The ABM Template Models A Reformulation with Reference Implementations

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Abstract

This paper refines a well-known set of template models for agent-based modeling and offers new reference implementations. It also addresses issues of design, flexibility, and ease of use that are relevant to the choice of an agent-based modeling platform.

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This paper has two core objectives: to refine a well-known set of template models for agent-based modeling, and to offer a new reference implementation. In pursuing these goals, we address issues of design, flexibility, and ease of use that are relevant to the choice of an agent-based modeling platform.

The use of agent-based models (ABMs) has been growing rapidly in many fields, including evolutionary biology, ecology, economics, epidemiology, game theory, political science, and sociology. Popular ABM platforms include NetLogo (http://ccl.northwestern.edu/netlogo/), Swarm and Java Swarm (http://www.swarm.org), Repast (http://repast.sourceforge.net), and MASON (http://www.cs.gmu.edu/%7Eeclab/projects/mason/). Each of these platforms has benefits and limitations that have been explored in the literature (Tobias and Hofmann, 2004; Railsback et al., 2006). The most popular of these platforms remains NetLogo, which is renowned for its combination good graphical capabilities, reasonable flexibility, and excellent of ease of use. Railsback et al. (2006) also judge NetLogo to be the most professional platform in terms of appearance and documentation. The most common complaint against NetLogo is its failure to adopt an open source license, which some researchers view as a crucial component of scientific ABM research.

Railsback et al. (2006) discuss a collection of sixteen template models, which they designed as tools to introduce and explore agent-based modeling (ABM) platforms. (Railsback et al. (2005) provide the full model specifications.) The template models are intended to be "ridiculously simplified". They illustrate general modeling considerations required by many different real-world applications and do not constitute an attempt to implement a specific real-world application. These template models have already proved their usefulness. They are used in teaching and are chosen as a point of reference for introductory presentations of new ABM platforms. Nevertheless, in this paper we propose to remove certain ambiguities, tighten certain specifications, remove from the specification some implementation details, highlight additional learning goals, and draw a clearer distinction between general programming goals and goals focused on the visual display of information.

Railsback et al. (2005) provide reference implementations of the template models for a few popular platforms. The template-model reference implementations are intended to be "simple and intuitive" rather than clever or fast. As might be expected, the reference implementations clarify the intent of certain parts of the specifications and highlight some of their limitations. The simplest and least verbose are the NetLogo reference implementations. Robertson (2005) notes that, as an ABM platform, NetLogo excels at ease of use and compactness of representation. This makes the NetLogo reference implementations particularly relevant as a point of comparison for other ABM platforms.

In this paper we provide new reference implementations. The reference implementations use the Python programming language. After modest initial start-up costs, our Python implementations of the template models prove simple, readable, and short. That is, they are useful as reference implementations. We show how use of a simple gridworld module allows for Python implementations that usually approach and often exceed the simplicity of NetLogo, while providing improved readability and power. Following the intent of the original reference implementations, our code emphasizes readability and ease of use (rather than speed or generality). We also suggest a few advantages and disadvantages of using Python as an ABM platform. Since NetLogo consistently receives high marks on these criteria, we take it as our primary point of comparison.

Template Model 1: Spatial Movement of Agents

The first template model provides a basic introduction to ABM platforms. The core programming goal is to implement the random movement of agents in a simple two-dimensional space. That is, we must implement a specified behavior for a base agent type that is spatially situated.

The background needed to attempt the first template model is platform dependent, but generally it requires a modest introduction to programming on the chosen ABM platform. Required skills include the use of basic built-in functions, definition and use of new functions, some understanding of variable scope (local vs. global), use of a looping construct, iteration over a collection (of agents), and simple randomization using built-in facilities.¹ With this background, we can attempt the specification of the first template model.

Specification: Template Model 1

World

• a 100 x 100 toroidal grid of possible agent positions

Setup

- create an iterable collection of 100 agents
- give each agent a unique, random position on the grid

Iteration

• each time step, each agent moves to a random, unoccupied neighboring location

Stopping Condition

• Not part of the specification.

Supplementary Detail

- agent positions are characterized by integer pairs (locations on the grid)
- no two agents share a position, not even initially
- agent movement is constrained to a Moore neighborhood of radius 4
 - an agent must change position unless all neighboring locations are occupied
 - the new position is a "random" selection from the unoccupied neighboring locations (no particular algorithm or PRNG is specified)
 - the move action must terminate, even if all neighboring locations are occupied
- the order in which agents move is unspecified, but agents must move sequentially (i.e., one at a time)
- a "time step" is one iteration through the model schedule

Display Suggestions

- position: display each agent on screen at a position corresponding to its grid position
- shape: display agents as circles
- color: use a red fill color for agents
- size: make sure adjacent agents are easily distinguishable
- update: display once each iteration

Despite its simplicity, the original specification contained some minor ambiguities. The emphasized text in our specification constitutes clarifying additions. We specify that the initial positions of agents are chosen randomly subject to the constraint that locations are not shared. This addition is not very consequential (and matches the NetLogo reference implementation). We also add that agents should be members of an iterable collection. Most ABM platforms support iterable collections for each agent type, so this too is not very consequential. More substantively, we explicitly specify that agents move sequentially. (This matches the reference implementations.) Sequential movement ensures that two agents do not move to the same location, and as Kahn (2007) notes, violation of this constraint can affect outcomes in later template models.

Finally, we explicitly specify that the move action must terminate. While this is the natural reading of the original specification, it conflicts with the reference implementations.² As Kahn (2007) notes, the reference implementations use a simple loop that makes repeated random draws from the entire neighborhood until a vacant cell is found. If there are no vacant cells, the program never escapes this loop. (Admittedly, this is a low probability event in the first template model.) However we do not augment the specification to require a specific algorithm, since the ease of any particular approach can be platform specific.

It is notable that the display suggestions have no essential relationship to the model specification. In fact, one drawback of the original template model specifications is the lack of a clean separation of core modeling goals and visual display considerations. We cannot address this fully without diverging substantially from the original specifications, but a natural supplement to the template models is a cleaner separation of these concerns. We will provide this on a template by template basis. One other drawback or the original specifications presumed an ecological emphasis and somewhat light-heartedly referred to their agents as "bugs". Our interest encompasses the social sciences, and we therefore stick with the more generic term 'agents'.

Procedural Implementation

To implement the first template model, we need a description of the agents and a description of the "world" in which the agents reside. The template models also make visual display suggestions, and we will implement these as well. With such limited needs, we have many different options. Starting from scratch is entirely feasible.³ Free and open source game development toolkits are also options: pygame (http://www.pygame.org) and pyglet (http://www.pyglet.org) are fairly simple and very powerful. For the purposes of this paper, however, we take a minimalist approach: we use a small gridworld module that provides a basic grid topology, "patches", and agents. Since Python 2.6, this approach provides ABM facilities that approach the simplicity of NetLogo.

The properties of an Agent resemble those of a NetLogo "turtle", which is the base NetLogo agent type.⁴ We will care primarily about the ability of these agents to report a current position and move to a new location. We will access and set the position of an agent via its position attribute. A position is an *x*,*y* pair of numbers, interpreted as Cartesian coordinates in a plane. (Generally, the coordinates can be floating point numbers, but for the template models they will be integers.)

To facilitate comparison with NetLogo, we consider a preliminary version of the first template model that is procedurally oriented. Our world will be a GridWorldGUI from the gridworld module; this class handles a little grid-related accounting for us. For example, if myworld is a GridWorldGUI instance, we can determine whether a location is unoccupied as myworld.is_empty(location). With this background, we get the following implementation of the first template model. (For completeness, we are including the entire file.)

```
""" Template Model 1 (procedural): Random Movement on a Toroidal Grid """
import random
from gridworld import Agent, GridWorldGUI
from gridworld import moore_neighborhood, Torus
def initialize(agent):
 agent.shape('circle')
 agent.shapesize(0.25, 0.25)
 agent.fillcolor('red')
def move(agent):
 choice = choose_location(agent)
 agent.position = choice
def choose_location(agent):
 old_position = agent.position
 hood = moore_neighborhood(radius=4, center=old_position)
 random.shuffle(hood)
 for location in hood:
   if agent.world.is_empty(location):
     return location
 return old_position
def schedule():
 for agent in myagents:
   move(agent)
#create a 100x100 grid and a world based on this grid
mytorus = Torus(shape=(100,100))
myworld = GridWorldGUI(grid=mytorus)
#create 100 agents, located in our world, and then initialize them
myagents = myworld.create_agents(AgentType=Agent, number=100)
for agent in myagents:
 initialize(agent)
```

for ct in range(250): #run the model (250 iterations)
 myworld.screen_updating = False
 schedule()
 myworld.screen_updating = True

Since this is our first model implementation, we will explicate the code. Readers with a little Python programming experience may be able to simply read through the code and then skip ahead to the more objectoriented implementation. (This invitation should not be taken for granted: it is a reasonable suggestion *because* readability is an explicit Python language design goal.)

The source file begins with a documentation string. (Python docstrings are conventionally triple quoted; triple quoted strings can include line breaks.) Immediately following the docstring are three import statements. The first imports the random module from the standard library, giving us access to Python's random number facilities. The other two import useful objects from the gridworld module. We import Agent and GridWorldGUI, two classes that will be useful for our simulation. After import, names are available for use anywhere in our program (i.e., they are in our module's global namespace). We also import the moore_neighborhood function, which can produce a Moore neighborhood of any specified radius, along with the Torus class, which characterizes a rectangular grid that wraps at its boundaries.

Our approach will be to define a collection of functions that we can use to implement the simulation.⁵ Our first function simply initializes an agent. This initialization focuses on the visual display of the agent: we set its shape, size, and color.⁶ We then attack the core of the first template model: the detailed description of how an agent moves. We define a move function, which chooses a new location and then moves the agent there. Location choice is delegated to a choose_location function. Movement to a new location is handled simply by assigning a new value to the agent's position attribute.

Let us consider the body of the choose_location function, which does the real work of the first template model. We generate a Moore neighborhood of radius 4 around the agent's current position as as moore_neighborhood(radius=4,center=old_position), which returns a list of eighty (x,y) locations. An agent must move to a random location in its neighborhood, so we shuffle (in place) the locations with the random.shuffle function. We sequentially consider each location as a possible new position (thereby avoiding the error in the reference implementations, discussed above). If the location is empty, we choose it. Note that a gridworld.Agent has a world attribute. (When a world creates agents it sets this attribute.) To determine whether a location is empty, an agent queries its world's is_empty method. If no new location is empty, the agent chooses its current position. The choose_location function returns a location, and the move function sets the agents position to this location.

We have completed the hardest and most essential part of the first template model. Our schedule function is relatively simple: it applies our move function to each of our agents. We will call schedule once per iteration as long as the model is running.

