density estimate at <code>eval.points</code> . Kernel density estimates sum to one.
H	bandwidth matrix. This is a technical detail you can ignore.
h	scalar bandwidth (1-dimension only).
names	names of variables in x .
w	weights. This is another technical detail you can ignore.

Identify Outliers: Function LF.outlier

Description

Function `LF.outlier` is the second step in identifying outliers. It first assigns individual cells the kernel density estimate of the bins into which they were grouped. Then, it identifies which cells occur beyond the user-specified density threshold defining outliers. This density threshold can be estimated from the plot generated by function `LF.kde`. Function `LF.outlier` also outputs to the working directory information about the location of bins containing non-outlier cells.

Usage

```
LF.outlier(x, threshold=90)
```

Arguments

- | | |
|------------------------|---|
| <code>x</code> | an object returned from function <code>LF.kde</code> . |
| <code>threshold</code> | threshold corresponding to the density contour (from contour plot of <code>LF.kde</code>) beyond which observations are identified as outliers. For example, a threshold of 90 identifies the 10% of cells beyond the 90% contour as outliers (i.e., the 10% of cells with the lowest kernel density estimates would be identified as outliers). |

Output

This function outputs to the working directory `grid.csv`, a comma delimited file that contains the location of bins containing non-outlier cells.

Value

- | | |
|----------------------|---|
| <code>outlier</code> | a vector of length <code>nrow(x)</code> consisting of values 0 (indicates non-outlier) or 1 (indicates outlier). |
| <code>density</code> | a vector of length <code>nrow(x)</code> containing the interpolated kernel density for each object in <code>x</code> . Each raster cell is “interpolated” by assigning it the density of the bin in which it falls. |

Fuzzy c-means Cluster Analysis: Function LF.cluster

Description

Function `LF.cluster` is used to classify the non-outlier cells into land facets. This function implements the `cmeans` function of package `e1071` to perform fuzzy *c*-means cluster analysis, an iterative procedure that assigns each raster cell to one of *c* clusters in a way that minimizes the *c* within-cluster variances. Each such assignment is called a “partition” of the cells. Because there may be more than one partition that minimizes within-cluster variances for a given value of *c*, you are encouraged to repeat the procedure 30 times (iterations take lots of computing time, and our experiments suggest that 30 iterations are sufficient to detect such cases). Function `LF.cluster` requires the user to specify the range of values of *c* to be evaluated, and the number of iterations for each value of *c*. The function automatically computes eight cluster validity indices used to determine the optimal number of clusters for the given data set.

Once complete, this function generates two plots. The first is a plot of cluster centroids for each iteration of each *c*, which is useful for detecting cases in which more than one partition for a given *c* minimizes the within-cluster variance. The second plot graphs the validity indices for each iteration of each *c*, which is necessary for identifying *k*, the optimal number of clusters for the given data set. The Fukuyama-Sugeno and Average Within Cluster Distance indices are interpreted as a scree plot, where an “elbow” in the plot indicates the optimal number of clusters. The Xie-Beni, Xie-Beni*, and Davies-Bouldin indices are minimized for the optimal number of clusters, whereas the PBM, Calinski-Harabasz, and Fuzzy Silhouette indices are maximized.

Usage

```
LF.cluster(x, nclust=c(2:7), niter=30, psi=1.5, max=1000000)
```

Arguments

x	the matrix or dataframe containing topographic and/or soil data, minus rows identified as outliers by function <code>LF.outlier</code> . Consists of one row per non-outlier raster cell and one column per topographic or soil variable.
nclust	range of values of <i>c</i> for which to perform the cluster analyses.
niter	number of iterations of the cluster analysis to perform for each value of <i>c</i> .
psi	a weighting parameter that determines the overlap between clusters. A crisp classification (i.e., no overlap between classes) corresponds to psi = 1; larger values of psi produce increasingly fuzzy classifications. Based on our limited experimentation, we recommend using the default value of 1.5; we welcome feedback from users who experiment with different values.
max	the maximum number of observations upon which to perform the cluster analysis. Provided to avoid memory limitations encountered on large data sets.

