A quick user guide to the QCMAQUIS software suite for MOLCAS

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release version 1.0

We kindly request that, for reproducibility reasons, any use of the QCMAQUIS software suite for density matrix renormalization group (DMRG) calculations in MOLCAS that results in published material should cite the set-up steered by settings and warm-up procedures described in:

Check for a preprint on arXiv.org (to appear soon).Y. Ma, S. Keller, C. Stein, S. Knecht, R. Lindh, M. Reiher, *in preparation*.

The DMRG calculations are then conducted with the software QCMAQUIS that requires a citation. It is described in the following paper:

Check for the journal article asap on arXiv.org. S. Keller, M. Dolfi, M. Troyer, M. Reiher, arXiv:1510.02026 [physics.comp-ph].

QCMAQUIS builds upon the ALPS MPS project. The ALPS MPS codes implement the DMRG algorithm for variational ground and low-lying excited state search as well as time evolution of arbitrary one- and two-dimensional models in a matrix-product-state representation. They have been developed at ETH Zurich by Michele Dolfi and Bela Bauer in the group of Matthias Troyer with contributions from Sebastian Keller and Alexandr Kosenkov and at the University of Geneva by Timothe Ewart and Adrian Kantian in the group of Thierry Giamarchi.

For further information on the ALPS project, please visit alps.comp-phys.org.

Refer to the original ALPS MPS paper:

M. Dolfi, B. Bauer, S. Keller, A. Kosenkov, T. Ewart, A. Kantian, T. Giamarchi, M. Troyer, *Comp. Phys. Commun.* **2014**, 12, 3430. doi:10.1016/j.cpc.2014.08.019

ALPS is a general open-source framework for the description of strongly correlated manyparticle systems.

B. Bauer, et al. (ALPS Collaboration), The ALPS project release 2.0: open source software for strongly correlated systems, J. Stat. Mech. **2011** P05001. http://dx.doi.org/10.1088/1742-5468/2011/05/P05001.

Contents

1	Intr	oduction to the QCMaquis Software Suite	1
	1.1	Overview and Goals	1
	1.2	What features are included in the release version 1.0?	1
		1.2.1 QCMAQUIS standalone version	1
		1.2.2 QCMAQUIS in MOLCAS	2
	1.3	Organization of this document	2
2	Soft	ware Requirements & Registration	4
	2.1	Prerequisites	4
	2.2	Registration	4
		2.2.1 QCMAQUIS standalone version	4
		2.2.2 QCMAQUIS in MOLCAS	5
3	Inst	allation	6
	3.1	QCMAQUIS standalone version	6
		3.1.1 Download QCMAQUIS	6
		3.1.2 Setting up a build folder	6
		3.1.3 Configuration	7
		3.1.4 Building and installation	8
		3.1.5 Setting up the runtime environment	8
	3.2	QCMAQUIS as external module of MOLCAS	9
		3.2.1 Download MOLCAS	9
		3.2.2 Switch to the MOLCAS-DMRG branch	10
		3.2.3 Initialization of git submodules	11
		3.2.4 Setting up a build folder	11
		3.2.5 Configuration	11
		3.2.6 Building and installation	13
		3.2.7 Setting up the runtime environment	13
	3.3	Supported operating systems and compiler environments	14
	3.4	First tests and verification of the installation	14
4	Mai	intenance	6
	4.1	New versions and patches	16

	4.2	Reporting bugs and user support	16	
5	Ger	neral Considerations for Running a QCMaquis DMRG Calculation 1'		
	5.1	Memory management and memory requirements	17	
	5.2	Files required and written by QCMAQUIS	17	
	5.3	Typical workflow for a DMRG calculation including a post-processing analysis	18	
6	Inp	ut Keywords	19	
	6.1	Keywords and Options for MOLCAS	19	
		6.1.1 Compulsory keywords	19	
		6.1.2 Optional keywords	19	
		6.1.3 Inoperative keywords	19	
		6.1.4 Molcas environment variables	21	
	6.2	Keywords and Options for QCMAQUIS	22	
		6.2.1 Compulsory keywords	22	
		6.2.2 Optional keywords	24	
		6.2.3 Keywords for expectation value calculations	27	
	6.3	QCMAQUIS tools	28	
	6.4	QCMAQUIS PYTHON scripts for wave function analysis and visualization \ldots	30	
7	Exa	mples of Molcas DMRG and QCMaquis DMRG Input Files	33	
	7.1	Example file for MOLCAS – DMRG-SCF(14,10)	33	
	7.2	Example file for QCMAQUIS– DMRG-CASCI(8,8)	34	

1 Introduction to the QCMaquis Software Suite

1.1 Overview and Goals

The QCMAQUIS software suite allows for an efficient optimization of a matrix product state (MPS) wave function based on a second-generation DMRG algorithm [1]. The quantumchemical operators are represented as matrix product operators (MPOs) which provides the necessary flexibility to accommodate abelian and non-abelian symmetries as well as the implementation of non-relativistic and relativistic quantum chemical Hamiltonians [2], respectively, in a unified framework. We have implemented the special unitary group of degree 2 (SU(2)) in the MPO representation of the non-relativistic Hamiltonian to ensure spin conservation [3]. The current implementation of QCMAQUIS allows for efficient full-CI-type calculations of active space sizes beyond capabilities ("CAS(18,18)") of standard CI approaches.

The QCMAQUIS software suite is also available [4] within the framework of MOLCAS [5] where we have implemented a state-specific and state-average DMRG self-consistent field (DMRG-SCF) algorithm, the possibility to include solvent effects in DMRG calculations and provide analytic gradients for state-specific calculations. The latter enables structure optimization within the QCMAQUIS DMRG framework.

Advice: The break-even point wrt computational cost for a DMRG-CI/-SCF calculation compared to a "traditional" CAS-CI/-SCF calculation is approximately reached for a CAS(14,14) space. For active spaces smaller than CAS(14,14) we recommend to choose a traditional MOLCAS CAS approach.