We are now ready to set up and run the model. Following the specification, we create our 100 by 100 grid as mytorus = Torus(shape=(100,100)). We then create our world as myworld = GridWorldGUI(grid=mytorus), initializing our world with our torus topology. We then populate the world with 100 agents: a GridWorldGUI also has a create_agents convenience method, so we need only specify the number and type of agents that we want. (Since we do not specify positions, the agents are positioned randomly when they are created.) We then use our initialize function to prepare the agents for our simulation.

Running the model is essentially a matter of calling the schedule function repeatedly. However we also perform a subsidiary, display-related task: we turn off screen updating before we start moving our agents, and we turn screen updating back on after we are done moving our agents. This was requested by the specification, and it substantially speeds the simulation. We arbitrarily stop after 250 iterations. (The specification does not include a stopping criterion.)

Object-Oriented Implementation

For illustrative contrast, we reimplement the first template model with more object-oriented code. We can again use Python, since it combines simplicity and power by supporting both procedural and object-oriented programming paradigms.

This time we use the GridWorldGUI and Agent classes of the gridworld module as base classes for two new classes, WorldO1 and AgentO1. Instead of defining four global functions to manipulate the objects in our model, we provide our objects with behavior by defining four corresponding methods. We initialize the shape, size, and color of our agents with an initialize method. We add a move method to our agents, which will be supported by a choose_location method. These are analogues for three of the four functions we defined in the procedural version. The fourth function was our schedule, which we now implement as method of our world class.

Before proceeding, we should note two features of the gridworld module. Agent defines an initialize method, intended to be overridden, which is automatically called as part of object initialization. Also, GridWorldGUI defines a schedule method, intended to be overridden, which is called repeatedly by its run method. So we propose the following design.

Agent01 extends gridworld.Agent

- New Methods: move, choose_location
- Overridden Methods: initialize

World01 extends gridworld.GridWorldGUI

• Overridden Methods: schedule

Here we use the term 'extends' to indicate inheritance: Agent01 is a subclass of Agent. To say that Agent01 extends Agent is to say that Agent01 inherits data and methods from Agent. Specifically, we will use the position and the world data attributes that Agent01 inherits from Agent. Similarly, we will use the is_empty method that World01 inherits from GridWorldGUI, which reports whether a given location is empty or occupied by another agent.

Explicit class definition has costs and benefits relative to other possible designs. The costs accrue primarily to programming novices, which make them largely of pedagogical relevance. (This matters, since pedagogy is a common use of the template models.) Object-oriented design requires an understanding of class definition. In Python, this is a minimal barrier: understanding how NetLogo handles instance variables (as required by the second template model) is a comparable cost.⁷ As a somewhat more substantial cost, object-oriented design immediately requires a minimal understanding of inheritance: that a derived class behaves like its base class, in the sense the it can receive the same method calls. As we develop our objectoriented approach to the first template model, we will not find large advantages off-setting this initial cost. However, as we work through additional template models, substantial advantages of a more object-oriented approach become evident.

For most researchers choosing an ABM platform, the issue is not whether but rather when to use inheritance. For example, NetLogo is strongly procedurally oriented and is designed for simple use, so the NetLogo reference implementations initially can dodge the issue by relying on a kind of dynamic attribute creation for the base agent class (using the turtles-own and patches-own keywords). But once a model requires different types of agents, a discussion of the NetLogo concept of breed becomes unavoidable. Any reasonable introduction to breeds will strongly overlap elementary discussions of class definition and inheritance.⁸

The NetLogo reference models do not introduce breeds until template model 16. We could similarly postpone the introduction of inheritance, as illustrated by our procedural version of the first template model. Postponement slightly decreases the background required to implement the first template model, but it does not change the requirements for the set of template models. Additionally, an object-oriented approach substantially simplifies the set of models. A comparison of our procedural implementation with the following permits an assessment of the barrier to entry is raised by early use of a more object-oriented approach.

```
""" Template Model 1: Random Movement on a Toroidal Grid """
import random
from gridworld import Agent, GridWorldGUI
from gridworld import moore_neighborhood, Torus
class Agent01(Agent):
 def initialize(self):
   self.shape('circle')
   self.shapesize(0.25, 0.25)
   self.fillcolor('red')
 def move(self):
   choice = self.choose_location()
   self.position = choice
 def choose_location(self):
   old_position = self.position
   hood = moore_neighborhood(radius=4, center=old_position)
   random.shuffle(hood)
   for location in hood:
     if self.world.is_empty(location):
       return location
   return old_position
class WorldO1(GridWorldGUI):
 def schedule(self):
   for agent in self.agents:
     agent.move()
if __name__ == '__main__': #setup and run the simulation
 #create a 100x100 grid and a world based on this grid
 mytorus = Torus(shape=(100,100))
 myworld = World01(grid=mytorus)
 #set up agents (create 100 agents, automatically initialized)
 myagents = myworld.create_agents(AgentType=Agent01, number=100)
 #run the world's schedule repeatedly
 myworld.run(maxiter=250)
```

A reasonable first reaction is that this more object-oriented implementation appears nearly identical to our procedural implementation. The four functions defined in the procedural version are clearly evident as the three methods defined in the Agent01 class and the one method defined in the World01 class. (A method definition is just a normal function definition that is part of a class definition.) A closer look reveals some small differences, and we focus on those.

Again the module begins with a short docstring. The three import statements are unchanged. We then define a new class, Agent01, which inherits from Agent and defines three methods. The initialize method has one difference from our earlier function of the same name: the parameter name is self rather than agent. This is is inessential: the choice of the name self is a standard Python convention to emphasize that when we call this method on an instance, it will act on that instance itself. (We will return to this.)

The move method also mirrors our previous move function. There is one notable difference: instead of the function call choose_location(agent), we have the method call self.choose_location().⁹ Similarly, the choose_location method is also essentially identical to our previous choose_location function.

So far we have introduced only very minor changes in program logic, but they all reflect a more fundamental change in perspective: behavior is now an attribute of an agent. To give this a slightly misleading but nevertheless suggestive phrasing, in the procedural design we do things to agents, whereas in the objectoriented design our agents do things.

Our remaining changes are just as minor. Instead of defining a global schedule function, we subclass GridWorldGUI and override its schedule method. The schedule method has three notable changes from our earlier function of the same name. First, we do not have to turn screen updating on and off. (We

will use the run method that our WorldO1 inherits from GridWorldGUI, which handles this for us.) Second, we will not access myagents as a global variable: instead we use the agents attribute of our WorldO1, which it inherits from GridWorldGUI. Finally, we replace the function call move(agent) with the method call agent.move().

As before, we must take four steps to run our first simulation: create a grid of locations for our agents, create a world based on that grid, populate the world with initialized agents, and run the scheduled actions repeatedly. Each of these steps is familiar, and only the last changes substantively from our procedural implementation. A WorldO1 has a run method (inherited from GridWorldGUI) that repeatedly calls its own schedule method, so myworld.run(maxiter=250) will run our simulation for 250 iterations. Our more object-oriented implementation of the first template model is complete.

We add one modification that is not needed to implement the model: we run the simulation only if __name__=='main'. This is a purely forward looking change: we want to import Agent01 and World01 into other modules without running our first template model. However, a module's code is executed when the module is imported. We could put the code to set up and run the model in a separate file, but for the purposes of this paper, we wish to group our class definitions beside the code that creates and runs our simulations. Our solution is to use the special module attribute, __name__, which is just the filename (as a string) for an *imported* module. In contrast, the module executed as the main program is always assigned the string '__main__' as its name. We can therefore condition on the value of __name__ in order to prevent some code from being executed when a module is imported. The code in the body of this if statement will not be executed if the module is imported, but it will be executed if the module is executed as a script.¹⁰ This ensures that we can freely import our module into other scripts.

Template Model 2: Agent Growth

The second template model assumes completion of the first template model. (The template models are generally sequential.) The new requirement is the addition of agent state in the form of data attributes. An associated visual-display goal is the provision of visual clues to the state of each agent.¹¹ Once again, the emphasized text in our specification constitutes additions or changes to the original.

Specification: Template Model 2

World and Setup

• unchanged from model 1

Iteration (sequential)

- each agent moves
- each agent grows

Supplementary Detail

- movement: agents move as in model 1
- growth: each agent "grows" at a fixed rate
 - each agent has an data attribute named $\verb+size+$
 - growth is a change in the "size" attribute
 - size is initialized to 1.0; the growth increment is 0.1

Display Suggestions

- position, shape, and update: as in model 1
- color: each agent's fill color should represent its "size". (Specifically, use white if size=0.0, red if size>=10.0, and increasingly chromatic tints of red as "size" increases from 0 to 10.)
- delay: ensure that the agents' color changes during the model's first ninety iterations are not too rapid for viewing

We clear up one ambiguity in the original specification, which says that the growth action "is scheduled after the move action". In accord with the NetLogo reference implementation, we interpret this to mean that all agents move, and after that all agents grow. We also cut the growth increment from 1.0 to 0.1. The growth increment is inessential to the model, aside from visual display considerations. Even after our change, on many platforms the color transition will take place too quickly to be easily seen, unless the model iterations are radically delayed. We therefore add a new display suggestion: schedule a delay if needed for comfortable viewing of the color transitions.

Note that the notion of **size** here is very abstract, and correspondingly so is the notion of **growth**. A biologist might conceive of **size** as the physical size of the agent, while a social scientist might conceive of **size** as the monetary value of the agent's wealth.

With this background, we propose a basic design. As we take up the second template model, we would like to take advantage of our work on the first template model. One approach to this is to simply copy our Agent01 code into the file that implements the second template model, modifying it where appropriate. Indeed, examination of the NetLogo reference implementations reveals the use of this copy-and-paste approach. For languages that support inheritance, a much better approach is to import into our second template model any useful objects from the first template model.¹² We therefore subclass Agent01 to define a new agent class (Agent02). that has a new data attribute (size) and two new methods (grow and change_color). Additionally, we create a new class, named World02, for our new schedule of actions. Since World01 does not offer much here, we again subclass GridWorldGUI in order to override its schedule method.