Details

Depending on the size of the data set, this function could take hours to complete. For example, testing `nclust=c(2:7)` and `niter=30` on a data set containing 2 attributes and 256205 objects took 6 hours to complete on a Microsoft Windows XP platform with 3.0 GHz Intel Core 2 Duo processor. Computation time increases with the size of `x` (raster cells in your landscape, which you cannot control), the number of values of `c` to be evaluated (we never found an optimum at $c > 5$, so we recommend stopping at $c = 7$ unless your validity indices suggest that additional values should be tested), and number of iterations (we recommend stopping at 30).

Value

centroids	location of cluster centroids for each iteration of each c .
validity	validity indices for each iteration of each c . Contents:
c	number of clusters
z	Iteration
FS	Fukuyama-Sugeno index
AWCD	Average Within Cluster Distance
XB	Xie-Beni index
XB_star	Xie-Beni* index
DB	Davies-Bouldin index
PBM	PBM index
CH	Calinski-Harabasz index
FSil	Fuzzy Silhouette index

Exporting Information for Land Facet CorridorDesigner: Function LF.export

Description

Outputs to the working directory three comma delimited files necessary for compatibility with the Land Facet CorridorDesigner extension to ArcGIS: (1) cluster centroids for the optimal fuzzy-*c* partition, (2) mean and standard deviation of attributes (elevation and slope in the sample data set) across all non-outliers, regardless of cluster ; these are needed later to standardize your data, and (3) value for *psi* used in function LF.cluster. the mean and SD of elevation and.

Usage

```
LF.export(x, k, iter=1)
```

Arguments

x	object returned from LF.cluster.
k	optimal number of clusters.
iter	iteration having optimal validity indices for <i>k</i> clusters. Necessary only for instances where multiple solutions minimize the within-cluster variances for <i>k</i> partitions.

Output

Outputs to the working directory: (1) centroids.csv, which contains the location of cluster centroids for the optimal fuzzy-*c* partition; (2) params.csv, which contains the mean and standard deviations of the attributes in the data set; and (3) psi.csv, which contains the value of *psi* used in function LF.cluster.

Downloading The R Functions For Defining Land Facets

Download and extract the files contained in LF_R_fxns.zip from <http://www.corridordesign.org/>. The Zip file contains three files:

1. LF_fxns.R – source code for the R functions for defining land facets
2. LF_code.R – sample code for using the R functions in LF_fxns.R
3. sample_data.csv – a sample data set

Workflow For Defining Land Facets

1. Use the “Export for R Analysis” tool in the Land Facet Corridor extension to ArcGIS to export topographic and soil data from ArcGIS in a format compatible with R.
2. Open R.
3. Open the LF_code.R file by selecting “Open Script...” from the “File” menu and navigating to and selecting the LF_code.R file. This file contains all of the R code in the workflow below. Note that you will need to change the file directories in this code, unless your files are located in the directory C:/land_facets.
4. The R functions for defining land facets depend on R packages ks, e1071, lattice, clusterSim, and nnclust. Install these add-on packages:

```
install.packages("ks")
install.packages("e1071")
install.packages("lattice")
install.packages("clusterSim")
install.packages("nnclust")
```

5. Load the R functions for defining land facets into the workspace using the source function:

```
source(file="C:/land_facets/LF_fxns.R")
```

The “file” argument to this function is the location of LF_fxns.R. Execution of this file also loads the add-on packages in Step 3 into the workspace.

6. Set the working directory:

```
setwd("c:/land_facets")
```

Note: the functions for defining land facets automatically write files to the working directory for compatibility with the Land Facet CorridorDesigner extension to ArcGIS.

7. Load the topographic and soils data from ArcGIS into R:

```
data <- read.csv("c:/land_facets/example_data.csv")
head(data) #inspect first six rows of data
  elevation slope
1 1655.584 29.4104
2 2484.788 32.2004
3 2057.512 20.6244
```