1.2 What features are included in the release version 1.0?

1.2.1 QCMaquis standalone version

The release version 1.0 of the QCMAQUIS software suite includes:

- optimization of spin-adapted SU(2) MPS wave functions with the DMRG algorithm
- non-relativistic and scalar-relativistic quantum-chemical Hamiltonians

- calculation of excited states
- a python tool set to analyze the MPS wave function and its quantum entanglement

1.2.2 QCMaquis in Molcas

The release version 1.0 of the QCMAQUIS software suite in MOLCAS supports:

- DMRG-CI and DMRG-SCF calculations w/wo reaction field (e.g. PCM)
- State-specific and state-averaged DMRG-SCF calculations
- Analytic gradients for state-specific DMRG-SCF calculations

1.3 Organization of this document

In the following we list and briefly summarize the remaining sections of this document.

- Section 2, Software Requirements & Registration, guides through the software requirements and the registration process for QCMAQUIS.
- Section 3, Installation, guides through the installation process for QCMAQUIS (and possibly the host program MOLCAS).
- Section 4, Maintenance, summarizes general information concerning the QCMAQUIS software suite including how to ask for user support, retreive future patches for the code and where to send bug reports.
- Section 5, General Considerations for Running a QCMAQUIS DMRG Calculation, introduces the basic workflow for QCMAQUIS DMRG calculations and provides details about memory requirements as well as input and output data required and generated by QCMAQUIS, respectively.
- Section 6, Input Keywords, provides in the first part a list of keywords and options to control QCMAQUIS DMRG calculation in MOLCAS. The second part explains in detail all mandatory and optional QCMAQUIS keywords and their usage. In addition we introduce several tools that are part of the QCMAQUIS software suite which can be used to analyze and visualize the resulting DMRG wave function(s).

• Section 7, Examples of MOLCAS DMRG and QCMAQUIS DMRG Input Files, then shows two example input files for QCMAQUIS DMRG calculations in MOLCAS and with the QCMAQUIS standalone suite, respectively.

2 Software Requirements & Registration

2.1 Prerequisites

In order to install either QCMAQUIS or the developers version of the quantum chemistry package MOLCAS with DMRG support through the QCMAQUIS software suite [1, 4], requires the following libraries/programs:

- Git
- Python version 2.x with $x \ge 5$
- HDF5 (http://www.hdfgroup.org/HDF5)
- GNU Scientific Library GSL (http://www.gnu.org/software/gsl/)
- CMake version 3.x with $x \ge 0$ (https://cmake.org/)

Please make sure that these libraries/programs are available and their location is visible in your **\$PATH** and **\$LD_LIBRARY_PATH**, respectively. Note that these libraries are <u>NOT</u> part of the installation package of the QCMAQUIS software suite (see Section 3 for further details).

Warning! The combined installation of MOLCAS and QCMAQUIS requires to follow the CMake installation of MOLCAS, whereas a "configure"-based installation is <u>NOT</u> possible. A detailed step-by-step installation guide is provided in Section 3.2.

2.2 Registration

QCMAQUIS can be installed either as standalone version (Section 3.1) or as external module of the quantum chemistry software MOLCAS (Section 3.2). In the former case proceed with the registration as described in Section 2.2.1 else with Section 2.2.2.

2.2.1 QCMaquis standalone version

The use of the standalone version of the QCMAQUIS software suite requires a registration at http://tc-gitlab.ethz.ch. To sign up at http://tc-gitlab.ethz.ch please send an e-mail to dmrg@phys.chem.ethz.ch. After confirmation of your registration, login to http: //tc-gitlab.ethz.ch and upload your local public ssh key to your gitlab profile. Verify that
you have been granted access to the following projects, for example, they should be listed on
the right as projects you are enrolled at:

- QCMAQUIS/QCMAQUIS-PUBLIC
- QCMAQUIS/QCMAQUIS-SRC .

If this is not the case, please send a notification to dmrg@phys.chem.ethz.ch.

2.2.2 QCMaquis in Molcas

The use of the QCMAQUIS software suite in MOLCAS requires (apart from a valid MOLCAS developers license) a registration at http://tc-gitlab.ethz.ch. To sign up at http://tc-gitlab.ethz.ch. To sign up at http://tc-gitlab.ethz.ch. After confirmation of your registration, login to http://tc-gitlab.ethz.ch and upload your local public ssh key to your gitlab profile. Verify that you have been granted access to the following projects, for example, they should be listed on the right as projects you are enrolled at:

- QCMAQUIS/QCMAQUIS-PUBLIC
- QCMAQUIS/QCMAQUIS-SRC
- MOLCAS-DEV/HDF5-UTILS
- MOLCAS-DEV/DMRG-INTERFACE-UTILS .

If this is not the case, please send a notification to dmrg@phys.chem.ethz.ch.

3 Installation

Section 3.1 describes in details the installation process for a standalone version of QCMAQUIS. Ton install QCMAQUIS as external module of the quantum chemistry software MOLCAS proceed to Section 3.2.

3.1 QCMaquis standalone version

In the following steps 3.1.1-3.1.5 we describe how to successfully build and install the QC-MAQUIS software suite. The installation of QCMAQUIS has been tested for different operating systems and compiler/math libraries environments. Their list can be found in Section 3.3. While other combinations might work equally well they are <u>not</u> officially supported. The installation of the QCMAQUIS software suite will comprise several libraries which are automatically downloaded and installed during the QCMAQUIS build process

- QCMAQUIS
- Boost
- ALPS

All of the above libraries will be installed locally in the user-defined build folder my-QCMaquis-build.

3.1.1 Download QCMaquis

Type

```
git clone git@tc-gitlab.ethz.ch:qcmaquis/qcmaquis-public.git my-QCMaquis-src
```

to download a new local QCMAQUIS repository in the source folder my-QCMaquis-src.

3.1.2 Setting up a build folder

Create a build folder my-QCMaquis-build – note that this folder <u>does not</u> necessarily have to be a subfolder of my-QCMaquis-src – and change to this new folder:

mkdir /path/to/my-QCMaquis-build && cd /path/to/my-QCMaquis-build

3.1.3 Configuration

Table 1 in Section 3.3 summarizes the list of tested and supported operating system and compiler combinations for the installation of QCMAQUIS. Below we will show the configuration steps for the most popular compiler suites GNU (Section 3.1.3.1) and Intel (Section 3.1.3.2), respectively. How to setup and use a shared-memory OMP installation of QCMAQUIS is described in Section 3.1.3.3.