Agent02 extends Agent01

- New data attribute: **size**
- New Methods: grow, change_color
- Overridden Methods: initialize

World02 extends GridWorldGUI

• Overridden Methods: schedule

With this design in hand, we are now ready to implement the second template model. We begin with three import statements. We import the time module, which is in the Python standard library, so that we can use its sleep function to delay our model iterations. From the gridworld module we import two familiar classes, GridWorldGUI and Torus, along with an inessential but convenient function, ask. Analogously to the ask command in NetLogo, this ask function applies a specified method to each object in an iterable collection. (Thus ask(myagents, 'move') is equivalent to for agent in myagents: agent.move().) Finally, from our (obviously names) template01 module we import Agent01, which we intend to subclass.

```
""" Template Model 2: Agent Growth """
```

```
import time
from gridworld import ask, GridWorldGUI, Torus
from template01 import Agent01
class Agent02(Agent01):
 def initialize(self):
   self.shape('circle')
   self.shapesize(0.25, 0.25)
   self.size = 1.0
   self.change_color()
 def grow(self):
   self.size += 0.1
   self.change_color()
 def change_color(self):
   g = b = max(0.0, 1.0 - self.size/10)
   self.fillcolor(1.0, g, b)
class World02(GridWorldGUI):
  def schedule(self):
   time.sleep(0.2)
   myagents = self.agents
   ask(myagents, 'move')
   ask(myagents, 'grow')
```

```
if __name__ == '__main__':
  myworld = World02(grid=Torus(shape=(100,100)))
  myagents = myworld.create_agents(AgentType=Agent02, number=100)
  myworld.run(maxiter=100) # run simulation
  myworld.mainloop() # keep GUI open after `run` completes
```

Our new agent class, Agent02, has two new methods (grow and change_color) and a new data attribute (size). We initialize each agent's shape, shapesize, and size, and then we initialize its color by calling its change_color method. The change color method sets the agent's fillcolor based on its size, following the display suggestions in the specification.

The grow method is almost trivial: as required by the specification, an agent adds 0.1 to its size each time its grow method is called. Since the agent's color should always reflect its size, the grow method then calls the agent's change_color method. Using the default RGB color model, we specify colors as (red,green,blue) triplets of floating point numbers between 0 and 1. The intensity of red is always 1.0. The intensity of green and blue decreases from 1.0 to 0.0, as size increases from 0 to 10, and remains at 0 thereafter.

Agent02 is ready for use. We just need to create a collection of these agents and schedule their movement and growth according to the specification. As before, we approach this by defining a new class (World02), which subclasses GridWorldGUI in order to override its schedule method. We first schedule a brief sleep (i.e., a suspension of the program execution), which provides us with time to examine the current state of the visual display. The schedule method then retrieves an iterable collection of the agents, sequentially calls the move method on each of these agents, and then sequentially calls the grow method on each of these agents.

With our schedule in place, we can set up and run the simulation as in the first template model. We introduce one slight change: after we run the model, we call the mainloop method of our world. For now, this is just to keep our display visible after our simulation is done running. (We will return to this.)

We emphasize that our code listing is again complete. Although the second template model is slightly more complex, its code is no lengthier than that for the first template model. (Of course this is due to our import of Agent01.) This is a stark contrast to the NetLogo reference implementation of the second template model, where we find that code size increases rapidly with the complexity of the model. While brevity is no virtue if it sacrifices clarity, our Python code remains clear and readable. As early as the second template model, we discover an evident strength of Python as an ABM platform.¹³

Template Model 3: Spatially Distributed Resources

In comparison to the modest goals of the first two template models, the third template model is somewhat ambitious. The core programming goal is to introduce spatial resources in the form of spatially distributed "cells" with which agents interact. This interaction changes the state of the cell and the state of the agent. To make this concrete, we say that cells produce a resource, and agent growth is determined by the resource it extracts from its cell. A secondary goal is to introduce a random change in state: cells produce randomly.

We remove two requirements from the original specification: we do not require that a "grid space object" hold the cells, and we do not require that each cell store its occupant in an instance variable. We consider these to be implementation details that users would have trouble confirming on many platforms.¹⁴ Even when a model is implemented from the ground up, these are not sensible requirements: there are many competitive designs. (For example, a cell might delegate the determination of its occupants to an intermediary, which might maintain a mapping from cells to occupants.)

Furthermore, the rest of the specification (and its interpretive framework) make it more natural that an agent "know" its cell than that a cell "know" its agent. For example, in the NetLogo reference implementation a grow procedure is applied to each agent, which consumes from its cell and grows.¹⁵ We can conceive a more patch-centered approach—say, applying a supply-agent procedure to each patch—but this is not natural, necessary, or efficient.

Specification: Template Model 3

Setup

- same as model 2, plus
- create a "cell" for each grid location

Iteration (sequential)

- each cell produces, which adds to its available supply
- each agent moves
- each agent grows

Supplementary Detail

- production: random, uniform between 0 and the cell's maximum production rate
 - a cell has an available supply of the produced resource (data attribute, initialized to 0.0) and a maximum production rate (data attribute, initialized to 0.01)
 - a cell's production is added to its supply
- movement: agents move as in model 1
- growth: an agent grows by extracting from its cell
 - an agent can interact with the cell at its position (specifically, it can extract the cell's supply)
 - an agent has a maximum extraction rate (a data attribute, initialized to 1.0)
 - an agent extracts whichever is smaller: its maximum extraction rate, or its cell's supply
 - agent growth equals the quantity it extracts
 - a cell's supply is reduced by the amount extracted

Display Suggestions

• unchanged from model 2

As a minor matter, we have adopted a somewhat more general description of the agent and cell activities. The original specification suggested the following interpretation: cells grow food, which bugs eat to grow. However many other interpretations are possible. (For example, itinerant laborers solicit paid jobs, which add to their wealth.) Again, the interpretive framework of the template models is secondary: any serious application to interactions between an agent and its spatial environment will require many more details.

With this background, we are ready to propose a design. We need to describe a cell that produces something that can be taken by our agents. We also need to make some changes to our agent description, so that it can appropriately consume and grow.

Cell03 extends gridworld.Patch

- New Data: supply, max_produce
- New Methods: produce, give
- Overridden Methods: initialize

Agent03 extends Agent02

- New Data: max_take
- New Methods: extract
- Overridden Methods: initialize, grow

World03 extends gridworld.GridWorldGUI

• Overridden Methods: schedule

At this point, our basic strategy should be growing familiar. We inherit as much as we can from past work, and we add any new behavior we need. For example, Agent03 will inherit the patch_here method from Agent02, who inherited it from Agent01, who inherited in from gridworld.Agent. However, it must override the grow method rather than inherit it from Agent02. We now move to discussion of the code.

```
""" Template Model 3: Spatially Distributed Resources """
import random
from gridworld import ask, GridWorldGUI, Patch, Torus
from template02 import Agent02
class Cell03(Patch):
 def initialize(self):
   self.supply = 0.0
   self.max_produce = 0.01
 def produce(self):
   self.supply += random.uniform(0, self.max_produce)
 def give(self, amount):
   amount = min(self.supply, amount)
   self.supply -= amount
   return amount
class Agent03(Agent02):
 def initialize(self):
   Agent02.initialize(self)
   self.max_take = 1.0
 def grow(self):
   self.size += self.extract()
   self.change_color()
 def extract(self):
   mycell = self.patch_here()
   mytake = mycell.give(self.max_take)
   return mytake
class WorldO3(GridWorldGUI):
  def schedule(self):
   ask(self.patches, 'produce')
   ask(self.agents, 'move')
   ask(self.agents, 'grow')
if __name__ == '__main__':
 myworld = World03(grid=Torus(shape=(100,100)))
 mypatches = myworld.create_patches(PatchType=Cell03) #setup patches
 myagents = myworld.create_agents(AgentType=Agent03, number=100)
 myworld.run(maxiter=100)
 myworld.mainloop()
```

For now, the only important thing we get by having CellO3 inherit from gridworld.Patch is that a GridWorldGUI knows how to create instances of Patch. (We will use this when we set up the model.) All the important cell behavior is new. We begin by overriding the initialize method, which is automatically called during instance creation. This initializes the supply and max_produce attributes of each cell. We define a produce method to augment supply by a random amount, which is uniform between 0 and max_produce. And the give method will give from the cell's current supply the amount requested (up to the entire supply), while reducing the cell's supply by the amount given.

An Agent03 has all the initializations of an Agent02, and we invoke by calling Agent02.initialize. (This is for illustrative purposes: the gain from reusing the Agent02 initializations is tiny in this simple class.) An Agent03 is an Agent02 that knows how to extract resources from its cell and to grows based on this extraction. The grow method calls the agent's extract method, and growth equals the amount extracted. Given a call to its extract method, an Agent03 will try to extract its max_take (e.g., its maximum capacity). (Of course it can only extract up to its cell's current supply.) The max_take of an Agent03 is set at initialization to 1.0.

As usual, we create a schedule this by overriding the schedule method of GridWorldGUI. First we ask each patch to produce, then we ask each agent to move, and finally we ask each agent to grow (by extracting from its cell). With our schedule in place, we can set up and run our simulation as usual, with one small change. Before we create our agents, we must create their environment (i.e., the cells). (This step has no corollary in NetLogo, which always conveniently creates a patch environment for its agents, but it is required by most ABM platforms.) Note that the specification still does not include a stopping condition, so our decision to run the simulation for 100 iterations is in this sense arbitrary.

Template Models 4, 5, 6, 7: Probes, Parameters, Histograms, and Stopping

The next three template models emphasize the GUI. In principle the GUI is a mere adjunct to ABM platforms. In practice it has proved an important tool for model exploration and understanding. It therefore receives a strong emphasis in the template models.

Template Model 4: Click Monitors

The core task of the fourth template model is to implement click monitors, or "probes", fore both agents and cells. A click monitor displays the state of an object type when the object receives a mouse click. The specification is correspondingly simple.

Specification: Template Model 4

World, Setup, and Iteration

• unchanged from model 3 (with new supplementary detail)

User Interaction

• report agent size and cell supply in response to mouse clicks in the visual display

Display Suggestions

- as in model 3, plus
- display click monitor reports in the GUI

The ease of producing such probes varies substantially by platform. On some platforms it is a substantial effort to probe both agents and cells (Railsback et al., 2006). NetLogo once again makes things easy: probes for agents and cells are provided automatically and displayed in the GUI.¹⁶ We add probes explicitly using our world's add_clickmonitor method, which takes as arguments a label for the display, an object type to monitor, and an attribute (or attributes) whose values are to be monitored.¹⁷

```
""" Template Model 4: Probe Object State """
from gridworld import Torus
from template03 import Agent03 as Agent04, Cell03 as Cell04, World03
class World04(World03):
    def initialize(self):
        self.add_clickmonitor('Agent', Agent04, 'size')
        self.add_clickmonitor('Cell', Cell04, 'supply')

if __name__ == '__main__':
    myworld = World04(grid=Torus(shape=(100,100)))
    mypatches = myworld.create_patches(PatchType=Cell04)
    myagents = myworld.create_agents(AgentType=Agent04, number=100)
    myworld.run(maxiter=100)
    myworld.mainloop()
```

The resulting code is very simple. We simply reuse Agent03 and Cell03 (renamed as Agent04 and Cell04). We subclass World03 in order to override its initialize method. (Recall that the initialize method is special: it is called when our world instance is initialized.) This is where one adds probes, using the add_clickmonitor method. We add two click monitors: one to report the size of a clicked agent, and another to report the supply of a clicked cell.