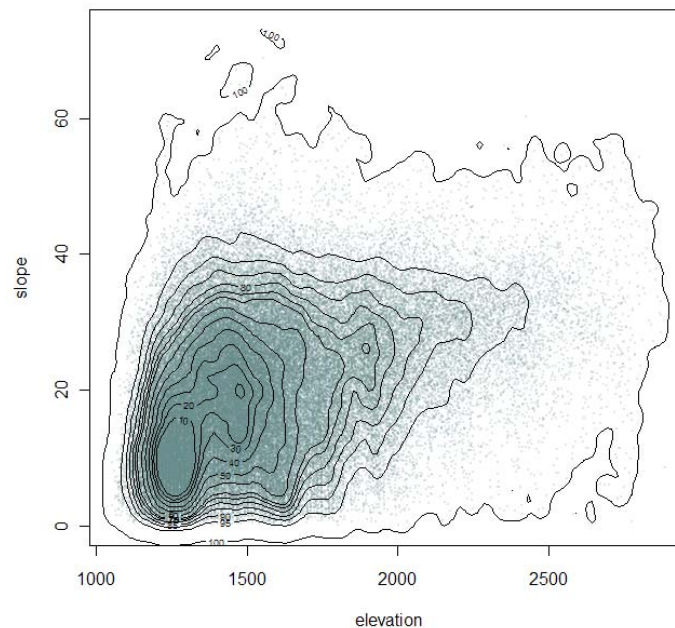
```
4 2044.320 13.4432
5 1308.766 16.5707
6 1473.009 25.7639
```

To read a dbf file into R, you will need to install and load the `foreign` package. The corresponding function is `read.dbf`.

8. To identify outliers, first use function `LF.kde` :

```
kde <- LF.kde(x=data, gridsize=151)
```

The resulting plot of the objects in *data* and the kernel density estimation should look like this:



Examine this plot to determine an appropriate density threshold (contour) beyond which cells should be classified as outliers. An appropriate threshold separates regions in attribute space densely populated by cells from those more sparsely populated. Here, for example, the 90% contour appears to be appropriate. This threshold is provided as an argument to function `LF.outlier` in step 8.

9. Identify outliers using the density threshold from Step 7:

```
out <- LF.outlier(x=kde, threshold=90)
```

The object *out* contains a variable `outlier` (accessed by `outlier$outlier`) indicating which rows of *data* are outliers (1) and which are not (0). To keep things clean, let's add this information to a column named `outlier` in the object *data*:

```
data$outlier <- out$outlier
head(data)
  elevation slope outlier
1 1655.584 29.4104    0
```

```

2 2484.788 32.2004 1
3 2057.512 20.6244 1
4 2044.320 13.4432 1
5 1308.766 16.5707 0
6 1473.009 25.7639 0

```

Next, tabulate the number of outliers in *data*:

```

table(data$outlier)
  0    1
89842 10158

```

That's 10,158 outliers (10.2%) and 89,842 non-outliers. The proportion of outliers (10.2%) differed slightly from the 10% you specified because the most extreme 10% of the 22,801 bins contained a bit more than 10% of your 100,000 raster cells.