3.1.3.1 Configuration with the GNU compiler suite

To configure QCMAQUIS with the GNU compiler suite type

```
FC=gfortran CC=gcc CXX=g++ cmake -DQCM_standalone=ON /path/to/my-QCMaquis-src
```

where we assumed that the Intel Math Kernel Library (MKL) is available (recommended option). If the MKL libraries are not available QCMAQUIS will search for other suitable math libraries installed on the operating system. If none are found the configuration step will stop with an appropriate message.

3.1.3.2 Configuration with the Intel compiler suite

To configure QCMAQUIS with the Intel compiler suite including MKL type

FC=ifort CC=icc CXX=icpc cmake -DQCM_standalone=ON /path/to/my-QCMaquis-src

3.1.3.3 Shared-memory OMP parallel configuration

By default QCMAQUIS is built as shared-memory OMP parallelized version which should work with either compiler suite, GNU or Intel.

In order to exploit the shared-memory OMP parallelization of QCMAQUIS the user is strongly encouraged to set at runtime the environment variable

export OMP_NUM_THREADS=XX

where XX specifies the number of shared-memory cores to be used. The default (<u>depending</u> on the operating system!!!) is to use a single core.

3.1.4 Building and installation

After a successful configuration, type

make

or

```
make -j8
```

to compile QCMAQUIS (in parallel on 8 cores) and install all its components in the build folder my-QCMaquis-build. In the same folder BOOST and ALPS will be downloaded and installed, respectively. The installation process thus requires a working internet connection.

3.1.5 Setting up the runtime environment

After having successfully passed the QCMAQUIS installation step as indicated by CMake messages like

[xxx%] Built target alps
...
[xxx%] Built target qcmaquis

and

```
[xxx%] Installation of QCMaquis, ALPS and Boost was successful!
```

adjust your runtime environment variables (assuming a bash environment) as follows:

```
export PATH=/path/to/my-QCMaquis-build/alps/bin:$PATH
```

export PATH=/path/to/my-QCMaquis-build/qcmaquis/bin:\$PATH

export PYTHONPATH=/path/to/my-QCMaquis-build/alps/lib:\$PYTHONPATH

```
export PYTHONPATH=/path/to/my-QCMaquis-build/qcmaquis/lib/python/pyeval:$PYTHONPATH
```

```
export PYTHONPATH=/path/to/my-QCMaquis-build/qcmaquis/lib/python:$PYTHONPATH
```

```
On Linux systems (x86_64) set in addition
```

```
export LIBRARY_PATH=/path/to/my-QCMaquis-build/alps/lib:$LIBRARY_PATH
export LD_LIBRARY_PATH=/path/to/my-QCMaquis-build/alps/lib:$LD_LIBRARY_PATH
whereas on Mac OS X set
```

export LIBRARY_PATH=/path/to/my-QCMaquis-build/alps/lib:\$LIBRARY_PATH export DYLD_LIBRARY_PATH=\$LIBRARY_PATH:\$DYLD_LIBRARY_PATH

Full instructions ready for copy+paste will also be printed on the screen and shall be copied to either your local \$HOME/.bashrc file, or be executed in the QCMAQUIS bash session.

<u>Alternative</u>: use the "sourceable" configuration file qcmaquis.sh that is created after the build/install step succeeded. To do so type

```
source /path/to/my-QCMaquis-build/qcmaquis/bin/qcmaquis.sh
```

3.2 QCMaquis as external module of Molcas

In the following steps 3.2.1-3.2.7 we describe how to successfully build and install the MOLCAS program together with the QCMAQUIS software suite. The installation of QCMAQUIS has been tested for different operating systems and compiler/math libraries environments. Their list can be found in Section 3.3. While other combinations might work equally well they are not officially supported.

The installation of the QCMAQUIS software suite within MOLCAS will comprise several libraries which are <u>automatically downloaded and installed</u> during the MOLCAS build process provided that DMRG support within MOLCAS is requested by the user. The list of external libraries comprises:

- QCMAQUIS
- QCMAQUIS-driver-utils
- Boost
- ALPS

All of the above libraries will be installed locally in the user-defined build folder my-Molcas-build of MOLCAS.

3.2.1 Download Molcas

If you already have a local MOLCAS repository in my-Molcas-src that points to the remote repository git@molcas:molcas skip this section, otherwise choose either to download a new local MOLCAS repository (Section 3.2.1.1) or add a new remote repository to an existing local

MOLCAS repository (in my-Molcas-src) that does <u>NOT</u> yet have a pointer to the remote repository git@molcas:molcas (Section 3.2.1.2).

3.2.1.1 Cloning a new local Molcas repository

Type

git clone --recursive git@molcas:molcas my-Molcas-src

to download a new local MOLCAS repository in the source folder my-Molcas-src.

3.2.1.2 Adding a new remote repository to an existing local Molcas repository Type

git remote add gitsrc_molcas git@molcas:molcas

to add the additional remote repository gitsrc_molcas that hosts the MOLCAS-DMRG branch to your local MOLCAS repository (which we assume in the following to be located in my-Molcas-src). To obtain all remote informations from gitsrc_molcas type next

git fetch gitsrc_molcas

3.2.2 Switch to the Molcas-DMRG branch

QCMAQUIS is available on the master branch of MOLCAS which is the default branch that you currently reference if you "git cloned" a new local MOLCAS repository in the previous step. Typing

git branch

should then yield something like

* master

The "*" in front of the branch name indicates which local branch you are currently tracking. In this particular case you are tracking the branch master.

If you added a new remote repository ("gitsrc_molcas") to your existing local MOLCAS repository (see Section 3.2.1.2) type

git checkout -b dmrg-master gitsrc_molcas/master

Typing next

git branch

should then yield something like

master

*dmrg-master

The "*" in front of the branch name indicates which local branch you are currently tracking. In this particular case you successfully switched to track the development branch dmrg-master.

3.2.3 Initialization of git submodules

Type

```
git submodule update --init --recursive
```

to initialize (and possibly download) the necessary git submodules of MOLCAS.