The code for creating our world, adding cells and agents, and running the simulation is by now familiar. When we create our world, the two click monitors appear in the GUI (see Figure 1), and they display the current state of the objects we click. This highlights a new reason for calling the mainloop method of our world: the "main loop" is an event loop, which waits for and handles GUI events. In this case, it handles our mouse click events.

Template Model 5: Model Parameters

The fifth template model introduces user settable model parameters. While the concept is not precisely defined, the idea is that certain variables that govern the simulation should be easily settable by users of the model.

Specification: Template Model 5

Setup and Iteration

- unchanged from model 4
- Model Parameters
 - initial number of agents (suggested default: 100)
 - maximum extraction rate of agents (suggested default: 1.0)
 - maximum production rate of cells (suggested default: 0.01)

Supplementary Detail

• model parameters should be easily settable by users of the model.

Display Suggestions

- as in model 4, plus
- enable GUI setting of model parameters (e.g., with sliders)
- include SetUp and Run buttons in the GUI (where "SetUp" creates the agents (and patches if needed), and "Run" should run the simulation

We make two changes in the original specification. First, we do not *require* GUI parameter setting. While this can be quite useful for experimentation with the model, use of the GUI for parameter setting interferes with replicability, is an inefficient approach to testing model robustness, and is not a good ultimate practice in a research setting. We therefore demote this to a display suggestion. Second, we add to the display suggestions that provision of SetUp and Run buttons. This suggestion is a natural implication of allowing parameter setting in the GUI: the parameters values must be determined before the model can be set up and run. (Thus, for example, we find setup and go buttons in the NetLogo reference implementation.)

As Railsback et al. (2006) note, model parameters are often implemented as attributes of a model class. For the three specified model parameters, we introduce three class variables to our World05 class. Since patches and agents created by a GridWorldGUI know their world, they have access to these parameters as attributes of their world.

With this background, we expect that the primary change from the third template model is a change in the **initialize** methods of our cell, agent, and world classes. We add button and slider creation to the initialization of our world. During their initializations, cells and agents need to access the parameter values stored by their world. Correspondingly, we now move patch and agent creation into a **setup** method of our world.

```
""" Template Model 5: Parameters """
from gridworld import Patch, Torus
from template04 import Cell04, Agent04, World04
class Cell05(Cell04):
 def initialize(self):
   self.supply = 0.0
   self.max_produce = self.world.cell_max_produce
class Agent05(Agent04):
 def initialize(self):
   Agent04.initialize(self)
   self.max_take = self.world.agent_max_take
class World05(World04):
 n_agents = 100
 cell_max_produce = 0.01
 agent_max_take = 1.0
 def initialize(self):
   World04.initialize(self)
   self.add_slider('Initial Number of Bugs', 'n_agents', 10, 500, 10)
   self.add_slider('Agent Max Extraction', 'agent_max_take', 0.0, 2.0, 0.1)
   self.add_slider('Cell Max Production', 'cell_max_produce', 0.0, 0.1, 0.01)
   self.add_button('Set Up', self.setup)
   self.add_button('Run', self.run)
   self.add_button('Stop', self.stop)
 def setup(self):
   mypatches = self.create_patches(PatchType=Cell05)
   myagents = self.create_agents(AgentType=Agent05, number=self.n_agents)
if __name__ == '__main__':
 myworld = World05( grid=Torus(shape=(100,100)) )
 myworld.mainloop()
```

Let us focus on the initialize method of WorldO5. We begin by invoking all the WorldO4 initializations. Then we add three sliders, one for each of the model parameters that we introduced as class variables. The sliders allow users to set new values for these parameters. (This approach matches the NetLogo reference implementation.) A slider is created with the add_slider method, which needs a label, an attribute (of our world) to be set, minimum and maximum possible values for the attribute, and a resolution (i.e., minimum increment) for the slider. The values for these are not part of the specification, but clearly they should encompass the default parameter values.

We then add the two specified buttons. As a convenience, we also add a **Stop** button, although this is not required by the specification. Each button is created with the **add_button** method, which requires as arguments a label and a function. This function is called a "callback" (or "command"): it is called when the button is clicked. Our buttons call the **setup**, **run**, and **stop** methods of our world.

Our WorldO4 inherited run and stop methods from GridWorldGUI. We do not override these. It also inherited a setup dummy method, intended to be overridden. We override setup to create our patches and agents.

Recall that in template model 4 we saw that the mainloop method prepared our world to receive mouse clicks. Here too it sets up event handling, and now these events include button clicks and slider adjustments. We now use button clicks to set up and run the model.

Template Model 6: Dynamic Histogram

Agent-based models can generate a lot of data. Graphical summaries of the data can be helpful in understanding the model evolution and outcomes. The sixth template model addresses this need by requiring the production of a histogram to summarize the distribution of **size** among the agents.

We make a minor change in the original specification: we do not require that the histogram be displayed in the GUI, and we thereby remove the implicit requirement that histogram generation be synchronous with the simulation run. This reflects our view that the ability to synchronously view the histogram during a simulation run is a convenience rather than a fundamental feature of an ABM platform. (For example, MASON has no integrated graphing facilities, and lack of graphics documentation in Java Swarm suggests this is not yet a priority.) Indeed, saving data from simulation runs and analyzing it with separate tools is an reasonable and flexible approach to ABM assessment. We therefore demote GUI presentation of the histogram to a display suggestion.

Specification: Template Model 6

Setup, Iteration, and Model Parameters

as in model 5

Data Display

• produce a series of histograms that represents the evolution of the distribution of an agent attribute

Supplementary Detail

- the histogram should be of the size attribute of agents
- the sampling frequency for the histogram is not specified, but should be high enough to be informative about the evolution of this distribution

Display Suggestions

- use 10 bins for the histogram, with a minimum size of 0 and a maximum size of 10 $\,$
- display a histogram chart in the GUI, and update the histogram as the simulation runs

Fine graphics control will always be complex, but even the ease of basic graph creation varies substantially among platforms (Railsback et al., 2006). Once again NetLogo sets the standard for ease of basic use: to add a continually updated histogram of turtle size to the NetLogo GUI, just place histogram [size] of turtles in a procedure that will be called each iteration. The approach used by gridworld.py is only slightly more complex and very flexible.

```
""" Template Model 6: Histogram """
from gridworld import Torus
from template05 import Agent05 as Agent06, World05
class World06(World05):
    def initialize(self):
        World05.initialize(self)
        def get_sizes():
            agents = self.get_agents(Agent06)
            return list(agent.size for agent in agents)
        self.add_histogram('Agent Sizes', get_sizes, bins=range(11))
if __name__ == '__main__':
    myworld = World06(grid=Torus(shape=(100,100)))
    myworld.mainloop()
```

We add a dynamic histogram to the GUI with the add_histogram method of our world. This method needs as arguments a title for the graph and a function that will be recomputed each iteration. When called, this function must provide the data for the histogram. We therefore define a get_sizes function, which returns a list of agent sizes.¹⁸ In doing so, we add one forward looking refinement: we illustrate the get_agents method our world inherited from GridWorldGUI. This returns a list of the agents of the specified type. (Of course currently all of our agents are of type Agent06, so we get a list of all agents.) From this, we produce a list of the agent sizes. This is the data needed for our histogram. We create our world, set up the model, and run the simulation as before. Our histogram appears in the GUI, where it is updated each iteration.

Template Model 7: Stopping Condition

Template model 7 simply adds a stopping condition to template model 6. The condition is that the model iterations should stop when any agent reaches a **size** of 100 or larger.¹⁹

Specification: Template Model 7

Setup, Iteration, Model Parameters, and Data Display

• unchanged from model 6

Stopping Condition

• terminate iteration based on model state

Supplementary Detail

- base stopping condition on a cutoff for the agent $\verb"size"$ attribute
- the suggested cutoff is that any agent reaches size >= 100
- after stopping, completely exit the simulation

Display Suggestions

- as in model 6, plus
- close GUI when the simulation terminates

We scarcely change the original specification. As usual, we demote the GUI aspects to display suggestions. We also remove a reference to "clean up steps" to be done upon termination, because these steps were not specified (Railsback et al., 2006).²⁰

There are many ways to approach this problem, but the most straightforward is to add a conditional check to the schedule. (This is essentially the approach taken by the NetLogo reference implementation.) We test for the stopping criterion, and once it is satisfied, we stop the simulation and exit the program. Note that this approach is an implementation detail, and is not required by the specification. To stop the iterative process we use the **stop** method that our world inherited from **GridWorldGUI**; to exit the mainloop (and thus completely terminate the program) we use its **exit** method.²¹

```
""" Template Model 7: Stopping Condition """
from gridworld import Torus
from template06 import Agent06 as Agent07, World06
class World07(World06):
    def schedule(self):
        World06.schedule(self)
        if max(agent.size for agent in self.agents) >= 100:
            self.stop()
            self.exit()

if __name__ == '__main__':
    myworld = World07(grid=Torus(shape=(100,100)))
    myworld.mainloop()
```

Template Model 8: Output Files

Railsback et al. (2006) point out that producing data for subsequent analysis is a core facility for ABM platforms. For the eighth template model, we can break this into two parts: the production of summary statistics, and file input-output operations. In template model 8, each iteration, a summary of the agent states is computed and written to an output file.

We make a single substantive change in the original requirements: we drop the (implicit) requirement that output be written as plain text.²² Plain text output has the great advantage of being human readable, but when we generate a large amount of data this advantage is rapidly outweighted by speed (of reading and writing) and eventually even file-size considerations. (Vaingast (2009) offers a good introductory discussion.)

Even if we settle on a plain text file format, many issues are unaddressed by the specification. Will the data be written in a well-known format, such as the CSV format? (CSV is the most obvious format to use for plain text data storage, since it is a standard spreadsheet format, but it is not the choice of the reference implementations.) Will the data be documented in any way, at least with a file header (as is a common first row in CSV files)? These are general concerns for data generation and maintenance. While we do not attempt to force decisions into the specification, as the needs and resources of users vary widely, we do introduce some output *suggestions* into the specification.