10. Classify the non-outlier cells into land facets using the function `LF.cluster`:

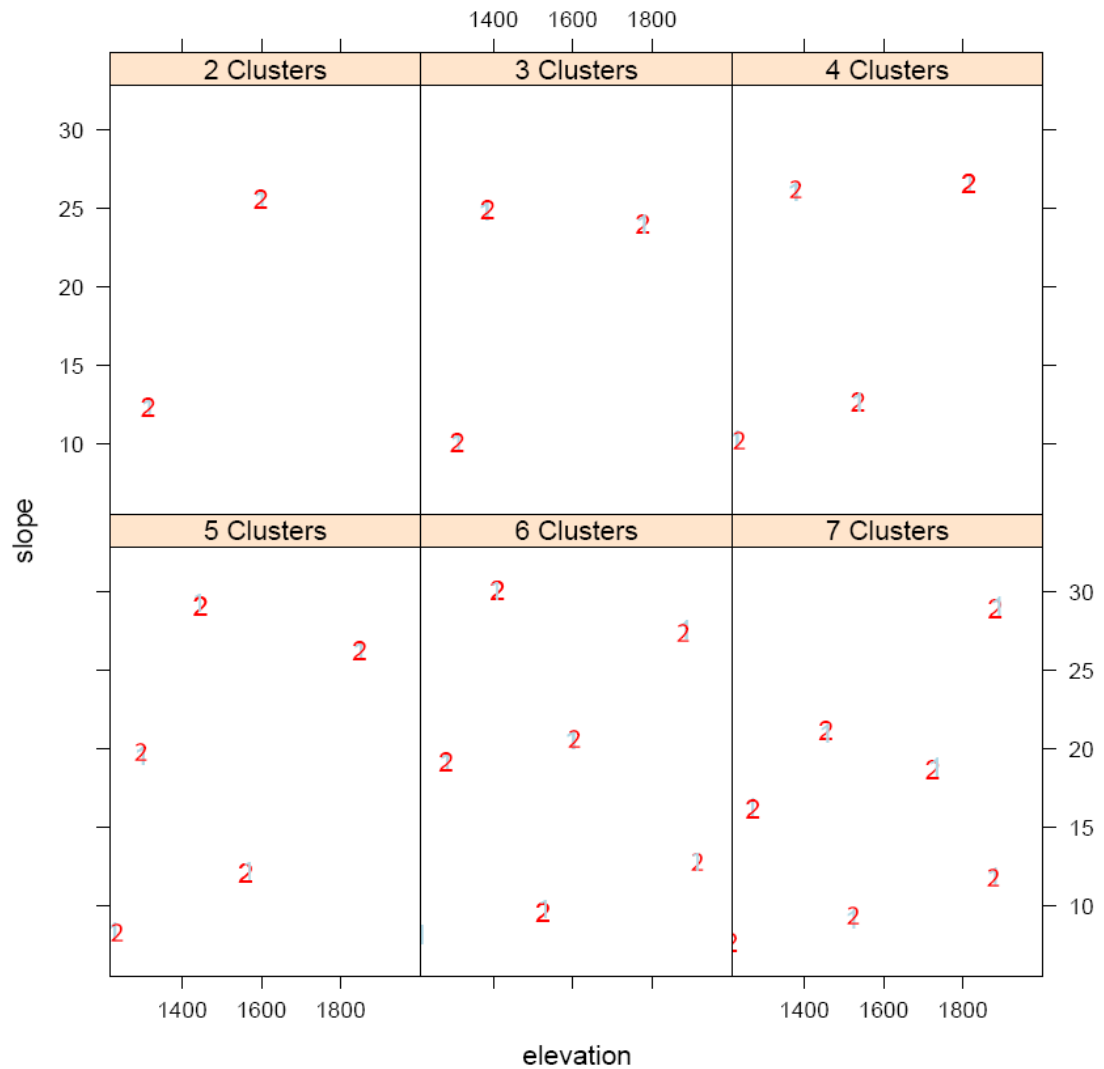
```

clust <- LF.cluster(x=data[data$outlier==0,1:2], nclust=c(2:7), niter=2, psi=1.5,
max=1000000)

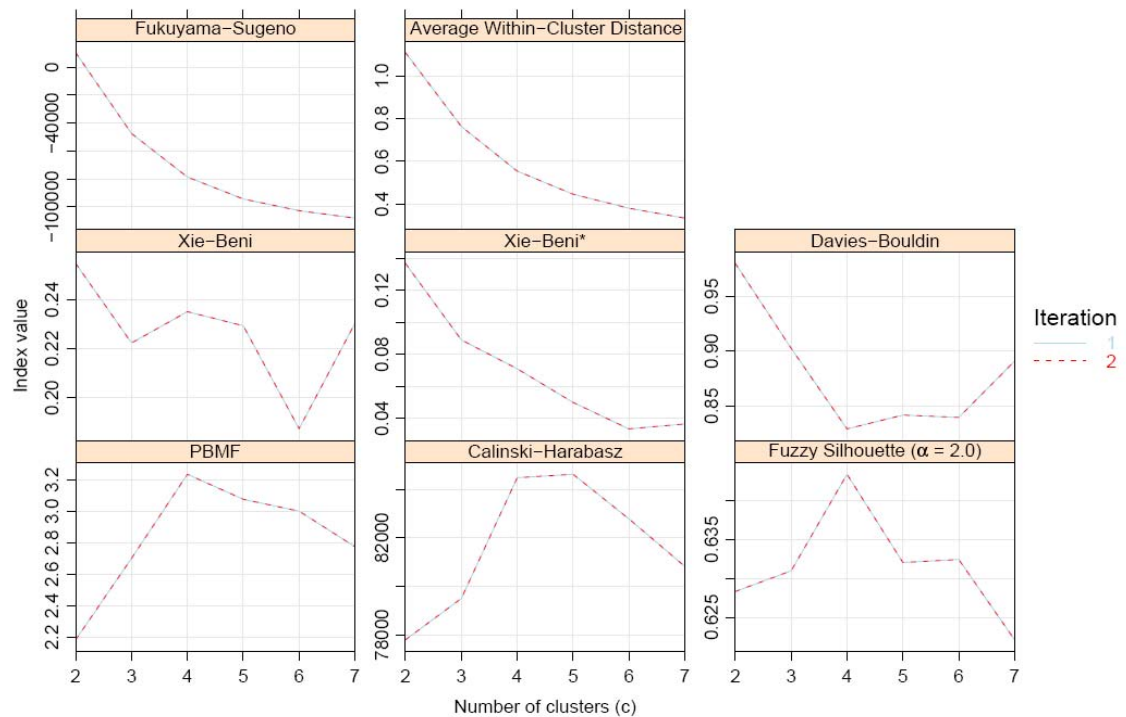
```