3.2.4 Setting up a build folder

Create a build folder my-Molcas-build – note that this folder <u>does not</u> necessarily have to be a subfolder of my-Molcas-src – and change to this new folder:

mkdir /path/to/my-Molcas-build && cd /path/to/my-Molcas-build

3.2.5 Configuration

Table 1 in Section 3.3 summarizes the list of tested and supported operating system and compiler combinations for the simultaenous installation of MOLCAS and QCMAQUIS. Below we will show the configuration steps for the most popular compiler suites GNU (Section 3.2.5.1) and Intel (Section 3.2.5.2), respectively. How to setup an MPI-parallel MOLCAS installation is described in Section 3.2.5.3.

Note! We strongly recommend to configure QCMAQUIS (and MOLCAS) with the Intel Math Kernel Library (MKL) to ensure the best numerical performance.

3.2.5.1 Configuration with the GNU compiler suite

To configure MOLCAS and QCMAQUIS with the GNU compiler suite type

FC=gfortran CC=gcc CXX=g++ cmake -DDMRG=ON -DLINALG=MKL /path/to/my-Molcas-src where we assumed (-DLINALG=MKL) that the MKL libraries are available (recommended option). If the MKL libraries are not available internal math libraries of MOLCAS can be requested with -DLINALG=Internal (default option for LINALG in MOLCAS).

3.2.5.2 Configuration with the Intel compiler suite

To configure MOLCAS and QCMAQUIS with the Intel compiler suite including MKL type FC=ifort CC=icc CXX=icpc cmake -DDMRG=ON -DLINALG=MKL /path/to/my-Molcas-src

3.2.5.3 MPI-parallel and shared-memory OMP parallel configurations

Installing an MPI-parallel version of MOLCAS with DMRG support is possible although QC-MAQUIS itself is by default shared-memory OMP but <u>not</u> yet MPI-parallelized. To configure MOLCAS for an MPI-installation type

FC=mpif90 CC=mpicc CXX=mpiCXX cmake -DDMRG=ON /path/to/my-Molcas-src

A shared-memory OMP parallelized version of MOLCAS can be activated with the option -DOPENMP=ON passed to cmake during the configuration step, for example

FC=... CC=... CXX=... cmake -DDMRG=ON -DOPENMP=ON /path/to/my-Molcas-src

It should work with either compiler suite, GNU or Intel, but the user may want to consult the MOLCAS user manual for further information.

In order to exploit the shared-memory OMP parallelization of QCMAQUIS which is enabled by default the user is strongly encouraged to set at runtime the environment variable

export QCMaquis_CPUS=XX

where XX specifies the number of shared-memory cores to be used. The default is to use a single core.

3.2.6 Building and installation

After a successful configuration, type

make

or

```
make -j8
```

to compile MOLCAS (in parallel on 8 cores) and install all its components in the build folder my-Molcas-build. In the same folder QCMAQUIS as well as the required BOOST and ALPS libraries will be downloaded and installed, respectively. The installation process thus requires a working internet connection.

3.2.7 Setting up the runtime environment

After having successfully passed the QCMAQUIS installation step as indicated by CMake messages like

```
[xxx%] Built target alps
...
[xxx%] Built target qcmaquis
```

and

[xxx%] Installation of QCMaquis, ALPS and Boost was successful!

adjust your runtime environment variables (assuming a bash environment) as follows:

export PATH=/path/to/my-Molcas-build/alps/bin:\$PATH

export PATH=/path/to/my-Molcas-build/qcmaquis/bin:\$PATH

export PYTHONPATH=/path/to/my-Molcas-build/alps/lib:\$PYTHONPATH

export PYTHONPATH=/path/to/my-Molcas-build/qcmaquis/lib/python/pyeval:\$PYTHONPATH

```
export PYTHONPATH=/path/to/my-Molcas-build/qcmaquis/lib/python:$PYTHONPATH
```

```
On Linux systems (x86_64) set in addition
```

```
export LIBRARY_PATH=/path/to/my-Molcas-build/alps/lib:$LIBRARY_PATH
export LD_LIBRARY_PATH=/path/to/my-Molcas-build/alps/lib:$LD_LIBRARY_PATH
whereas on Mac OS X set
```

export LIBRARY_PATH=/path/to/my-Molcas-build/alps/lib:\$LIBRARY_PATH export DYLD_LIBRARY_PATH=\$LIBRARY_PATH:\$DYLD_LIBRARY_PATH

Full instructions ready for copy+paste will also be printed on the screen and shall be copied to either your local **\$HOME/.bashrc** file, or be executed in the MOLCAS bash session.

<u>Alternative</u>: use the "sourceable" configuration file qcmaquis.sh that is created after the build/install step succeeded. To do so type

```
source /path/to/my-Molcas-build/qcmaquis/bin/qcmaquis.sh
```

3.3 Supported operating systems and compiler environments

Table 1 summarizes tested and officially supported operating system/compiler/math library combinations for building MOLCAS together with the QCMAQUIS software suite. Note that other combinations might work equally well but they are not officially supported at present. See the MOLCAS manual at www.molcas.org for details on supported operating systems and compiler environments of a "plain" MOLCAS installation.

 Table 1: Supported operating system/compiler/math library combinations for the combined installation of MOLCAS and QCMAQUIS.

operating system	compiler	math library
Mac OS X (10.11 "El Capitan")	GNU 5.2	"Accelerate" (Xcode)
Mac OS X (10.11 "El Capitan")	Intel XE 15 (patch 0)	MKL 11.2
x86_64	Intel XE 15 (patch 0)	MKL 11.2
x86_64	GNU 4.8	MKL 11.1
x86_64	GNU 4.7.2	MKL 11.1
x86_64	Intel XE 13	MKL 11.1
x86_64	Intel XE 13 (sp 1)	MKL 11.1
x86_64	OpenMPI 1.6.5 + Intel XE 13 (sp 1)	MKL 11.1

3.4 First tests and verification of the installation

To verify that your installation of MOLCAS and QCMAQUIS was successful, type in your build folder my-Molcas-build

molcas verify qcmaquis

A message like

Verification has been completed

indicates that all tests passed correctly and your installation is good to go for production work.

Note that all test inputs can be found in my-Molcas-build/test/qcmaquis. They may also serve as sample inputs for your actual calculation. Table 2 comprises a short summary of the seven tests for QCMAQUIS covering different computational aspects within the MOLCAS framework.