Specification: Template Model 8

Setup, Model Parameters, Data Display, and Stopping Condition

• unchanged from model 7

Iteration (sequential)

- as in model 7
- compute summary statistics for the model
- write model summary to a file

Supplementary Detail

- summary statistics are for the **size** of agents
- summary statistics should *include* the minimum, mean, and maximum size

Output Suggestions

- open, append to, and close the output file each iteration
- write output as plain text
 - output from a single iteration is a single line in the text file
 - use CSV format for the output file
 - write a header as the first line in the log file

Display Suggestions

• as in model 7

Implementations of input-output facilities vary substantially: some platforms provide special classes to facilitate file output, but Java-based platforms usually expect users to use the basic Java file-handling facilities (e.g., the FileWriter class). As one expects, NetLogo provides fairly easy access to very basic facilities.²³ In contrast, Python's input-output facilities are not only easy to use but also very powerful. Additionally, they can be coupled with Python's powerful string manipulation facilities to produce nicely formatted plain text output.

We will use Python's basic file handling abilities, as implemented in the built-in open command.²⁴ We provide two arguments to open: a filename (as a string) and a mode (as a string). The basic text modes are 'r' (read), 'w' (write), or 'a' (append). For example, we can open the file sizes.csv for writing with the statement fh=open('sizes.csv', 'w'). (The open command returns a file object, which we bind to the name fh.) We can then write a string mystring to the file as fh.write(mystring).

We can implement the eighth template model simply by extending WorldO7. We add two new class variables (logfile and logformat), add two new methods (header2logfile and log2logfile), and override two methods (setup and schedule).

Our setup keeps the WorldO7 set up but appends logging of a header and an initial data summary to our log file. Data logging is handled by a new log2logfile method, which retrieves a list of agent sizes, gets the summary statistics, and appends them to our output file. We handle data description with describe, which is a gridworld convenience function.²⁵ This has functionally similar to Swarm's Averager class. It takes a list of numbers as its argument and returns a Python dictionary of descriptive statistics, with keys including the self-explanatory min, max, and mean. The expression self.logformat.format(**stats) uses our logformat string to format the corresponding values in the stats dictionary. (This offers a nice illustration of the power and flexibility of using a Python format string). This is all it takes to log our data in CSV format.

```
""" Template Model 8: Log Model State Information to File """
from gridworld import Torus, describe
from template07 import Agent07 as Agent08, World07
class World08(World07):
 logfile = 'c:/temp/sizes.csv'
 logformat = '\n{min}, {mean}, {max}'
 def setup(self):
   World07.setup(self)
   self.header2logfile() # write header to logfile
   self.log2logfile() # log initial state to logfile
 def schedule(self):
   World07.schedule(self)
   self.log2logfile()
 def header2logfile(self):
   logheader = "minimum, mean, maximum"
   fh = open(self.logfile, 'w')
   fh.write(logheader)
   fh.close()
 def log2logfile(self):
   agents = self.get_agents(AgentType=Agent08)
   sizes = list(agent.size for agent in agents)
   stats = describe(sizes)
   fh = open(self.logfile, 'a')
   fh.write( self.logformat.format(**stats) )
   fh.close()
if __name__ == '__main__':
 myworld = World08(grid=Torus(shape=(100,100)))
 myworld.mainloop()
```

We have one last change to make, and that is to the schedule. We begin with the schedule of World07, but we append to it the data logging we want to do for each iteration. With that adjustment, we are done with the eighth template model. We set up and run the simulation as before.

Template Models 9, 10, and 11: Randomization, Hierarchy, and Optimization

In the template models, each agent moves once each iteration. However, we have not specified the order in which agents they move. Neglecting this has different implications on different platforms. For example, the most commonly used iterable collection in NetLogo is the "agent set". Iteration over a NetLogo agent set retrieves agents in random order. (For example, when we **ask** a NetLogo agent set to take an action, the individual agents are asked in random order to take this action.) In contrast, the basic iterable collection of **gridworld** is a Python list, which is not randomized. However, **gridworld** provides separate **askrandomly** and **ask** functions, allowing us to explicitly state whether or not we want to shuffle our agents before making our method calls. This has some advantages: shuffling the agents is a computational expense, which we should incur on an as needed basis.

In the first eight template models, the one place order might matter is when we ask agents to move. (Since occupation is unique, when one agent moves to a cell, the next agent cannot move to that cell.) Randomizing the order in which agents move can help us avoid artifacts, such as unintended first mover advantages. The ninth template model specifies that agents move in random order. We make no changes to the original specification.

Specification: Template Model 9

Setup, Model Parameters, Iteration, Data Display, and Stopping Condition

• unchanged from model 8 (but with a new supplementary detail)

Supplementary Detail

• each iteration, the order in which agents move is randomized

After the eighth template model, implementation is of the ninth is trivial: in our schedule we simply change ask(self.agents, 'move') to askrandomly(self.agents, 'move'). So we will not repeat the code here. Instead we will focus on our implementation of the tenth template model, which requires a slightly larger change.

The tenth template model drops randomization of agent moves in favor of hierarchical priority: "bigger" agents get to move before "smaller" agents. (This will matter when we get to our next template model.) On a biological interpretation, this hierarchy might suggest an advantage of physical size. On a economic interpretation, the hierarchy might suggest an advantage of the wealthiest individuals when choosing from the available economic opportunities.

Specification: Template Model 10

Setup, Model Parameters, Iteration, Data Display, and Stopping Condition

• unchanged from model 8 (but with new supplementary detail)

Supplementary Detail

• the order in which agents move is determined by their **size** attributes: bigger agents move before smaller agents

Sorting is fairly simple on most ABM platforms. (Most use the built-in sorting facilities of their implementation languages.) Some require the user to implement a boolean comparison, and others want a sort key (i.e., a function whose values determine the sort order). For example, NetLogo's sort-by command requires a user implemented boolean comparison, while Python's sorted function takes a sort key.

```
""" Template Model 10: Hierarchy """
from gridworld import ask, Torus
from template08 import World08
class World10(World08):
 def sortkey10(self, agent):
   return agent.size
 def schedule(self):
   ask(self.patches, 'produce') #from model 3
   #version 10: agents move in size order
   agents = sorted(self.agents, key=self.sortkey10, reverse=True)
   ask(agents, 'move') #from model 1
   ask(agents, 'grow') #from model 3
   self.log2logfile() #from model 8
   if max(agent.size for agent in agents) >= 100: #from model 7
     self.stop()
     self.exit()
if __name__ == '__main__':
 myworld = World10(grid=Torus(shape=(100,100)))
 myworld.mainloop()
```

Implementation is of the tenth template model is a very small modification of the eighth: we just need to sort agents by size before they move. World10 therefore extends World08 by adding a new method, our sort key sortkey10. This takes an agent as its argument and returns the agent's size. We also override schedule in order to sort agents before they move. (The rest of the schedule should be familiar after our

work on the previous template models.) Python's built-in **sorted** function handles the sorting for us, once we specify our sort key. (Note that by default sorting is lowest to highest, so we set the **reverse** keyword argument to **True**.) With out **World10** definition in place, we set up and run the simulation as usual.

Template Model 11: Optimization

Recall that we defined a choose_location method for Agent01, which we did not subsequently override. Location choice has remained random. Such agents have very limited agency. In the eleventh template model, we add interest to our agents by adding optimization to their movement.

We remove a couple ambiguities in the original specification. Substantively, we make it clear that the hierarchical movement of model 10 still applies. As a minor matter, we resolve "ties" in a specific way: an agent's choice among multiple best cells is random. Of course, since each cell's **supply** is a random floating point number, the probability that tie resolution will be required is very low. (However, during the initial iterations of later models, ties will be much more likely.)

Specification: Template Model 11

Setup, Model Parameters, Iteration, Data Display, and Stopping Condition

• unchanged from model 10 (but with new supplementary detail)

Supplementary Detail

- agent movement is no longer random
 - an agent explores cell its neighborhood and moves to the cell that has the largest supply
 - an agent's neighborhood is still a Moore neighborhood of radius 4, but now the agent's current cell is included
 - in case of a tie, the agent moves to a random choice of the best cells

We will reuse our Cell05 class, renaming it to Cell11. We will essentially reuse our World10 class: World11 just overrides setup to use our new Agent11. The only substantial changes are to our agent class. Agent11 has two new methods: the new sortkey11 method, which provides a key for sorting cells by their supply, and an overridden choose_location method, which picks the best location in the agent's neighborhood.

```
""" Template Model 11: Optimization """
import random
from gridworld import Torus
from template05 import Agent05, Cell05 as Cell11
from template10 import World10
class Agent11(Agent05):
 def sortkey11(self, cell):
   return cell.supply
 def choose_location(self):
   hood = self.neighborhood('moore', 4)
   MyType = self.__class__
   hood4move = [ cell for cell in hood if not cell.get_agents(MyType) ]
   hood4move.append(self.patch_here())
   random.shuffle(hood4move)
   best_cell = max(hood4move, key=self.sortkey11)
   return best_cell.position
class World11(World10):
 def setup(self):
   mypatches = self.create_patches(PatchType=Cell11)
   myagents = self.create_agents(Agent11, number=self.n_agents)
```

```
if __name__ == '__main__':
    myworld = World11(grid=Torus(shape=(100,100)))
    myworld.mainloop()
```

We focus on this choose_location method. An Agent11 must choose the unoccupied neighboring cell with the greatest supply. So first we retrieve a list of all the cells in a Moore neighborhood of radius four. Then we filter out the occupied patches. (The expression cell.get_agents(AgentType) returns a list of the agents of type AgentType on cell, which has a boolean value of False if the list is empty.) We want the agent to consider its own cell as well, so we retrieve it with the agent's patch_here method (inherited from gridworld.Agent and append it to the list. Then we shuffle the list as a way to ensure that any "ties" will be resolved randomly. The best cell is the one with the greatest supply. We can use Python's built-in max function to do the maximization, as long as we supply an appropriate key (sortkey11) on which to base the comparison. Having discovered the best patch, choose_location returns its position. This is our agent's choice of the best location for its move.

Template Models 12 and 13: Entry, Exit, and Time-Series Plots

In some agent-based models, agents remain in the model during the entire simulation. Other models require that agents exit or enter the simulation as it runs. For example, "bugs" in a biological model may exit through death and enter via birth, or "firms" in an economic model may exit through bankruptcy and enter as new start ups. The twelfth template model illustrates this common need of agent-based simulations: existing agents have a fixed probability of exit, and new agents enter when existing agents "split".

We make two changes to the original specification. We addresses a potential first mover advantage to the **split** action by specifying that agents split in random order. We also remove some ambiguities by clarifying that new agents will not immediately exit and by specifying that an agent makes its attempts to split and *then* dies (implying that its position remains occupied during the split action).