Note: the argument for `niter` used here is demonstration only. A larger number of iterations for each *c* (i.e., `niter=30`) is necessary to identify partitions with multiple optimal solutions.

Once `LF.cluster` is finished iterating, it generates two plots. Save each of these plots by selecting “Save as” from the “File” menu in the plot window. The first plot is a graph of cluster centroids for each iteration of each *c*. Centroids in this plot are numbered according to their iteration. In the plot, a blue “1” lies underneath each red “2,” indicating that there was only one optimal partition for each value of *c* (although performing two iterations does not give much opportunity to identify multiple optimal solutions).



The second plot is a graph of validity indices for each iteration of each c . Note that this plot will likely need to be resized to prevent panel text from getting cut-off. The top two indices are read like a scree plot, where an “elbow” in the plot indicates the optimal number of clusters. The middle three indices are minimized for the optimal partition, whereas the bottom three are maximized. This plot suggests that a four cluster solution is optimal.



11. Export information about the cluster analysis:

LF.export(x=clust, k=4)

Here, the argument **k** specifies that a 4 cluster solution was optimal. Since only one optimal partition was found for 4 clusters, **niter** (the iteration with the optimal partition) does not need to be specified. If there were two or more optimal partitions at 4 clusters, you would select the partition with the highest value in the bottom row, the lowest value in the middle row, and the “best elbow” in the top row.

12. Use the “Land Facet Clusters from R” tool in the Land Facet CorridorDesigner extension to ArcGIS to import the results from these R functions into ArcGIS. These results are contained in:

- bin_width.csv**: the (multidimensional) half-width of the bins used in the kernel density estimation
- grid.csv**: the location of bins containing non-outlier cells
- centroids.csv**: the location of cluster centroids for the optimal fuzzy-c partition
- params.csv**: the mean and standard deviation of the attributes in the data set
- psi.csv**: the value of **psi** used in the function **LF.cluster**

Recall that all of these files were outputted to the working directory.

About the Land Facet Evaluation Tools and Manual



The “About” dialog includes links to the Corridor Designer website, as well as email links to all the authors. The full manual (in PDF format) is available by clicking the “Open Manual” button.

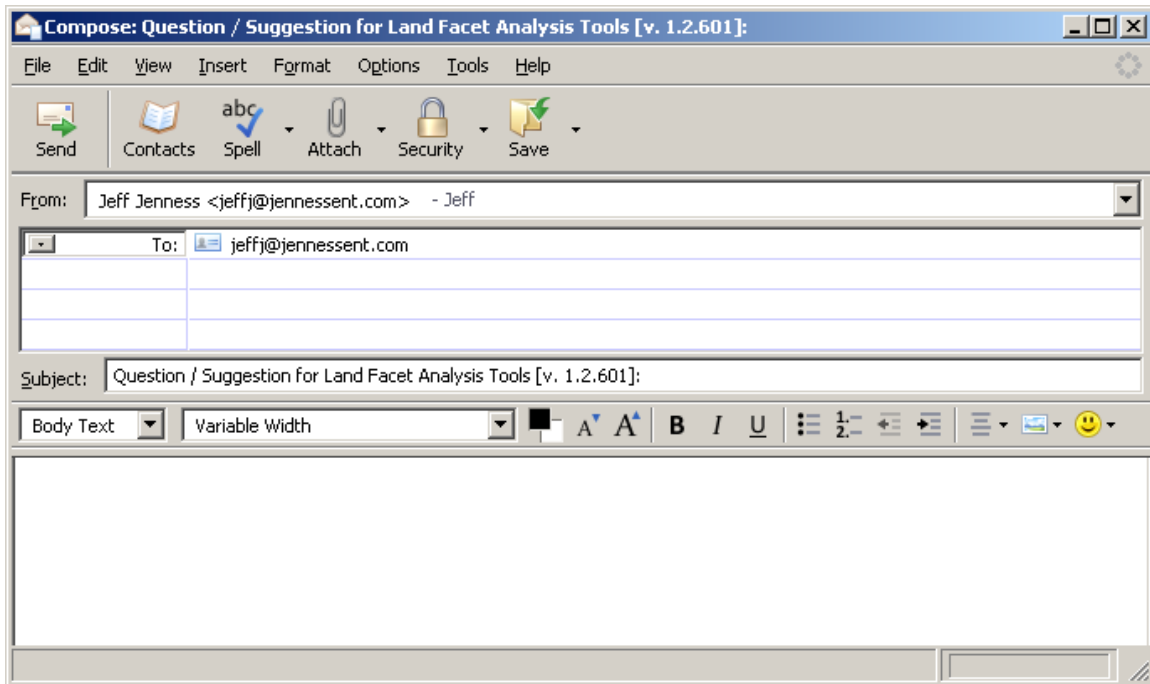
Documents Related to Land Facet Analysis