Table 2: List of test inputs that are stored in my-Molcas-build/test/qcmaquis.

file	type	details
001.input	State-specific	introduces the DMRG keyword under the RASSCF card
002.input	State-average	two-state (S_0/S_1) DMRG-SCF of N_2
003.input	DMRG-CI	dynamic list of renormalized states m
004.input	State-specific	structure optimization of the ground state of dioxetanone
005.input	State-specific	structure optimization of the S_1 state of N_2
006.input	PCM model	DMRG-SCF for a non equilibrium state
007.input	State-specific	DMRG-SCF with manual orbital ordering

4 Maintenance

4.1 New versions and patches

New versions of the QCMAQUIS and/or QCMAQUIS-driver software suite as well as possible bug fixes will be announced on the QCMAQUIS homepage. The latter patches will be made available as git commit(s) on the QCMAQUIS repository at http://tc-gitlab.ethz.ch that can be directly applied ("git merge"d) to the user's release version of QCMAQUIS.

4.2 Reporting bugs and user support

The QCMAQUIS program suite is distributed to the MOLCAS community with no obligations on the side of the authors. The authors thus take no responsibility for the performance of the code nor for the correctness of the results. This distribution policy gives the authors no responsibility for problems experienced by the users when using the QCMAQUIS program in MOLCAS.

Bugs/suggestions for improvements are to be reported as <u>issues</u> on the <u>gitlab</u> server. Please open an issue concerning:

- QCMAQUIS on the project page QCMaquis/QCMaquis-public
- QCMAQUIS in MOLCAS on the project page molcas-dev/dmrg-interface-utils

Any issue will be dealt with by one of the authors, although no responsibility on the promptness of response is given. In general, serious bugs that have been reported and fixed will lead to a new patch of the QCMAQUIS program, announced and distributed from the QCMAQUIS homepage.

5 General Considerations for Running a QCMaquis DMRG Calculation

Running a QCMAQUIS DMRG calculation — either DMRG-CI or DMRG-SCF — within the framework of MOLCAS involves the QCMAQUIS host program driver described in Ref. [4]. In doing so, MOLCAS-DMRG calculations are easily accessible since they are integrated in the RASSCF module of MOLCAS. Hence, if the user considers to run a MOLCAS-DMRG calculation rather than doing a standalone QCMAQUIS DMRG calculation section 5.3 may be skipped.

5.1 Memory management and memory requirements

The memory layout of QCMAQUIS is designed for large multinode architectures and therefore the memory consumption on a single node is not consequently minimized.

Note that if you run a MOLCAS-QCMAQUIS DMRG calculation, the memory consumption and memory allocation of QCMAQUIS is entirely <u>disconnected</u> from the host program MOLCAS. This in turn means that the amount of core memory assigned to the host program should be carefully chosen. For example, DMRG-SCF calculations for large active spaces will not require a considerably larger amount of memory in the RASSCF module (apart from memory for reduced one- and two-particle density matrices that scale approximately with the number of active orbitals N_{act} as N_{act}^2 and N_{act}^4 , respectively) than regular CASSCF calculations with modest-sized active spaces. The reason being that in the former case we do not need to reserve memory for CI vector(s) expansions which grow roughly factorily with the number of electrons and N_{act} .

5.2 Files required and written by QCMaquis

QCMAQUIS requires only two files to start a calculation, (i) an input file, named for example dmrg-input that includes all keywords and options as specified in Section 6.2 and (ii) an integral file in the FCIDUMP format as described in Ref. [6]. The latter can be produced for example with the MOLCAS/QCMAQUIS-host program driver described in Ref. [4]. Different types of reference orbitals may be used as starting orbitals for a QCMAQUIS DMRG calculation.

QCMAQUIS produces two types of files, (i) a result-file in which all information on, e.g. the energies and expectation values, is stored and (ii) a checkpoint-folder which contains the matrix product state (MPS) wave function. The checkpoint-folder is required for a later restart of the calculation, while the tools and the analysis scripts described in Sections 6.3 and 6.4, respectively, require either a result-file or a checkpoint-folder or both. All data is stored in the hdf5 format.

5.3 Typical workflow for a DMRG calculation including a postprocessing analysis

The usual workflow to set up, run and analyze a DMRG calculation proceeds as follows:

- prepare an FCIDUMP integral file [6] using the MOLCAS-QCMAQUIS host program driver [4]) starting from a set of previously computed reference orbitals
- prepare an input file dmrg-input starting for example from the template input file provided in Section 7.2 and adjust all molecular system and wave function specific parameters (for example nelec, spin, irrep, L, ..., see Sections 6.2.1-6.2.3 for a list of all compulsory and optional input arguments)
- run the DMRG calculation with dmrg dmrg-input (| tee out)
- compute expectation values with dmrg_meas dmrg-input
- analyze the results using the PYTHON tools provided with the QCMAQUIS package (see Sections 6.3 and 6.4, respectively, for a list of utility programs and scripts)

6 Input Keywords

Caution! Be aware of underscores "_" in some of the QCMAQUIS or MOLCAS keywords. They might get lost when you copy+paste keywords from this pdf to your input file.

6.1 Keywords and Options for Molcas

6.1.1 Compulsory keywords

This section describes the QCMAQUIS input to the RASSCF program within the MOLCAS program system. The minimal input to run a DMRG-SCF calculation with QCMAQUIS in the framework of the RASSCF program is

&RASSCF

DMRG

where the keyword DMRG is compulsory to activate the DMRG functionality in MOLCAS.

6.1.2 Optional keywords

Table 3 summarizes optional keywords under the RASSCF input card that allow to control the type of DMRG calculation, that is, DMRG-SCF, DMRG-CI or just a dump of information (input, one- and two-electron integrals) to perform a DMRG calculation outside of MOLCAS. The detailed input control for QCMAQUIS in MOLCAS is designed such that parameters between the RGINput and ENDRG section of the RASSCF input card only affect QCMAQUIS that is, they have no effect within the RASSCF module of MOLCAS. These parameters are described in Section 6.2.

6.1.3 Inoperative keywords

Table 4 comprises a list of keywords under the RASSCF input card which are have no meaning when a DMRG calculation is requested.