Specification: Template Model 12

Setup and Data Display

• unchanged from model 11 (with new supplementary detail)

Model Parameters

- as in model 11, plus
- probability of agent exit (suggested default: 0.05)

Iteration

- as in model 11, then
- each "big" agent splits
- each "smaller" agent exits with a fixed probability

Supplementary Detail

- split: each agent of size > 10.0 makes five attempts to produce a new agent, and then exits
 - agents take the split action in random order
 - to produce a new agent requires finding an unoccupied location in a randomly searched Moore neighborhood of radius 3, where no more than 5 cells may be searched for each attempt to produce a new agent
 - $\ast\,$ when an unoccupied cell is found, it becomes the position of a new agent, and search terminates
 - $\ast\,$ if all five cells are occupied, search terminates, and the attempt to bring a new agent into the world fails
 - $-\,$ each new agent has initial size of $0.0\,$
- exit: each "smaller" agent (*except the new entrants*) exits the simulation with fixed probability
 the probability of agent exit is a model parameter

Stopping Condition:

• the number of agents reaches 0, or the number of iterations exceeds 1000

We approach the twelfth template model by very slightly extending World11 to implement our new schedule and by extending Agent11 to handle the split action and to accommodate a chance of exit. This leads to the following design.

Agent12 extends Agent11

• New Methods: split, propagate, chance

World12 extends World11

- New Data: agent_exit_probability
- Overridden Methods: schedule, setup

World12 is a very small extension of World11. As usual, we modify the setup method so that it creates agents and cells of from most recent classes. We also add a new class variable, agent_exit_probability, for our new model parameter.²⁶ Finally, we must append two agent actions (split and chance) to the World11 schedule, along with our new stopping condition.²⁷

```
""" Template Model 12: Entry and Exit """
import random
from gridworld import ask, askrandomly, Torus
from template11 import Agent11, Cell11 as Cell12, World11
class Agent12(Agent11):
 def split(self):
   if self.size > 10:
     self.propagate()
     self.die()
 def propagate(self):
   SplitClass = self.__class__ #splits share agent class
   hood4split = self.neighborhood('moore', radius=3)
   cells4split = list()
   for i in range(5): #5 attempts
     for cell in random.sample(hood4split,5): #5 tries per attempt
       if cell not in cells4split and not cell.get_agents(SplitClass):
         cells4split.append(cell)
         break
   splitlocs = list(cell.position for cell in cells4split)
   splits = self.world.create_agents(SplitClass, locations=splitlocs)
   for agent in splits:
     agent.size = 0.0
   return splits
 def chance(self):
   if self.is_alive:
     if random.uniform(0,1) < self.world.agent_exit_probability:</pre>
       self.die()
class World12(World11):
  agent_exit_probability = 0.05
 def schedule(self):
   World11.schedule(self)
   agents = askrandomly(self.agents, 'split')
   ask(agents, 'chance')
   if (self.iteration==1000) or (len(self.agents)==0):
     print self.iteration, len(self.agents)
     self.stop()
 def setup(self):
   mypatches = self.create_patches(PatchType=Cell12)
   myagents = self.create_agents(Agent12, number=self.n_agents)
```

```
if __name__ == '__main__':
    myworld = World12(grid=Torus(shape=(100,100)))
    myworld.mainloop()
```

Turning to Agent12, consider the new chance method. Each agent has an is_alive attribute which is set to False if the agent's dies method is called. ("Dying" is a model specific concept, which might represent physical death, failure of a firm, or even retirement of a worker.) The chance method draws from a standard uniform distribution and compares the draw to the agent_exit_probability model parameter. A small draw removes a "living" agent from the simulation; by default this happens five per cent of the time.

The real work of the twelfth template model is in the **split** action, where "bigger" agents propagate themselves and then die. Our very simple **split** method handles this by delegating propagation to a **propagate** method, which is where the real work takes place. Here we begin by specifying that successors (or "splits") will share the agent's type. Following the specification, we consider a Moore neighborhood of radius 3 as possible locations for these successors. We create an empty list to hold the cells that can accept successors — i.e., unoccupied neighboring cells. An agent gets five attempts to split (i.e., produce a successor), but for each potential successor the agent must find an empty cell within five tries. Each try is a random choice from the neighborhood. To implement this, we use the **sample** function of the **random** module to retrieve five random cells, which we check sequentially until we either find an empty cell or run out of options. This approach yields a list of empty cells, one for each successful split. We determine the position of each of these cells, and create the new agents at those locations. All that is left to do is to set the size of each new agent to zero, according to the specification.

Railsback et al. (2006) note that the twelfth template model is substantially more complex than the preceding models. They found themselves forced to resort to "clumsy and complex methods" on most platforms. The exception, once again, was NetLogo, and even so their NetLogo reference implementation is nearly 300 lines of code. Additionally, the closed-source nature of NetLogo proved problematic. While adding and removing agents during a simulation is very simple in NetLogo, they found the documentation inadequate to determine whether an agent will execute its actions in the same iteration that it was created.²⁸ Our Python implementation of the twelfth template model relies completely on open source code, is not "clumsy", and avoids disheartening complexity (despite a nested loop that in turn nests a conditional branch).

Template Model 13: Time-Series Plot

The time-series behavior of the state of a simulation model is often interesting and informative. For example, starting with template model 12, we may wish to examine how the number of agents changes over time. The thirteenth template model requires the production of a time-series plot of the number of agents. The focus is visual data analysis: such plots can help us to understand the evolution of the simulation.

Specification: Template Model 13

Setup, Iteration, and Model Parameters

• as in model 12

Data Display

- as in model 12, plus
- produce a time-series plot that displays the evolution of a model statistic over time

Supplementary Detail

- the plot should display the number of agents "alive" at each iteration
- update frequency for the plot is not specified, but the update frequency should be high enough to be informative about the evolution of this distribution

Display Suggestions

• display the plot in the GUI, and update it as the simulation runs

As a minor relaxation of the specification, we do not require that the plot be displayed in a GUI. This removes an implicit requirement that plot generation be synchronous with the model run and demotes GUI presentation of the plot to a display suggestion. Our reasons are unchanged from those given for model 6.

With that background, let us add a time-series plot to our GUI. NetLogo again epitomizes ease of use for very basic plots: to add a plot of the number of turtles to the NetLogo display, just place plot count turtles in a procedure that will be called each iteration.²⁹ The gridworld approach is similar and very flexible: use the add_plot method of our world (as inherited from GridWorldGUI), which needs as arguments a title for the graph and a function that will be recomputed each iteration. This function must provide a single data point for the plot.

```
""" Template Model 13: Time-Series Plot """
from gridworld import Torus
from template12 import Agent12 as Agent13, World12
class World13(World12):
    def initialize(self):
        World12.initialize(self)
        def number_living():
            return len(self.get_agents(Agent13))
        self.add_plot('Number of Agents', number_living)
if __name__ == '__main__':
    myworld = World13(grid=Torus(shape=(100,100)))
    myworld.mainloop()
```

To implement the thirteenth template model, we make no changes to Agent12, which we rename as Agent13. Our World13 is just a World12 with two items appended to its initialization: the addition of a time series plot (using addplot), and the definition of the function number_living. This function, which we provide as an argument to addplot, simply returns the number (len) of agents in the simulation at the time it is called. This completes the thirteenth template model.

Template Model 14: Randomized Initializations

One of the great strengths of agent-based modeling is that we have no need for a representative agent. Randomization can be a natural way to introduce initial heterogeneity. The object of the fourteenth template model is to illustrate the randomization of agent initialization. Each initial agent draws an initial size from a normal distribution, with mean and standard deviation that are user settable. The specification then requires that size be truncated at a minimum of zero.

Specification: Template Model 14

Model Parameters

- as in model 13, plus
- mean of distribution of sizes of initial agents (*default:* 0.1)
- standard deviation of distribution of sizes of initial agents (default: 0.03)

World, Setup, Iteration and Stopping Condition

- as in model 13, plus
- the initial agents are initialized with a random $\verb"size"$
 - $\verb"size"$ is based on a draw from a normal distribution
 - mean and standard deviation of this distribution are model parameters
 - if the size draw is less than 0.0, it is set to 0.0

${\bf Display} \ Suggestions$

- as in model 13, plus
- allow GUI setting of the new model parameters

We make one substantive clarification of the original specification, which said only that a check is introduced to limit size to a minimum of zero. This could mean that negative draws are set to zero or alternatively that negative draws are discarded in favor of a new draw (i.e., a truncated normal distribution). We remove this ambiguity by adopting the first interpretation as the simplest reading of the original specification.³⁰ Our only other change is the usual demotion of GUI parameter setting to a display suggestion.

Our agent type and world type will be largely identical to those in template model 13. Word14 has two new parameters, which we name agent_size_mean and agent_size_sd. As usual, we introduce these parameters as class variables, which are initialized with the specified default values. World14 reuses the initialize method of World13 and then appends two sliders corresponding to the new parameters. (We discussed the add_slider method in the fifth template model.)

```
import random
from gridworld import Torus
from template13 import Agent13, World13
class Agent14(Agent13):
 def initialize(self):
   Agent13.initialize(self)
   mean = self.world.agent_size_mean
   sd = self.world.agent_size_sd
   size_drawn = random.normalvariate(mean, sd)
   self.size = max(0.0, size_drawn)
class World14(World13):
  agent_size_mean = 0.1
 agent_size_sd = 0.03
 def initialize(self):
   World13.initialize(self)
   self.add_slider('Init. Size Mean', 'agent_size_mean', 0.0, 1.0, 0.1)
   self.add_slider('Init. Size SD', 'agent_size_sd', 0.0, 0.1, 0.01)
if __name__ == '__main__':
 myworld = World14(grid=Torus(shape=(100,100)))
 myworld.mainloop()
```

""" Template Model 14: Randomized Initializations """

Most ABM platforms provide a fairly extensive collection of distributions for (pseudo) random number generation. The **random** module of the Python standard library provides a variety of distributions including the normal. We use the **normalvariate** function to initialize our first collection of agents.

Agent14 overrides only the initialize method of Agent13. We keep all of the Agent13 initializations, and we then set the agent's size randomly. An agent retrieves the mean (agent_size_mean) and standard deviation (agent_size_sd) from its world, draws from a normal distribution with these parameters, and then sets its size to the maximum of this draw or 0. Once we have defined our new world and agent classes, we are ready to create a World14 instance and enter its main loop as usual.

Template Model 15: Data-Based Model Initialization

The fifteenth template model makes no fundamental changes in the characterization of agents or cells. However it requires that cell production rates be based on a data file. The data in this file provides a production rate at each location, and the shape of the grid must be determined by the listed locations.

Making the model set-up depend on data read from a file is the core change in the model, but the specification includes a few additional changes: agents must choose randomly among their best possible moves, agents are located on a bounded rectangular grid (instead of a torus), cell production is no longer random, and cells should change color to reflect their supply. While these are fairly minor changes, including them all does lengthen the specification of the fifteenth template model.