The “Additional Docs” button on the “About” dialog above will open a list of documents that may be of interest. Simply select the documents you wish to open and click ‘OK’, and your computer will open them for you.

Suggestions for Improvements?

We want these tools to be as useful as possible to you and we definitely want to correct any bugs that you might find. Many of the tools currently available here came directly from user suggestions. If you have any ideas for new methods or metrics for creating and analyzing land facets, please let us know. If we have time, we will do our best to incorporate them into the toolset.

Notice that on the “About Land Facet Corridor Analysis” dialog above, there is a “Suggestions” button. Just click that button to open up an email pre-addressed to Jeff Jenness.



Updates:

March 31, 2010:

- Version 1.2.598 – Initial Release

April 20, 2010

- Version 1.2.797
- Added a tool to identify Termini polygons
- Added documentation for all tools
- Fixed a number of bugs found in various tools

April 27, 2010

- Version 1.2.805
- Primarily modified manual to clarify and further explain several tools.
- Minor modifications to dialog control names.

June 24, 2010

- Version 1.2.808
- Several minor code changes throughout extension.
- Added discussion of R tools to the manual.

July 1, 2010

- Version 1.2.809
- Fixed a “Type Mismatch” error that occurred when you clicked the button for many of the raster tools. The error would only occur if you had a non-raster layer selected in your map when you clicked the tool.

July 20, 2010

- Version 1.2.813
- Repaired a bug in the 3-class slope position tool in which it mislabeled “canyons” as “ridges” and vice versa.

Literature Cited

- Adriaensen, F, JP Chardon, G deBlust, E Swinnen, S Villalba, H Gulinck, and E Matthysen. 2003. The application of 'least-cost' modeling as a functional landscape model. *Landscape and Urban Planning* 64:233-247.
- Beier, P, D Majka, and WD Spencer. 2008. Forks in the road: choices in procedures for designing wildlife linkages. *Conservation Biology* 22:836-851.
- Beier, P., and B. Brost. 2010. Use of land facets to plan for climate change: conserving the arenas, not the actors. *Conservation Biology*. DOI: 10.1111/j.1523-1739.2009.01422.x
- Beier, P., DR Majka, and T. Bayless. 2007. Wildlife linkage designs for the state of Arizona. Reports to Arizona Game and Fish Department, Phoenix. available at www.corridordesign.org
- Bezdek, C. J. 1981. Pattern recognition with fuzzy objective function algorithms. Plenum Press, New York
- Brost, B. 2010. Use of land facets to design linkages for climate change. Thesis, School of Forestry, Northern Arizona University.
- Clark, Joseph D., Dunn, James E., and Smith, Kimberly G. 1993. A multivariate model of female black bear habitat use for a geographic information system. *Journal of Wildlife Management*. 57:519-526.
- Conover, W. J., 1980. Practical nonparametric statistics, 2nd Ed. John Wiley and Sons. 493 p.
- Cowling, R. M., R. L. Pressey, A. T. Lombard, P. G. Desmet, and A. G. Ellis. 1999. From representation to persistence: Requirements for a sustainable system of conservation areas in the species-rich Mediterranean-climate desert of southern Africa. *Diversity and Distributions* 5:51-71.
- Cowling, R. M., R. L. Pressey, M. Rouget, and A. T. Lombard. 2003. A conservation plan for a global biodiversity hotspot---the Cape Floristic Region, South Africa. *Biological Conservation* 112:191-216.
- Dimitriadou, E., K. Hornik, F. Leisch, D. Meyer, and A. Weingessel. 2009. e1071: Misc Functions of the Department of Statistics (e1071), TU Wien. R package version 1.5-19.
- Dickson, B. and P. Beier. 2006. Quantifying the influence of topographic position on cougar (*Puma concolor*) movement In Southern California, USA. The Zoological Society of London. *Journal of Zoology*. doi: 10.1111/j.1469-7998.2006.00215.x
- Draper, Norman R. and Smith, Harry. 1998. Applied Regression Analysis, 3rd Ed. Wiley Series in Probability and Statistics. 706 p.
- Farber, Oren. and Kadmon, Ronen. 2002. Assessment of alternative approaches for bioclimatic modeling with special emphasis on the Mahalanobis distance. *Ecological Modeling*. Elsevier Science. 160:115-130.
- Golub, Gene H. and Van Loan, Charles F. 1996. Matrix computations, 3rd Ed. Johns Hopkins University Press. 694 p.
- Guisan, A., S. B. Weiss and A. D. Weiss. 1999. GLM versus CCA spatial modeling of plant species distribution. *Kluwer Academic Publishers. Plant Ecology*. 143:107-122.