 $\label{eq:Table 3: Optional keywords under the RASSCF card to control the DMRG calculation.$

keyword	description
	RGInput marks the beginning of the QCMAQUIS parameter
	control section while ENDRG marks its end. Any
	QCMAQUIS-internal keyword can be forwarded directly to
RGINput	$\operatorname{QCMAQUIS}$ by replacing the $\tt XXX$ with a list of keywords, each
XXX	keyword in a new line. A list of compulsory, optional, and
ENDRG	property calculation keywords for QCMAQUIS are described in
	Sections 6.2.1-6.2.3.
	Notable exceptions are the active-space and wave function \mathbf{N}
	symmetry dependent parameters L, nelec, spin, irrep that
	will be forwarded automatically by MOLCAS.
CIONLY	This keyword disables orbital optimization. A single DMRG-CI calculation is performed instead.
	This keyword disables orbital <u>and</u> wave function optimization,
ECTDUMD	a formatted integral file named "ECIDIMP" (see Ref. [6] for a
FCIDUMP	detailed description of the format) which can be used in
	subsequent OCMAQUE DMBC calculations
	subsequent & MAQUIS DMITCH Calculations.
	Initial electronic configuration for the calculated state(s). For the
	calculation of a single state this is equivalent to the $\mathtt{hf_occ}$ card
SOCCupy	in the QCMAQUIS input (see Section 6.2). The occupation is
	inserted as a string of blank space separated aliases of occupations
	of the active (RAS2) orbitals with the aliases $2 = $ full, $u = $ up,
	d = down, 0 = empty.

Table 4: Inoperative keywords in the RASSCF section when DMRG is active.

keyword	description
RASScf	This keyword is not available because it is not possible to restrict the excitation level between subspaces in DMRG calculations.
TIGHt	This keyword is not available because the Jacobi-Davidson diagonalization is independent and can be controlled with the ietl_jcd_tol and ietl_jcd_maxiter parameters (see Section 6.2)
	in the RGINPUT section.

6.1.4 Molcas environment variables

As described in Section 3.2.5.3 QCMAQUIS is built by default with a shared-memory OMP parallelization. To speedup calculations the user can thus set at runtime the environment variable

export QCMaquis_CPUS=XX

where XX specifies the number of shared-memory cores to be used. The default is to use a single core.

6.2 Keywords and Options for QCMaquis

In the following we describe (i) compulsory keywords (Section 6.2.1), (ii) optional keywords (Section 6.2.2) for QCMAQUIS DMRG calculations as well as (iii) keywords for property calculations (Section 6.2.3). Most of the QCMAQUIS keywords have default settings that guarantee convergence in the general case and are inserted automatically by the host program (MOLCAS in this case). A reasonable choice of default values for optional keywords is given in our example QCMAQUIS input file in Section 7.2.

Caution! MAQUIS has many features beyond quantum chemistry, e.g. related to solid state physics. Some keywords listed in the example file in Section 7.2 are therefore not explained in the following and are not to be changed, if a quantum chemical calculation is desired.

6.2.1 Compulsory keywords

The keywords in Table 5 have to be set for every DMRG calculation since they may crucially affect the accuracy of the final result. Their choice depends for example on the molecule under consideration (do you expect strong static electron correlation and/or dynamical correlation to play a major role), the nature of the reference orbitals (Hartree-Fock orbitals, natural orbitals of some kind, ...), the size of the active space, and many other aspects.

Note! We strongly encourage any new user of QCMAQUIS or QCMAQUISin-MOLCAS to carefully read first Ref. [7] which gives a detailed introduction to DMRG calculations in quantum chemistry. Further quantum chemical DMRG sample calculations starting from different computational setups are discussed for example in Refs. [4, 8, 9, 10].

Some of the compulsory keywords listed in Table 5 are indeed automatically set if you run a QCMAQUIS DMRG calculation through the QCMAQUIS host program driver which is the case for MOLCAS-QCMAQUIS DMRG calculations. In this case skip the upper part of Table 5 and proceed immediately to the lower part marked by "Keywords <u>NOT</u> set by the host program MOLCAS".

keyword	description
	Keywords set by the host program MOLCAS
nelec	Total number of electrons.
irrep	Irreducible representation of the point group symmetry of the target state. Note: Counting starts with 0 which has to be the totally symmetric representation.
spin	Total spin $(2 \times S)$ of the target state, for example: spin=0 (singlet), spin=1 (doublet), spin=2 (triplet),
L	Length of lattice = number of orbitals in the active space.
integral_file	Path and filename of the integral file, for example integral_file = /path/to/file/FCIDUMP
chkpfile	Path and name of the folder in which the MPS is stored.
resultfile	Path and filename of the result file.
n_ortho_states	If an excited state calculation is desired, the number of states the current wave function is to be orthogonalized against shall be specified here.
ortho_states	Path(s) and filename(s) of the MPS checkpoint file(s) that store the lower lying states to which the current MPS shall be orthogonal to.

Table 5: Compulsory keywords to be set in all QCMAQUIS DMRG calculations.

Table 5 – continued from previous page		
keyword	description	
	Possible options are default, thin and hf. The default and	
	thin initializations fill the initial MPS with random numbers, the	
	difference being that a singular value decomposition reduces the	
	bond dimension to init_bond_dimension in the case of thin.	
init_state	Usage of hf generates an MPS consisting of only the determinant	
	defined on the $\mathtt{hf_occ}$ card. Note that the CI-DEAS procedure	
	[11, 4] (as invoked by dmrginit.py, see Section 6.4) behaves like a	
	restart from the newly generated CI-DEAS MPS.	
	default in Molcas: init_state = "default"	
Ke	ywords <u>NOT</u> set by the host program MOLCAS	
	Maximum number of renormalized states (commonly referred to	
max_bond_dimension	as m -value or virtual bond dimension) kept during each	
	microiteration step of a forward- or backward sweep.	
	Maximum number of DMRG sweeps. Please be aware that	
nsweeps	$\tt nsweeps$ sets the number of combined forward and backward	
	sweeps. Thus, the actual number of sweeps is $2 \times nsweeps$.	