Specification: Template Model 15

World

• a rectangular grid of possible agent locations

\mathbf{Setup}

- read in a given file of cell data
- determine the grid shape based on the cell data
- create a rectangular grid (not a torus) based on the shape implied by the cell data (see below)
- create a patch for each grid location
- set a production rate for each patch based on the cell data
- create agents as in model 14

Model Parameters, Iteration, and Stopping Condition

• as in model 14 (but with new supplementary detail)

Supplementary Detail

- cell data file (from http://condor.depaul.edu/~slytinen/abm/):
 - the unzipped file format is plain text
 - the first three lines are header information (to be discarded)
 - each additional line provides three *space-delimited* numbers: an *integer* x coordinate, an *integer* y coordinate, and a *floating point* production rate.
- Moore neighborhood: on a rectangular grid (instead of a torus) our neighborhood definition must change: locations off the grid are now unavailable (instead of wrapping)
- movement: an agent randomly resolves "ties" for best cell
- production: each iteration a cell produces the amount specified by the file of cell data (i.e., production is no longer random)

Display Suggestions

- as in model 14, plus
- display cells in the GUI
- base a cell's color on its supply
- a cell is green when supply is 0.5 or higher and shades to black as supply goes to 0

Other Suggestions

• if the platform does not easily allow dynamic setting of the grid size, preset the grid size using the grid shape implicit in the data file, which is 251 ('x' values of 0 to 250) by 113 ('y' values from 0 to 112)

We make few changes to the original specification. Most substantively, we remove the implementation details for random "tie" resolution, as we consider implementation details extraneous to the specification. The randomization itself is important to avoid movement artifacts (Railsback et al., 2005). Similarly, we do not require that the change in the grid (from torus to rectangle) be implemented as a change in the move method of agents, since agents might have direct access to an appropriately constrained neighborhood. Finally, we add a few details about the cell data file format, and we demote display specifications to suggestions.³¹

We are ready to propose a design using new world and cell types. Cell15 extends Cell03 by adding a change_color method and overrides initialize to set an initial color. It also overrides the produce method to make production deterministic. World15 is just World14 with a slightly more complex setup method, since our set up depends on the cell data we must read from a file.

Cell 15

- inherits data and methods from Cell03 $\,$
- New Methods: change_color
- Overridden Methods: initialize, produce

World15

- inherits data and methods from World14
- Overridden Methods: setup

Note that we need not change the move method of our agent. One reason is that our implementation of template model 11 already correctly handles tie resolution. The other reason is a convenience of the gridworld module: an Agent has a neighbors method that queries its world, correctly handling the topology of that world. (E.g., for a Torus, it returns a list of patches that includes locations that "wrap" on the torus, while for a RectangularGrid patches beyond the boundary are not returned.) As a result, our agent description does not change at all.

```
""" Template Model 15: Data-Based Initialization """
from gridworld import RectangularGrid
from template03 import Cell03
from template14 import Agent14 as Agent15, World14
def read_celldata(filename):
 location2value = dict()
 maxx, maxy = 0, 0
 fh = open(filename,'r')
 for _ in range(3):
   trash = next(fh) #discard 3 lines
 for line in fh:
   x, y, prodrate = line.split()
   x, y = int(x), int(y)
   maxx, maxy = max(x,maxx), max(y,maxy)
   prodrate = float(prodrate)
   location2value[(x,y)] = prodrate
 location2value['shape'] = (maxx+1,maxy+1)
 return location2value
class Cell15(Cell03):
 def initialize(self):
   self.supply = 0.0
   self.change_color()
 def produce(self):
   self.supply += self.max_produce #no longer random
   self.change_color()
  def change_color(self):
   r = b = 0
   g = min(2*self.supply, 1.0)
   self.set_fillcolor(r, g, b)
class World15(World14):
  def setup(self):
   celldata = read_celldata('Cell.Data')
   shape = celldata.pop('shape')
   self.set_grid(RectangularGrid(shape=shape))
   patches = self.create_patches(PatchType=Cell15)
   for (x,y), prodrate in celldata.items():
     patches[x][y].max_produce = prodrate
   myagents = self.create_agents(Agent15, number=self.n_agents)
if __name__ == '__main__':
 myworld = World15(grid=None)
 myworld.mainloop()
```

We do not gain much in having Cell15 inherit from our previous cell types. We reuse the give method we implemented for Cell03, but we override the initialize and produce methods. Our new initialize method simply sets an initial supply of zero, as before, but then changes the cell's color to match its supply. Our new produce method deterministically (instead of randomly) augments the cell's supply and then

changes the cell's color to match its new supply. (Note that max_produce now denotes this deterministic production level.) The new change_color method is used to set the cell's color to a shade of green, as specified. Once again we set the colors via the default RGB color model, which we discussed during the specification of the second template model.

World15 is identical to World14 except for the new setup method. As part of setup, we read the cell data from file using the helper function read_celldata.³² This reads each line of the cell data file, discarding the first three and collecting the data from the others. It returns a Python dictionary mapping locations to production rates. It also computes the implicit shape of the grid but keeping track of the maximum values for each coordinate. We set our world's grid to a RectangularGrid (no longer a Torus), with dimensions based on the discovered shape. We then create our patches and set max_produce for each patch based on the data. As the final step in our setup, we create our agents. At this point we are read to create our world and enter its main loop, as usual.

Template Model 16: Interacting Agents of Different Types

The core programming goal of the sixteenth template model is to introduce a new agent type that can interact with our previous agent type. This interaction changes the state of one or more cells and the state of the agents. To lend concreteness, we will say our agents are hunters and prey.

Specification: Template Model 16

Model Parameters, World, and Setup

- as in model 15, plus
- create 200 randomly distributed "hunters"
- Iteration (sequential)
 - as in model 15, then
 - each hunter hunts

Stopping Condition

• as in model 15

Supplementary Detail

- a cell may contain a hunter and a prey
- hunting: hunters randomly search for prey and "kill" the first found
 - search randomly samples (without replacement) a Moore neighborhood of radius 1, center included
 - if *another* hunter is found in a cell, search terminates, and the hunter and remains at its current location.
 - if another hunter is not found in a cell, but a prey is found, search terminates, and the hunter moves to the cell and "kills" the prey
 - if no neighboring cell contains another hunter or a prey, the hunter moves randomly to an unoccupied cell
 - prey are removed from the simulation as soon as they are "killed"

Display Suggestions

- as in model 15, plus
- hunters are colored yellow with the classic (arrowhead) shape

Our changes to the original specification are primarily an effort to reduce ambiguity. Kahn (2007) points out an important ambiguity in the original specification: does search terminate whenever a hunter is encountered during cell search, or only if a prey is encountered *and* there is already a hunter in its cell? We follow the reference implementations and adopt the first interpretation.³³ Also, the original specification simply refers to the "immediately neighboring cells" of a hunter, but we specify that this is a Moore neighborhood of radius 1. This is the apparent intent of the original wording, and it matches the NetLogo reference implementation. A substantive clarification is that we specify that search terminates if *another* hunter is found during the search.³⁴ As a very minor change, we remove the implementation detail that random search be implemented

with a shuffled list and replace it with the underlying requirement that sampling from the neighborhood be done without replacement. Finally, we remove the pointless requirement that prey be created before hunters, we add a display suggestion for the color and shape of the hunters.

Our implementation reuses Agent15, now renamed as Prey. Our World16 overrides the schedule and setup methods of World15 and make no other changes. And we introduce a Hunter class that extends our basic Agent class with a new hunt method.

```
""" Template Model 16: Interacting Agents of Different Types """
import random
from gridworld import Agent, ask, askrandomly, Torus
from template15 import Agent15 as Prey, Cell15 as Cell16, World15
class Hunter(Agent):
 def initialize(self):
   self.fillcolor('yellow')
   self.shapesize(0.75,0.75)
 def hunt(self):
   hunthood = self.neighborhood('moore', radius=1, keepcenter=True)
   random.shuffle(hunthood)
   change_position = True
   for patch in hunthood:
     hunters = patch.get_agents(AgentType=Hunter)
     prey = patch.get_agents(AgentType=Prey)
     if hunters and not self in hunters:
         change_position = False
         break
     elif prey:
       prey.pop().die()
       self.position = patch.position
       change_position = False
       break
   if change_position:
     newcell = random.choice(hunthood)
     self.position = newcell.position
class World16(World15):
 def schedule(self):
   ask(self.patches, 'produce')
   prey = self.get_agents(AgentType=Prey)
   prey = sorted(prey, key=self.sortkey10, reverse=True)
   ask(prey, 'move')
   ask(prey, 'grow')
   askrandomly(prey, 'split')
   ask(prey, 'chance')
   hunters = self.get_agents(Hunter) #model 16
   askrandomly(hunters, 'hunt') #model 16
   self.log2logfile()
  def setup(self):
   World15.setup(self)
   hunter_locations = self.get_random_locations(200)
   hunters = self.create_agents(Hunter, locations=hunter_locations)
if __name__ == '__main__':
 myworld = World16(grid=None)
 myworld.mainloop()
```

Our new Hunter class overrides the initialize method of Agent simply to set a color and size. The real work is in the new hunt method. A hunter starts by retrieving a neighborhood for hunting. This

is shuffled. The hunter begins searching with the variable change_position set to True: we will negate this upon encountering another hunter or upon moving to the position of a discovered prey. The hunter sequentially considers each patch in the shuffled neighborhood, retrieving a list of hunters and a list of prey from that patch. Each list might be empty. If the hunters list contains another hunter, search terminates and the hunter does not change position. Otherwise, if the prey list contains a prey, search terminates and the hunter moves to that position and "kills" the prey. If no hunters are encountered and no prey found in the entire neighborhood, the hunter moves to a random cell in the neighborhood.

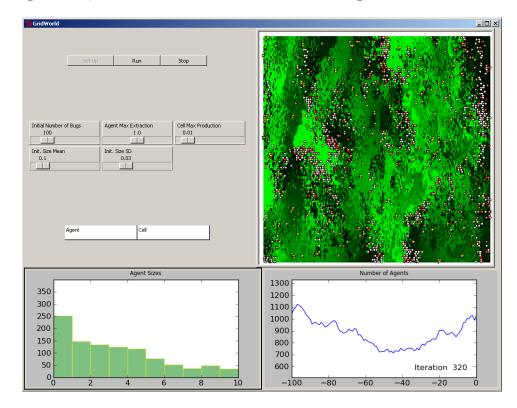


Figure 1: Figure 1: Template Model 16, GUI Display

Our new World16 class retains all the initializations and parameters of World15. It also reuses the setup method, but appends the creation of 200 hunters at random locations. The real change is in the schedule, although that too is largely familiar. We still have patches produce and agents (prey) move, grow, split, and (possibly) exit. Only the next two statements are truly new: we need to retrieve a list of hunters and ask them to hunt. Since there can be a first mover advantage in hunting, the hunters hunt in random order. We create our world and run the simulation as in model 15. Figure 1 captures the state of the GUI during a model run that keeps the default parameter values.