- Franklin, J. 1995. Predictive vegetation mapping: Geographic modeling of biospatial patterns in relation to environmental gradients. *Progress in Physical Geography* 19:474–499.
- Hannah, L., G. F. Midgley, and D. Millar. 2002. Climate change-integrated conservation strategies. *Global Ecology and Biogeography* 11:485-495.
- Jenness Enterprises. 2006. Topographic position index. Version 1.3a. Available from: <http://www.jennessent.com> (accessed November 2009).
- Jones, K.B., D.T. Heggem, T.G. Wade, A.C. Neale, D.W. Ebert, M.S. Nash, M.H. Mehaffey, K.A. Hermann, A.R. Selle, S. Augustine, I.A. Goodman, J. Pedersen, D. Bolgrien, J.M. Viger, D. Chiang, C.J. Lin, Y. Zhong, J. Baker And R.D. Van Remortel. 2000. Assessing Landscape Conditions Relative to Water Resources in the Western United States: A Strategic Approach. *Environmental Monitoring and Assessment* 64: 227 – 245.
- Knick, Steven T. and Dyer, Deanna L. 1997. Distribution of black-tailed jackrabbit habitat determined by GIS in southwestern Idaho. *Journal of Wildlife Management*. 61:75-85.
- Lovejoy, TE, and L Hannah. 2005. Climate change and biodiversity. Yale Univ. Press.
- McCune, B., and J. B. Grace. 2002. Analysis of ecological communities. MjM Software Design, Gleneden Beach, Oregon.
- Meyer, Carl D. 2000. Matrix analysis and applied linear algebra. Society for Industrial and Applied Mathematics. Philadelphia. 718 p.
- Moore, I. D., R. B. Grayson, and A. R. Ladson. 1991. Digital terrain modeling: A review of hydrological, geomorphological, and biological applications. *Hydrological Processes* 5:3-30.
- Neter, John., Wasserman, William., and Kutner, Michael H. 1990. Applied Linear Statistical Models, 3rd Ed. 1181 p.
- Press, William H.; Teukolsky, Saul A.; Vetterling, William T., and Flannery, Brian P. 2002 Numerical recipes in C: the art of scientific computing. 2nd ed. Cambridge: Cambridge University Press; 994 pages.
- Phillips, S. J., P. Williams, G. Midgley, and A. Archer. 2008. Optimizing dispersal corridors for the Cape Proteaceae using network flow. *Ecological Applications* 18:1200-1211.
- Sanchez, P. A., et al. 2009. Digital soil map of the world. *Science* 325:680-681.
- Weiss, A. 2001. Topographic Position and Landforms Analysis. Poster presentation, ESRI User Conference, San Diego, CA. Available, by permission from the author, at http://www.jennessent.com/arcview/TPI_Weiss_poster.htm.
- Williams, P, L Hannah, S Andelman, G Midgley, M Araujo, G Hughes, L Manne, E Martinez-Meyer, and R Pearson. 2005. Planning for climate change: identifying minimum-dispersal corridors for the cape Protaceae. *Conservation Biology* 19:1063-1074.