6.2.2**Optional keywords**

The keywords summarized in Table 6 may be exploited by the more experienced user but can be safely ignored by those who just want to get started. They may affect the convergence and accuracy of the final result, though. For the inexperienced user however, we advise to not change these settings and accept the default values provided by QCMAQUIS.

keyword	description
orbital_order	Manual ordering of the orbitals along the one dimensional lattice. The order has to be entered as a string of comma separated orbital numbers. We recommend the Fiedler ordering based on the mutual information [4, 12] which can be obtained by means of the python script fiedler.py (see Section 6.4). default: orbital_order = "1,2,3,4,5,6,"
sweep_bond_dimensions	Sets max_bond_dimension for each sweep separately. <u>Note</u> : Replaces max_bond_dimension which does <u>NOT</u> need to be specified in this case. Example (nsweeps=3): sweep_bond_dimensions="300,400,500"
init_bond_dimension	Adjusts the maximal bond dimension of the MPS produced by the CI-DEAS procedure [11, 4].
conv_thresh	Sets the energy convergence threshold (in Hartree). If the lowest energy from the previous sweep differs from the lowest energy of the current sweep by less than conv_thresh, the DMRG calculation stops. <u>Note</u> : Requires to set also truncation_final and ietl_jcd_tol. Numerical format: xe-y with x and y being integers. Example: conv_thresh = 1e-6.
ietl_jcd_tol	Convergence threshold for the Jacobi-Davidson diagonalization. Numerical format: xe-y with x and y being integers. Example: ietl_jcd_tol = 1e-6.
ietl_jcd_maxiter	Maximum number of iterations in the Jacobi-Davidson diagonalization.

 Table 6: Optional keywords for QCMAQUIS calculations.

keyword	description
	If during the ngrowsweeps, the sum of the discarded singular
	values for m retained states is lower than the value defined here,
	more block states will be discarded until the discarded sum
truncation_initial	increases to truncation_initial.
	Numerical format: $xe-y$ with x and y being integers.
	Example: truncation_initial = 1e-6.
	If during the nmainsweeps , the sum of the discarded singular
	values for m retained states is lower than the value defined here
	more block states will be discarded until the discarded sum
$truncation_final$	increases to truncation final
	Numerical format: xo-y with x and y being integers
	Example: truncation final = $10-6$
	Example. cruncacion_rinar – re o.
	Tells the program to compute the expectation values every
measure_each	$2 \times \text{measure}_\text{each sweeps.}$
	Defines the total symmetry group. Default is the combined spin-
	(SU2) and point symmetry group (PG) su2u1pg, where the
	pg-suffix should be omitted for better performance if the molecule
	is C1-symmetric. For test purposes, it is possible to switch off
symmetry	spin-adaptation, again with or without point group symmetry:
	2u1(pg) . In the latter case the keywords spin and nelec (see
	Section 6.2.1) have no meaning. Instead u1_total_charge1 and
	u1_total_charge2 corresponding to the number of up and down
	electrons have to be specified.
chim anch	Tells the program to update the checkpoint file every
спкр_еасп	$2 \times \text{chkp}_{-}\text{each sweeps.}$

Table 6 – continued from previous page

Table 6 – continued from previous page		
keyword	description	
	Occupation of the starting orbitals (e.g. Hartree-Fock occupation)	
	to be entered as a comma separated string of occupation aliases.	
	The aliases are defined as follows: $4 = \text{full}, 3 = \text{up}, 2 = \text{down},$	
	1 = empty. This information has to be entered in case of hf as	
hf_occ	init_state and for the CI-DEAS procedure [11, 4] as invoked by	
	dmrginit.py.	
	example: $hf_occ = "4,4,4,2,2,1"$ for a CAS(8,6) triplet state	
	setup where the unpaired electrons are "located" in orbital # 4	
	and $\#$ 5.	
	Number of sweeps in which truncation_final is used in the	
nmainsweeps	singular value decomposition.	
narousuoons	Number of sweeps in which $\texttt{truncation_initial}$ is used in the	
пятомрмесрр	singular value decomposition.	

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6.2.3 Keywords for expectation value calculations

QCMAQUIS can (in principle) compute expectation values for any one- or two-particle operator that can be formulated in second quantization. Table 7 comprises a list of the available property keywords in the release version of QCMAQUIS. For further updates/other properties please contact dmrg@phys.chem.ethz.ch. The one-particle reduced density matrix as well as the one-particle spin-density matrix are implicitly computed from the expectation values of some of the operators contained in MEASURE [ChemEntropy].

keyword	description
	All expectation values over the operators required to
	calculate the mutual information (as specified in Ref. [13])
MEASURE[ChemEntropy]	will be computed. Please note that this is available only for
	SU2 symmetry.
	Computes the one-particle reduced density matrix, without
MEASURE[1rdm]	the additional correlators contained in the ChemEntropy
	measurement.
MEASURE[2rdm]	Computes the two-particle reduced density matrix.
	Computes $\langle \psi op_i \psi \rangle$, $i = 1 \dots L$. Nup, Ndown and Nup*Ndown
<pre>MEASURE_LOCAL[name] = "op"</pre>	are meaningful choices for <i>op</i> . Available for 2u1(pg) only.
	Note: <i>name</i> defines the name under which the expectation
	values are stored on the resultfile.
	Computes $\langle \psi op_{1i} op_{2j} \psi \rangle$, $i = 1 \dots L, j = i + 1 \dots L$. Nup,
	Ndown, Nup*Ndown, cdag_up, cdag_down, c_up, c_down,
	cdag_up*Ndown, c_up*Ndown, cdag_down*Nup, c_down*Nup,
MEASURE_HALF_CORRELATIONS	cdag_up*cdag_down, c_up*c_down, cdag_up*c_down, and
[name] = "op ₁ :op ₂ "	$cdag_down*c_up$, as op_1 and op_2 are recognized by the
	program. Available for 2u1(pg) only.
	<u>Note</u> : <i>name</i> defines the name under which the expectation
	values are stored on the resultfile.

 Table 7: Expectation value calculations available in the release version of QCMAQUIS.

6.3 QCMaquis tools

QCMAQUIS comes with several tools that allow for example further manipulation of the MPS or to acquire additional wave function analysis information. The tools det2mps_"symmetry",

mps2ci and mps_transform(_"pg") will be briefly described in the following. These tools are
provided in the my-Molcas-build/qcmaquis/bin folder.