Conclusion

The template models discussed by Railsback et al. (2006) have proven useful to instructors and researchers for ABM platform introduction and comparison. So have the reference implementations of (Railsback et al., 2005). However they contain some ambiguities, weaknesses, and errors. Rather than propose a new set of template models, we attempt to refine the existing set, and we provide a new, supporting reference implementation.

Reference implementations are important for removing remaining ambiguities in the specification and for providing concrete illustrations of implementation strategies. We present readable reference implementations that can serve these purposes. Our reference implementations retain the original emphasis on being "simple and intuitive" rather than clever or fast. However we also address issues of design, flexibility, and ease of use that are relevant to instructors and researchers choosing an agent-based modeling platform. Specifically, we explore some of the costs and advantages of taking an object-oriented approach to the template models. We provisionally conclude that the primary cost is a slight front-loading of the skill set needed to begin modeling and that the (somewhat language specific) benefits can include reusability, maintainability, compactness, clarity, and readability.

Railsback et al. (2005) conveniently provide reference implementations for a variety of platforms. In comparison, the Python implementations introduced by this paper are more compact, readable, and correct. They therefore provide a useful code resource for those who wish to utilize the template model specifications. Additionally, they add to the literature on the choice of ABM platforms. Our reference implementations show how a general purpose programming language such as Python can be readily exploited as a very powerful and yet easy to use ABM platform.

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Notes

¹ We therefore assume readers have read an introduction to Python. See Kuhlman (2008) for a quick introduction, Isaac (2008) for a narrower but more applied introduction, or Zelle (2003) for a textbook introduction. We also refer to some basic NetLogo, which is quickly introduced in (Izquierdo, 2007). Note that we use the term 'function' to refer to callable subroutines of any type, even when a specific platform may adopt a different terminology.

 2 The original specification says that if an occupied location is selected, "then another new location is chosen". However, for the reference implementations, the phrase "another new location" was evidentally interpreted as "a new random draw from the entire neighborhood" rather than "a *new* (i.e., different) random draw from the neighborhood", so we are more explicit.

 3 To start entirely from scratch, we could implement basic agents, patches, and worlds as Python classes. We could also implement a visual display environment using the Tkinter graphical user interface (GUI) toolkit, which is part of the Python standard library. Even though Tkinter is extremely simple to use, presenting a GUI toolkit is an unnecessary burden for the present paper. Those interested in examining such an approach should look at Swampy (Downey, 2009). We should also mention SLAPP, a recent Python implementation of the Swarm protocol (Terna, 2009). (The standard reference for the Swarm protocol has become (Langton, 1996).)

⁴ The gridworld module is at http://econpy.googlecode.com/svn/trunk/abm/gridworld/gridworld.py. The agents provided by the gridworld module are based on the Turtle class of the turtle module, which is part of the Python standard library. Like NetLogo, but unlike most other ABM platforms, Python provides a basic agent class (in its turtle module) along with automatic visual display of the agent instances. It depends (for graphs only) on Matplotlib, a popular free and open source Python graphics library. Matplotlib in turn depends on NumPy, a popular free and open source scientific computing library. These libraries are very simple to install on common platforms and are widely used in scientific computing. It is worth noting that the turtle module implements separate classes to isolate the movement and positioning methods from the drawing methods, making it easy to implement agent-based models without visual displays. Since the template models emphasize visual display, we will not explore this further. However, readers may wish to examine the excellent online turtle.py documentation, especially the documentation of the motion methods.

⁶ An overview of function definition can be found in the Python tutorial: http://docs.python.org/tutorial/controlflow. html#defining-functions

⁶ We call the **shape** method to set the shape, the **shapesize** method to set the size of this shape, and the **fillcolor** method to set the fill-color of our agent. If we were working directly with a **turtle.Turtle**, we would also want to which ensures that an instance begins life with its pen up (so that it is not drawing as it moves) and its speed set to 0 (i.e., to "jump", so that it is moving at maximum speed). However a **gridworld.Agent** handles these initializations for us.

⁷ For an introduction to class definition, see the tutorial discussion: http://docs.python.org/tutorial/classes.html# a-first-look-at-classes

⁸ See http://ccl.northwestern.edu/netlogo/docs/dictionary.html#breed. Note that a NetLogo turtle can change breeds. (So a breed is essentially an instance attribute of a NetLogo turtle.)

⁹ Note that no argument is passed. If myagent is an instance of Agent01, then myagent.move() and Agent01.move(myagent) mean the same thing. This means that the first parameter of a method definition is special: when the method is called on an instance, the first argument is automatically provided, and it is the instance itself. The first parameter name is (conventionally) called self for this reason. This sometimes feels a little peculiar to programmers coming from other languages, but most Python programmers come to feel that it is an excellent, explicit design choice. Python uses self roughly like *this in C++ or the this reference in Java and C#, except that it is never implicit.

¹⁰ For an extended discussion of this strategy, see (van Rossum, 2003).

¹¹ Inexplicably, the Netlogo reference implementations delay adding these color changes until template model 3.

 12 When appropriate, we would like to honor the DRY principle ("don't repeat yourself"), which provides an important rule for the production of maintainable code. A good discussion of the DRY principle can be found in (Hunt and Thomas, 1999). Note that NetLogo does not offer convenient mechanisms for class definition and reuse, although recent versions allow some reuse through file inclusion.

¹³ Improved compactness of the code base may be achievable in NetLogo 4.1 by using the experimental <u>__includes</u> keyword. (For example, procedure definitions can be grouped together for inclusion.)

¹⁴ Even when relatively easy to confirm, as with the gridworld module, the information is fundamentally irrelevant to the user. Railsback et al. (2006) discuss how their specified design was picked as "easiest" for the MASON, Repast, and Swarm implementations, again confirming that it is just an implementation detail. Note that neither of the deleted requirements would make much sense to a user of the NetLogo platform. NetLogo users do not worry about creating a grid space, since Netlogo automatically creates patches, and users can simply apply the turtles-here command to a patch (or turtle) without worrying how this is implemented.

¹⁵ The NetLogo reference implementation does not use the turtles-here command nor even the patch-here command. It relies instead on a convenient but very implicit NetLogo feature: a procedure call on a turtle that uses data attributes owned by patches will access, and alter, that turtle's patch's values.

 17 As a result, there is no separate NetLogo reference implementation for the fourth template model.

 17 One may also include any keyword arguments appropriate to a Tkinter label widget, which gives substantial control over the appearance of the click-monitor display. By default, monitors are updated each iteration, but click monitors always display the value obtained at the last click.

¹⁸ Here we define **get_sizes** in the body of our **initialize** method, taking advantage of Python's support of closure, but we could alternatively have added a new **get_sizes** method to **WorldO6**.

 19 Kahn (2007) notes that the Netlogo reference implementation erroneously stops at a size of 1000. This affects nothing of substance in this template model.

 20 In the present context, we can imagine two interpretations of possible clean up: resetting the model in order to begin a new simulation run, or housekeeping prior and subsequent termination of the process running the simulation. The NetLogo reference implementation addresses neither of these. The first interpretation conflicts with the instruction to close the graphics windows. The second should be otiose with any modern operating system. For example, memory used by the simulation should be released back to the operating system when the process running the simulation terminates.

²¹ Note that the **stop** method of a **GridWorldGUI** simply sets that world's <u>stop</u> attribute to **True**, and this attribute is tested each iteration by the **run** method. One implication is that we can call stop anywhere in the schedule, and the schedule will still be completely before the the model run terminates. (If stopping with only partial execution of the schedule is desired, we can of course add a **return** statement to our conditional branch.)

 22 We also suggest opening, appending to, and closing the file each iteration, so that a model crash does is less likely to cause data loss. A minor change is that we make it clearer that the *minimal* amount of information to be written each iteration is the minimum, mean, and maximum size. More information can be written at the user's discretion. For example, the NetLogo reference implementation also writes currentTime, which is simply the iteration number, and also writes a header at the top of the file.

 23 A difficulty for new users will be learning to distinguish between file-write, file-type, and file-print.

²⁴ This is the best match to the reference implementations. However it is worth noting that the Python standard library includes the csv module, which makes it particularly simple to write CSV files. In this paper we do not introduce the csv module, but interested readers should consider the csv.DictWriter class.

²⁵ Use of describe is for purposes of illustration: we are logging only the minimum, mean, and maximum agent size, which we could readily compute with Python's built-in functions as min(sizes), sum(sizes)/len(sizes), and max(sizes). This is essentially the approach of the NetLogo reference implementation, although NetLogo also provides mean as a built-in command.

 27 The original specification parameterized survival probability, which is the complement of our exit probability. Note that we have already addressed setting parameters in the GUI, so in parallel with the NetLogo reference implementation, we will not do that here.

 27 We do not need to worry about the model 7 stopping condition, as model 12 agents never reach the size cutoff for that to apply. Therefore for presentational simplicity, we can just ignore it. Although the NetLogo reference implementation inexplicably uses a different stopping codition, but we do not alter the specification to match that.

 28 The NetLogo 4 user manual now clarifies this: only agents in the agent set at the time the **ask** command executes will run the commands.

²⁹ The default behavior of a NetLogo plot is to continually add points, which make the plots uninformative during long simulation runs. The time-series plot provided by gridworld provides a window on the most recent iterations, which is arguably more informative.

 30 Unfortunately, the NetLogo reference implementation of the fourteenth template model does provide guidance as it does not conform to the original specification. The initial agents are given size 1.0 instead of a random size, new agents are given a random size instead of a size of 0.0, and the random size is not truncated at 0.0.

 31 Kahn (2007) notes a couple problems with the Netlogo reference implementation of the fifteenth template model. Of some importance, the Netlogo implementation neglects to drop the random determination of the production rate. A minor problem is that patch coloring in the Netlogo implementation does not follow the display suggestion. We note in addition that the Netlogo implementation does not set the grid size based on its reading the file of cell data.

 32 Note that Python can simply iterate over the distributed .zip file, but we stick the the apparent presumption in the specification that the compressed text file will be unzipped before use. We name the decompressed file Cell.Data.

³⁴ As Kahn notes this has some odd implications. (Adjacent hunters will remain stationary until prey comes within range.) Experimenting with alternatives to this specification will be a natural extension of the sixteenth template model.

 34 For example, the NetLogo reference implementation first asks if there are hunters on a cell, and then asks if there are prey. Since hunting stops if a hunter is found (there is no identity testing), in that implementation, a hunter will never find a prey on its own cell. However the NetLogo implementation also errs in not including that cell in the list of neighbors, so a hunter will never search its own cell in any case.