 $\label{eq:Table 8: Overview of QCMAQUIS tools.}$

tool	description
mps_transform(_pg)	This tool allows for a transformation of an $su2u1(pg)$ MPS
	wave function to 2u1(pg) symmetry.
	Command line:
	<pre>mps_transform(_pg) chkpfile</pre>
	<u>Note</u> : for an $su2u1(pg)$ MPS with $S > 0 2u1(pg)$ MPSs for
	all S_z components are generated.
	This tool generates determinants based on the CI-DEAS
	procedure [11] and inserts them in an MPS from which a
	new DMRG calculation can be started. Starting from such
	an MPS is likely to improve convergence behaviour and is
	loss prope to get stuck in local minime. The surrent
	implementation is described in Def. [4]. The number of
	Informentation is described in Ref. [4]. The number of
$det2mps_symmetry$	determinants will be chosen such that the maximal bond
	order at any site does not exceed the value set in
	init_bond_dimension. The new MPS will be stored in the
	checkpoint folder specified in chkpfile.
	Command line:
	det2mps_"symmetry" dmrg-input
	Note: "symmetry" must equal the total symmetry specified
	in the input file dmrg-input.
	This tool calculates the overlap between two MPS Θ_1 and
	Θ_2 , respectively, according to $\langle \Theta_1 \Theta_2 \rangle$.
	Command line:
<pre>mps_overlap_symmetry(_pg)</pre>	<pre>mps_overlap_"symmetry"(_pg) chkpfile_1 chkpfile_2</pre>
	Note: "symmetry" must equal the full symmetry specified in
	the input file dmrg-input.

Table 8 – continued from previous page

tool	description
	Given a text file determant_list.txt containing a list of
	determinant strings, this tool calculates the CI-coefficients of
	the respective determinants $[14]$. The determinant strings
	have to encode the occupation of the orbitals as described
	for the hf_occ keyword (4 = full, 3 = up, 2 = down,
mps2ci_2u1(pg)	1 = empty $).$
	Command line:
	<pre>mps2ci_2u1(pg) chkpfile determinant_list.txt</pre>
	<u>Note</u> : with the conversion tool $mps_transform(_pg)$ this
	analysis becomes possible also for MPS of the full symmetry
	su2u1(pg).

6.4 QCMaquis PYTHON scripts for wave function analysis and visualization

The python scripts of QCMAQUIS are helpful to analyze and visualize the results of a DMRG calculation. Their usage should be evident from the documentation strings in the PYTHON files. However, those that are most frequently used will be briefly explained here. All scripts except dmrginit.py take the QCMAQUIS output file resultfile as input. They are located in the folder my-Molcas-build/qcmaquis/lib/python/pyeval.

Table 9: Overview of QCMAQUIS PYTHON analysis and visualization scripts.

script	description
	Plots the energy for each microiteration.
	Command line:
sweeps.py	sweeps.py resultfile
	<u>Note</u> : use this tool to check the convergence wrt the number
	of sweeps.

script	description
	Starts a QCMAQUIS DMRG calculation with
	<pre>max_bond_dimension = 200 and nsweeps = 2, measures the</pre>
	entropy information $[15, 13]$ from this unconverged
	calculation and based on this, generates a new MPS with
	the CI-DEAS procedure according to all settings specified in
dmrginit.py	the input file dmrg-input. We recommend to use this script
	for the preparation of calculations for active spaces that are
	larger than those that can be handled with traditional CAS
	methods.
	Command line:
	dmrginit.py dmrg-input
	Optimizes the ordering based on entropy information as
	proposed in Ref. $[12]$. The current implementation is
	described in Ref. [4]. The ordering ensures that highly
	entangled orbitals are close to each other in the one
C · 17	dimensional lattice. The first ordering in the output ignores
fiedler.py	the point group symmetry of the orbitals, while the second
	version orders the orbitals within each irreducible
	representation and then reorders these symmetry blocks.
	Command line:
	fiedler.py resultfile
	<u>Note</u> : we recommend to use the second option.
	This script recovers the complete QCMAQUIS input file
	dmrg-input from a given resultfile.
input.py	Command line:
	<pre>input.py resultfile</pre>

script	description
mutinf.py	Produces mutual information plots $[13]$ given that an
	expectation value calculation for MEASURE[ChemEntropy]
	has been performed.
	Command line:
	mutinf.py resultfile
	Note: if orbital images (in .png format) named 1.png, 2.png
	\dots , L.png (with L being the number of active orbitals) are
	present in the same folder where mutinf.py is executed,
	they can be added to the mutual information plot by
	providing the optional argument -i to mutinf.py.

Table 9 – continued from previous page

7 Examples of Molcas DMRG and QCMaquis DMRG Input Files

7.1 Example file for Molcas – DMRG-SCF(14,10)

&GATEWAY 2Angstrom N 0.000000 0.000000 -0.54880 N 0.000000 0.000000 0.54880 basis=cc-pvdz &SEWARD &SCF &RASSCF DMRG RGinput **!!!!** QCMAQUIS Keywords input $conv_thresh = 1.0E-07$ nsweeps = 4 $max_bond_dimension = 100$ **!!!!** End of QCMAQUIS Keywords input endRG inactive = $0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0$ $RAS2 = 3\ 1\ 1\ 0\ 3\ 1\ 1\ 0$ ITER = 10,100&Grid_it all

7.2 Example file for QCMaquis– DMRG-CASCI(8,8)

//active-space dependent parameters L = 8nelec = 8// target symmetry (spin and spatial) of the wave function: $// 2^*$ spin = 0 (singlet) + totally symmetric point group irrep spin = 0irrep = 0//parameter to control the actual DMRG calculation nsweeps = 8 $max_bond_dimension = 256$ $conv_thresh = 1e-6$ // initialization procedure init_state = 'default' // technical parameters symmetry = 'su2u1pg' $integral_cutoff = 1e-40$ truncation_initial = 1e-50truncation_final = 1e-7chkpfile = 'chkp.h5'resultfile = 'result.h5' $integral_file = "FCIDUMP"$ storagedir = '/scratch/\$USER/boundaries' LATTICE = "orbitals" $lattice_library = "coded"$ $MODEL = "quantum_chemistry"$ $model_library = "coded"$ //all expectation value calculations required for entropy measures MEASURE[ChemEntropy]

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